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MODELLING THE POTENTIAL DISTRIBUTION OF TREE SPECIES ON A NATIONAL SCALE IN COLOMBIA: APPLICATION TO *PALICOUREA ANGUSTIFOLIA* KUNTH AND *PALICOUREA GUIANENSIS* AUBL. Modelación de la distribución potencial de especies arbóreas a escala nacional en Colombia: una aplicación para *Palicourea angustifolia* Kunth y *Palicourea guianensis* Aubl.

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ABSTRACT

The results in this study illustrate the methods of using the existing species' present records and environmental data to produce a niche-based model based on Mahalanobis distances, and also to predict the distribution of a number of tree species in order to apply it on a national scale to a tropical country such as Colombia. The technique applied is based on the Mahalanobis distance, a generalised squared distance statistic. We used environmental data integrated into a GIS, and a georeferenced collection of localities of Palicourea angustifolia and Palicourea guianensis to produce and test the predictive models. We used record data for Warszewiczia coccinea to validate the model. The two Palicourea species show largely complementary potential ranges. P. angustifolia shows a clear Andean distribution with a presence in lower and upper mountain areas but not in the highlands or in the inter-Andean valleys. P. guianensis was predicted throughout most of the lowland areas of Colombia including lowland Amazonian forests, and most of the tropical savannas of Orinoquia. The model predicted an overlapping distribution of the two species of 93.9 km². The Mahalanobian approach contributes to the development of biogeographically oriented modelling that makes the best use of the available data in data-scarce regions (such as most of the tropics). The technique provides key information about the environmental niche of the species being modelled, and allows comparisons between the species. The prediction achieved for the two species was considered satisfactory.

Key words. Colombia, GIS, Mahalanobis distance, ecological niche, *Palicourea*, predictive distributions model.

RESUMEN

Este estudio presenta una metodología para usar datos existentes actuales ambientales y de presencia de especies para producir un modelo de nicho ecológico basado en las distancias de Mahalanobis -un estadístico de distancia generalizada ajustada- y también para predecir la distribución de especies arbóreas a escala nacional en un país neotropical como es Colombia. Se utilizan datos ambientales integrados en un Sistema de Información Geográfica, y una serie localidades georeferenciadas de registros biológicos de Palicourea angustifolia y de Palicourea guianensis para producir y probar los modelos predictivos desarrollados. Las dos especies de Palicourea demuestran una distribución complementaria. P. angustifolia tiene una distribución claramente andina con presencia en áreas de montaña bajas y medias, pero no en la alta montaña ni en los valles inter-Andinos. Los resultados de la predicción de distribución para P. guianensis indican presencia en tierras bajas, incluvendo bosques amazónicos, y algunas zonas de la Orinoguia. La predicción del modelo indicó que existe un sobrelapamiento en la distribución de las dos especies con una superficie de 93.9 km². El uso de la prueba de Mahalanobian contribuye al desarrollo d ela ciencia de la biogeografía ya que permite modelar patrones de distribución en regiones con poca o escasa información. La técnica presentada aquí proporciona información importante sobre el nicho ambiental de la especie que es modelada, y permite comparaciones de patrones de distribución entre especies. Para concluir, los modelos de ambas especies aquí estudiadas pueden considerarse como satisfactorios.

Palabras clave. Colombia, SIG, distancia Mahalanobis, nicho ecologico, *Palicourea* sp., modelo predictivo de distribución.

INTRODUCTION

Predictive distribution models are an important tool for understanding factors that control species distributions, and have been broadly used in biogeography, ecology, conservation planning, and natural resources management (Busby, 1986, 1988; Box et al. 1993; Anderson et al. 2003; Farber & Kadmon, 2003). Such models have been developed for temperate areas (Carpenter et al. 1993; Franklin, 1995; Austin & Meyers, 1996; Bolliger et al. 2000; Felicisimo et al. 2002; Scott et al. 2002); however, tropical regions, where the areas harbouring the highest biodiversity remain, have rarely been the subject of such studies, specially South America. It is in the tropics, and specially in the sparsely inventoried neotropics, that these models can be of a major value, and have their greatest potential (Stockwell & Peters, 1999; Anderson et al. 2003, Hernández et al. 2006; Hijmans & Graham, 2006).

Rapid assessments of biological diversity and its geographical distribution are required to develop sound conservation policies, but particularly for a basis from which to start monitoring biodiversity change toward the 2010 biodiversity target of reduced rates of biodiversity loss agreed at COP 7 of the Convention on Biological Diversity (CBD, 2000). However, monitoring requires a baseline inventory, and a full inventory is practically impossible to achieve in biologically rich countries with significant wilderness areas. such as Colombia. Information is incomplete and tends to be biased toward accessible sites and specific taxa (Bojorquez et al., 1993). The great expense of new inventories requires the full utilisation of the limited physical and biological data that already exist in order to design the optimal strategy for further inventory.

Primary biological inventory data exist in the tropics, in the best of cases, as georeferenced coordinates from localities where scientists from museums, universities, or herbaria have collected specimens for their study. Most of this data are held in museums and herbaria around the world, and if repatriated and organised as a georeferenced record, it can provide a considerable database for better understanding of species distributions (see webs of INBIO in Costa Rica and CONABIO in Mexico). This information is usually in the form of a record of observation and rarely contains data indicating either absence or abundance at collection sites, specially in poorly sampled tropical regions (Peterson & Cohoon, 1999; Anderson et al. 2003). Most of the current modelling approaches require both presence and absence of data for their estimation. Moreover, many of these have been applied using mostly climatic data (Busby, 1988; Carpenter et al. 1993; Jones et al. 1997; Smith et al. 1997; Peterson & Cohoon, 1999; Robertson et al. 2001; Wilds et al. 2000;), despite the fact that spatially detailed landscape data (elevation, slope gradient, slope aspect, soils, geology, land cover) are now widely available at coarse spatial resolutions, and are clearly important in determining species distributions (Velázquez et al. 1996; Pérez.Vega et al. 2008).

Techniques which can be applied using only presence records are much less developed (Robertson et al. 2001; Carpenter et al. 1993; Gower, 1971; Anderson et al. 2003). In this study we present the application of a technique for mapping potential species distributions that utilises presence data for the prediction, and that is based on the Mahalanobis distance or generalised squared distance statistic (Clark et al. 1993; Knick & Dyer, 1997; Knick & Rotenberry, 1998). One of the most important advantages of this technique is undoubtedly the ability to cope with the presence of data only, thus making no a priori assumptions about the distribution of the species, and also avoiding the use of potential false negatives (Dunn & Duncann, 2000). In addition, the approach developed here allows the implementation of environmental variables' input from multiple sources of continuous, categorical, or Boolean data (Bar-Hen & Daudin, 1995). Further, the possible different scales of measurement of input variables do not have any effect since the

Mahalanobis statistic is dimensionless, being a function of standardised variables (Clark, *et al.* 1993; Knick & Rotenberry, 1998). Neither does it assume a normal distribution of the data, a normality that for most of the species is not satisfied (Austin & Smith, 1989). Nevertheless, its properties are best known when the assumption of multinormality is correct (Knick & Dyer, 1997). Last, the model developed here is firmly grounded in the niche theory that suggests the existence of optimal environmental conditions for species (Hutchinson, 1959; MacArthur, 1968; Whitaker, 1975).

Facilitating a strategic, cost-effective, and rapid inventory of Colombian biodiversity requires tools that use existing data to help focus on those areas in which the greatest diversity can be observed (and conserved) for the least cost, and to identify regions in which high diversity and rapid environmental change are in conflict. Given the rate of land use change and other forms of development in the Colombian countryside, and the lack of human and economic resources for wholescale inventory, some rapid sciencebased techniques for prioritisation of inventory and management activities are essential. Modelling species distributions has the potential to provide a much more spatially comprehensive assessment at the national scale than traditional point, plot, and transect-based studies, but will never be as reliable as field measurement, only more practical over large areas, or when there are reduced funding and other resources constraints. The main assumptions behind the modelling undertaken here are that:

[—] the principles of the species' fundamental niche theory (Hutchinson, 1957) are correct.

[—] on the national scale, environmental factors such as climate and topography control the distribution of species, and are more important than more local

ecological factors (such as competition). The heterogeneity and variability of Colombian climates and landscapes features can be described adequately for the purposes of species distribution modelling at a 1km grain and using globally available datasets.

— tree species distributions (under natural land cover) are controlled by these climatic and landscape drivers over other ecological interactions.

THE STUDY AREA

Colombia has a continental area of approximately 114 million hectares, representing 0.7% of the world's land surface. Colombia is geographically a variable country. The western part is mostly mountainous (45% of the territory) with the Andes which comprises of three cordilleras. However, most of the country is lowland plains located below 500 m. Due to its altitudinal variability determined by the presence of the three longitudinal mountain ranges, there is a diversity of climates. A diversity of geological and soil units are also associated with these cordilleras and their variable climates. Although its flora and fauna are only partially inventoried, Colombia is thought to contain 10% of the world's biodiversity (in terms of vertebrate & plant species) making it one of the most biologically diverse regions in the world (IAvH, 1998; IAvH, 1998a). Colombia hosts a great variety of ecosystems including forests, savannah, arid ecosystems, and wetlands, and 50% of the area is still under natural cover.

METHODOLOGY

The objective of this research was to develop and apply in Colombia a methodology that successfully uses existing species' presence records and environmental data in a nichebased model to predict the distribution of the tree species. The general methodological approach of this research is summarised in Fig. 1, as a combination of environmental and biological species data collection, computerbased spatial modelling of environmental parameters, and a multivariate modelling procedure developed to predict species distributions.



Figure 1. General methodological approach

Environmental data

Ten environmental variables from a countrywide GIS dataset at the resolution of 1km² (Armenteras, 2003) were analysed to construct the potential distribution model for the species. These consisted of seven continuous variables: mean, maximum, and minimum monthly temperatures (°C), mean annual precipitation (mm), mean annual solar radiation (W m-2), annual potential evapotranspiration (mm), slope gradient (%), and three categorical variables: soil type, geology class, and slope aspect class. Climatic variables were modelled (Armenteras, 2003) by interpolating from point meteorological station datasets (Jones, 1991). SOLARFLUX (Rich et al. 1995) was used for modelling solar radiation receipt, and the Thornthwaite method provided the annual

potential evapotranspiration (Armenteras, 2003). Slope gradient and slope aspect class were derived from the GTOPO30 DEM (USGS, 1996). Soil information was obtained from the Colombian Agustin Codazzi National Geographic Institute (IGAC). The soil map was constructed from regional and local studies all over Colombia and generalised at 1:1.500.000 into a national soil map by IGAC (1982). Geological information came from the South American Land Cover characteristics database of the EROS Data Center DAAC (USGS, 1996). All of the above factors have been shown to be indicators of potential physiological processes in trees such as growth and establishment (Table 1). Slope gradient is also an indicator of the variation of climatic properties within a cell since it is a measure of the within-cell range of elevation.

Table 1. Known associations between climatic and landscape properties and plant processes affecting species' distributions.

Variable	Mechanism of control on tree physiology	References
Temperature, mean	Controls rate of metabolic reactions according to Q_{10}^{-2} , controls water stress through evaporative demand, controls heat stress. Affects rates of photosynthesis, respiration, transpiration, and water absorption.	Johnson & Thornley, 1985; Woodward, 1987; Fitter & Hay, 2002, Enquist & Leffler, 2001
Temperature, min	Chilling stress, freezing stress, drought stress	Tranquillini, 1979; Begon et al. 1990; Cavieres et al. 2000
Temperature, max	Heat stress, drought stress	Johnson & Thornley, 1985; Hale & Orcott, 1987; Forseth & Norman, 1993; Saxe <i>et al.</i> 2001
Rainfall	Water availability, actual evapotranspiration (AET) and thus stomatal aperture and carbon uptake. Soil waterlogging and root respiration and inhibition. Drought stress	Longman & Jenik, 1987; Woodward, 1987; Whigham et al. 1990; Worbes et al. 1999; Cavelier, 1992; Swaine, 1996; Leigh, 1999; Enquist & Leffler, 2001; Laurance et al. 2001; Fitter & Hay, 2002
Solar radiation	Photosynthetically active radiation and thus productivity, also heat stress and drought stress	Harper, 1977; Bazzaz & Picket, 1980; Longman & Jenik, 1987; Woodward, 1987; Clark & Clark, 1994; Reich, 1995; Barone, 2001; Fitter & Hay, 2002
Potential evapotranspiration (PET)	Temperature and water stress, stomatal aperture	Stephenson, 1990
Slope gradient	Soil moisture dynamics, nutrient leaching, waterlogging, treefall dynamics, light distributions, resource partitioning	Hubbell & Foster, 1986; Brady, 1990; Moore et al. 1991; Basnet, 1992; Johnston, 1992; Austin & Meyers, 1998; Clark et al. 1998, Miyamoto et al. 2003
Soil	Water availability, nutrient availability (specially N and P), toxicity	Harper, 1977; Tanner, 1977; Begon <i>et al</i> . 1990; Swaine, 1996; Vitousek, 1984; Sollins, 1998, Tanner <i>et al</i> . 1998; Clark <i>et al</i> ., 1999; Baker <i>et al</i> . 2002, Phillips <i>et al</i> . 2003.
Geology	Nutrient availability, soil properties	Sollins, 1998
Slope aspect	Solar radiation, wetness	Brady, 1990; Moore <i>et al.</i> 1991; Austin & Meyers, 1998

Modelling the Potential Distribution of trees

Species data

The available biological data on species distribution was compiled from national and international collections and museums including the collection at the Humboldt Institute Herbarium (CB); Missouri Botanical Garden (MO); Herbario Jardín Botánico "Joaquin Antonio Uribe" in Medellín (JAUM); Instituto de Investigación Científica del Valle del Cauca (INCIVA); New York Botanical Garden (NYBG); Herbario Amazonico Colombiano (COAH); the Herbario Nacional Colombiano (COL) at the Instituto de Ciencias Naturales (ICN) and Herbario Alfonso Fernandez Perez (HAFP). Many records were georeferenced by the original collector often using 1:500.000 topographic maps (IGAC, 1970–1085), while others were georeferenced according to the collection site name using cartography available for the site. All records were converted to the same coordinate system for this study: Geographic, decimal degrees, WGS 1984 Datum and integrated with the ARCVIEW GIS (ESRI Inc., 1998).

We focused on modelling the distribution of species of the family Rubiaceae because they are well-studied, are ecologically and taxonomically diverse with high species richness, and abundant in many ecosystems. Rubiaceae are amongst the families with the highest number of species in Andean and humid tropical forests in Latin America (Taylor, 1999; IAvH, 1999a). Rubiaceae are also well-understood taxonomically (Taylor, 1999; IAvH, 1999a) and are ecologically important: most of the species of Rubiaceae, specially of the genera Psychotria and Palicourea, are important sources of food for animals (IAvH, 1999a). This family has been relatively well-sampled geographically (Lozano, 1994; Anderson, 1995; IAvH, 1999a; Taylor, 1999, Rangel-Churrio, 1995, 2000: Rangel-Churrio et al. 1997). Finally, new data becomes available with almost

every new field expedition being undertaken in Colombia.

To develop the predictive distribution model, we focused on two of the species that had more than 50 presence records: *angustifolia* Kunth 1818 (Rubiaceae) and *Palicourea guianensis* Aubl.1775. The first species belongs to the subgenus *Montanae*, and is generally found at higher elevations between 1,000–3,500 m (Taylor, 1997a, b). The second species belongs to the subgenus *Palicourea*, and is a widespread lowland species (Taylor, 1997a, b) generally found at lower elevations of 0–1,200 (1,500) m. We also used collection information for another lowland species of this family, *Warszewiczia coccinea*, to be used for validation purposes of the results.

Modelling approach

The approach used for the construction of potential distribution models is based on the Mahalanobis statistic (De Maesschalck *et al.* 2000), and has the following underlying assumption: given a set of environmental variables and a set of known species' locations, a training set can be built to define a multivariate space (m) that best describes the areas where a given species (j) is found and which may thus represent the "ideal conditions" for the species. The results can then be used to identify areas of the country where the environmental conditions are most similar to those of the "ideal" multivariate space for the species.

The Mahalanobis distance for mapping the potential habitat of species has been used successfully by Clark *et al.* (1993) and Knick & Dyer (1997). The Mahalanobis statistic can be used when there is only presence data, whereas other multivariate methods such as logistic regression or discriminant analysis require data on areas where the species is known to be present and also absent (Dunn & Duncan, 2000). In addition, Mahalanobis

distances are the sum of the squares of uncorrelated standardised variables; this means that assumptions of multivariate normality do not have to be met (Clark et al. 1993). Indeed, the method corrects for correlation between the different variables which are compensated for by an estimated covariance matrix (C) used to create new uncorrelated variables (Hand, 1981; Duda, 1997). The Mahalanobis statistic is also dimensionless since it is a function of standardised variables (Hand, 1981; Duda, 1997). Mathematically, the Mahalanobis distance from a vector x to a mean vector m is defined as: $r^2 = (x-m)^2 C^{-1} (x-m)$, where C is the covariance matrix for a set of observed vectors and has been explained in earlier studies (Duda, 1997; Farber & Kadmon, 1993), and so we will not discuss it in detail here. For a given species, the vector *m* represents its "optimum environmental conditions". An index of similarity for a site can be obtained by calculating the distance from those sites which are characteristic to the vector *m* using the Mahalanobis statistic

To estimate the Mahalanobis distances, C and m have to be calculated by performing a step-by-step matrix algebra amongst map layers containing environmental parameter information. We used an Avenue routine in ARCVIEW that automates this step and also assigns a Mahalanobis distance to every 1 x 1 km² grid cell in the study area. Areas with higher similarity have a smaller distance than those that differ more from the environmental characteristics of the presence data locations.

To model tree species distribution using this approach, the available presence data for the species were split into training and testing datasets (Figure 2) using three different ratios of parameterisation to validation data chosen based on different percentages of total dataset to understand the effect of the parameterisation dataset size on the simulation quality better. Table 2 summarises the number of records used for running a predictive model, and also the records set aside for validation purposes for each species. The three ratios were used to construct ten random sets of presence records resulting in a total of thirty different model sets (ten for each ratio) per species. For validation purposes, absence for a species was inferred using the localities with no known record for it but where two other species of the same family had been collected: for example, absence data for Palicourea angustifolia equals those localities with recorded presence of Palicourea guianensis and Warszewiczia coccinea and no presence of *P. angustifolia*. The number of absence records used was fifty-one for P. angustifolia.

To reduce the dimensionality of the model, to minimise parameter redundancy and select the most meaningful variables, we performed bivariate correlation analyses for the species P. angustifolia (Tables 3 and 4) using significance levels of 0.05. For continuous variables (mean, maximum, minimum temperatures, mean precipitation and potential evapotranspiration), the correlations between these variables were analysed at localities with presence of the species. For continuous variables, a test of colinearity between each variable pair was performed. Only those variables which were not significantly collinear were incorporated into the model. If two variables were collinear, the controlling factor that has a more direct control on plant physiology and plant growth was chosen over the other variable, for example, temperature is collinear with elevation since elevation is a control of temperature. Temperature is a control of plant growth (see Table 1). Elevation is only a control on plant growth because of its impact on temperature (and other variables). Thus temperature is preferred to elevation (Velázquez 1994). The same process was undertaken for P. guianensis



Figure 2. An example of the distribution of training and testing points to develop the model

Table 2. Numbers of presence records used for training and testing for each speciesTraining-testing ratio (%)Number of presence records (training-testing)

Training-testing ratio (%)	Number of presence records (training-testing)			
	Palicourea angustifolia	Palicourea guianensis		
80–20%	43-12	48-12		
70–30%	38-17	42-18		
60–40%	33–22	36–24		

		T_mean	P_mean	R_mean	T_min	T_max	EVP
T_mean	Pearson Correlation	1,000	,367**	,157	1,000**	1,000**	,875**
	Sig. (2-tailed)	,	,006	,252	,000	,000	,000
P_mean	Pearson Correlation	,367**	1,000	-,084	,367**	,367**	,343*
	Sig. (2-tailed)	,006	,	,543	,006	,006	,010
R_mean	Pearson Correlation	,157	-,084	1,000	,157	,157	,124
	Sig. (2-tailed)	,252	,543	,	,252	,252	,368
T_min	Pearson Correlation	1,000**	,367**	,157	1,000	1,000	,875**
	Sig. (2-tailed)	,000,	,006	,252	,	,000	,000
T_max	Pearson Correlation	1,000**	,367**	,157	1,000**	1,000**	,875**
	Sig. (2-tailed)	,000	,006	,252	,000	,	,000
EVP	Pearson Correlation	,875**	,343*	,124	,875**	,875**	1,000
	Sig. (2-tailed)	,000	,010	,368	,000	,000	,

Table 3. Results of bivariate correlations between continuous variables at 55 localities with presence of species *Palicourea angustifolia*.

** Correlation is significant at the 0.01 level (2-tailed); * Correlation is significant at the 0.05 level (2-tailed).

Table 4. Results of bivariate correlations between discrete variables and localities with presence and absence of species *Palicourea angustiolia*.

		Presence	Soil_class	Slope gradient_class	Geo_Class	Slope aspect_class
Presence	Pearson Correlation	1,000	,510**	,437**	-,282**	,071
	Sig. (2-tailed)	,	,000	,000	,002	,446
Soil_class	Pearson Correlation	,510**	1,000	,555**	-,593**	,116
	Sig. (2-tailed)	,000	,	,000	,000	,210
Slope gradient_class	Pearson Correlation	,437**	,555**	1,000	-,306**	,198**
	Sig. (2-tailed)	,000	,000	,	,001	,031
Geo_class	Pearson Correlation	-,282**	-,593**	-,306**	1,000	,109
	Sig. (2-tailed)	,002	,000	,001	,	,242
Slope aspect_class	Pearson Correlation	,071	,116	,198**	,109	1,000
	Sig. (2-tailed)	,446	,210	,031	,242	,

** Correlation is significant at the 0.01 level (2-tailed);* Correlation is significant at the 0.05 level (2-tailed).

Initially, preliminary testing was undertaken by producing predicted maps based on the Mahalanobis distance for *P. angustifolia*. We used ten different combinations of environmental parameters to identify the best fitted model for the species. The Mahalanobis distances were computed from the thirty different training datasets prepared earlier (3 parameterisation to validation ratios x 10 repetitions of randomly selected presence records). These resulted in a total of 300 predicted maps that represented a large dataset for further analysis. For predictive distribution models, accuracy assessment is usually carried out through the construction of an error matrix (a cross tabulation of the number of correctly and incorrectly classified observations) from which several measures of model performance are derived (Stockwell & Noble, 1992; Fielding & Bell, 1997; Stockwell & Peterson, 2002b; Anderson *et al.* 2002a, 2003; Farber & Kadmon, 2003). Each one of the 300 predictive maps was independently validated with the testing datasets, and the results were summarised in an error matrix

containing four measures of accuracy used commonly in this type of research: sensitivity, specificity, overall accuracy, and the Kappa statistic (Fielding & Bell, 1997; Farber & Kadmon, 2003).

Sensitivity is defined as the probability of correctly predicting a presence and specificity is of correctly predicting an absence. As aforementioned, we used records of the two other species for this study (*P. guianensis* and *Warszewiczia coccinea*) as absence sites to be included in the validation dataset. For the purpose of this study and for practical reasons we assumed that where there have been collection missions (focused on the same family) but no reports of the *P. angustifolia*, this species can be considered as absent from those localities.

We also undertook a preliminary survey of the Mahalanobis distance to be used as a threshold (d) beyond which a site is not considered as potentially suitable for the species. This threshold is used to determine the accuracy of the model. However it has to be taken into account that as the value of d increases, so does the the probability of including not only suitable sites but also potentially nonsuitable sites. We used the 90th percentile threshold after preliminary analyses (Armenteras, 2003). Table 6 summarises the results obtained for each of the environmental parameter combinations. The combination of variables that provided higher predictive success was selected for further analysis.

RESULTS

From the results in Table 3 and 4, it can be observed that evapotranspiration and minimum and maximum temperature are highly correlated to mean temperature, and thus mean temperature was selected for further use in the distribution models and the other three variables were discarded. Although evapotranspiration was also a strong physiological control, the variable was not considered because it was a secondary data derived from the temperature dataset. For precipitation, although the results indicate a significant correlation of precipitation with mean temperature, the variable is sufficiently different from temperature in its physiological impact to make it worthy of inclusion. Regarding categorical variables, slope aspect does not seem to be an important variable for the species (i.e., no correlation at all with presence of the species was found), hence it was not used further. Slope aspect is usually only important for driving solar radiation loads at sites away from the equator where N-S radiation differences become very large. Slope aspect (like slope gradient) is also notoriously difficult to quantify from coarse resolution topographic data; hence it was removed from consideration.

Accuracy measures were obtained for all the models and all model runs (Table 5). A threshold of the 90th percentile to the mean Mahalanobis distances of the training dataset was used for validation purposes, that is, areas within the 90th percentile to the mean mahalanobis distance were considered as suitable sites for the species. Table 5 summarises the results obtained for each one of the combinations of environmental parameters. Model 5 which uses: mean temperature, solar radiation, soil types, and slope gradient shows the highest predictive success for both species. Table 6 presents the corresponding accuracy assessments for the two species.

Predictive distribution models

After demonstrating that the preliminary model validated well with an accuracy of over 0.8 for both species, we modelled the species' potential geographic distribution using the whole available dataset of presence records. The resulting map can be seen in Figs. 3 & 4.

Model	Sensitivity	Specificity	Overall Accuracy	Kappa	Ν	
Madal 1	0,7149	0,6756	0,6856	0,2512	30	
Wodel 1	(0.1000)	(0,0878)	(0,0546)	(0,0787)		
M- J-10***	0,7281	0,6837	0,6961	0,2974	20	
Model 2	(0,1074)	(0.0973)	(0.0637)	(0,1029)	30	
Madal 2	0,6605	0,6945	0,6902	0,2532	20	
Widdel 3	(0,1007)	(0,1038)	(0,0726)	(0,1188)	30	
Madal 4**	0,7239	0,7145	0,7171	0,3136	20	
Widdel 4	(0,1035)	(0,0800)	(0,0546)	(0,0988)	30	
Model 5*	0,7700	0,7082	0,7263	0,3406	20	
Widdel 5	(0,0903)	(0,0951)	(0,0594)	(0,0944)	30	
Madal 6	0,6017	0,6548	0,6400	0,1644	20	
Widdel o	(0,1180)	(0,1141)	(0,0621)	(0,0685)	30	
Madal 7	0,7009	0,6767	0,6802	0,2721	20	
Widdel /	(0,1306)	(0,0985)	(0,0452)	(0,0765)	30	
Madalo	0,4921	0,6746	0,6249	0,1078	20	
Widdel 9	(0,1383)	(0,1163)	(0,0582)	(0,0677)	30	
Madal 10	0,6854	0,5714	0,5808	0,1791	20	
Model 10	(0,1161)	(0,2523)	(0,1760)	(0,1207)	30	

Table 5. Summary of accuracy measures of ten distribution models for *Palicourea angustifolia*.

 The standard deviation values are in parenthesis.

* best overall model performance, **second, *** third

 Table 6. Summary of accuracy measurements of the predicted distribution models for two

 species of Rubiaceae

	Species				
Accuracy	Palicourea angustifolia		Palicourea guianensis		
measures	Mean	Std. Deviation	Mean	Std. Deviation	
Sensitivity	0,8732	0,1017	0,8562	0,0986	
Specificity	0,6616	0,1142	0,9968	0,0097	
Overall Accuracy	0,7256	0,0883	0,9330	0,0483	
Карра	0,4429	0,1353	0,7875	0,1314	
N	30		30		

P. angustifolia and *P. guianensis* show largely complementary potential ranges (Figs. 3 & 4). *P. angustifolia* shows a clear Andean distribution with presence in lower and upper mountain areas but neither in the highlands nor in the inter-Andean valleys. The model also predicts the potential distribution of the species in both the upper mountain areas of Sierra Nevada de Santa Marta and the Serrania de La Macarena. A total of 308,768 km² are predicted as potentially suitable area for *P. angustifolia*. On the other hand, *P. guianensis* was predicted throughout most of the lowland areas of Colombia including

lowland Amazonian forests, and most of the tropical savannas of Orinoquia. Predicted as unsuitable for the species are the few highland areas in the Amazon such as around the Araracuara formation and the hill complex of Mitu. In general terms, the species was not predicted in the wetter lowland areas of the Pacific region or in the most arid enclaves of la Guajira, although some lowland areas of the Sierra Nevada de Santa Marta are predicted as potentially suitable for the species. A large area of 1,004,777 km² is predicted as potentially suitable for *P. guianensis*.



Figure 3. Model of predicted potential distribution for Palicourea angustifolia in Colombia

However, when analyzing the Mahalanobis distances observed from the 55 records used to construct the model for *P. angustifolia*, 5 of them (Table 7) have a Mahalanobis distance much higher than the 90% percentile used for model validation purposes. This means that they fall precisely in the predicted absence pixels. However, if we look in detail at each of

these records, all of them are within 1–2 pixels (km) of larger areas predicted as presence areas (Fig. 5). A similar situation occurred with 5 out of 60 records of *P. guianensis* (Table 7, also occurring within 2 km) pixels predicted by the model as sites of species presence for its model.



Figure 4. Model of predicted potential distribution for Palicourea guianensis in Colombia.

 Table 7. Presence records predicted as absence by their respective model and its identification attributes.

Species					
Palicourea	Palicourea angustifolia		a guianensis		
Specimen number	Origin Database*	Specimen number	Origin Database*		
2445	HAFP	115216	NYBG		
1129933	MO	4568895	MO		
1197094	MO	2716982	MO		
1275705	МО	3592219	МО		
520924	MO	999623	MO		

*HAFP, Alvaro Fernandez Perez herbarium, NYBG, New York Botanical Garden, MO, Missouri Botanical Garden

Modelling the Potential Distribution of trees



Figure 5. Location and specimen number of five presence records of *P. angustifolia* (a,b,c from Missouri Botanical Garden, d from HAFP database) predicted as absence. Pixel size is 1 km².

Table 8. Environmental characteristics at overlap areas predicted as potentially suitable for both *Palicourea angustifolia* and *Palicourea guianensis*.

Variable	Mean (stand. deviation)	Class type	Area (km ²)
Mean annual temperature (C°)	23.8 (1,41)	-	93,983
Solar Radiation (Wm- ² day)	624.58 (9,12)	-	93,983
Mean monthly precipitation (mm)	232.18 (95.26)	-	93,983
Slope gradient (%)	5.3997 (4.4)	-	93,983
Soil types	-	Cordillera Soils Alluvial Plains Soils	80,598 13,385
Elevation (m)	734.60 (282)	200–500m 500–750m 750–1000m 100–1250m <200m or > 1250m	16,808 30,555 26,886 15,860 3,874

We undertook a final analysis of these two species, looking for areas in which the predicted distribution of the two species overlaps. Figure 6 illustrates the geographic extent (93.983 km²) of areas predicted suitable for species co-occurrence. This area of potential overlap between the two species represents 30.4% of the potential distribution of *P. angustifolia* and 9% of *P. guianensis* and the environmental characteristics of this are indicate a mean annual temperature around 23.8 degrees Celsius, 624.5Wm⁻²day of solar radiation and around 232 mm of mean monthly precipitation (see more details in Table 8).



Figure 6. Overlap areas of potential distribution of both *Palicourea angustifolia* and *Palicourea guianensis*.

DISCUSSION

This study focused on developing and testing an alternative methodology that may help optimising the use of the existing species' presence records and environmental data within the framework of a a niche-based model of species distribution to predict the range of tree species occurrence in a relatively simple and efficient manner in tropical countries

Species data for distribution modelling

A limited number of records were available for building the predictive distribution models. Out of the 3000 records collected, only 3 species of Rubiaceae had over 50 records available for modelling, and even these 3 species had to go through a database purge of their localities, having specimens repeated, localities incompletely, inaccurately reported or poorly georeferenced, and typing errors. Also, errors in the accuracy of the geographic coordinates of the species data were impossible to determine. Many samples were georeferenced from museum label descriptions, and these were often rather generally located, specially the older records, not to mention the known bias of collection sites, the lack of a sampling design, and the different origins of the data.

Another important source of error, particularly for those working in the tropics is the determination of the species. This was minimised by choosing the genera Palicourea, on which there is extensive systematic recent work (Taylor, 1996, 1997a, 1997b, 1999, & 2000).

Despite the deficiencies inherent in the use of primary inventory data, the model developed provides very useful information on the species distribution in relation to environmental controls. The technique developed here for mapping potential species distribution offers a number of advantages over other classical modelling techniques (Stockwell & Peters, 1999; Anderson et al. 2003). One of the most important is undoubtedly the ability to cope with presence-only data, thus not making any a priori assumption about the distribution of the species, and also avoiding the use of potential false negatives (Dunn & Duncann, 2000). However, we did use surrogate absence data in this case for validation purposes, but validation can be undertaken by other means (i.e., field inventories). The approach applied here allows the use of environmental variables from multiple sources and in continuous, categorical, or Boolean form (Bar-Hen & Daudin, 1995). Further, different measurement scales of input variables are not problematic since the Mahalanobis statistic is dimensionless, being a function of standardised variables (Clark et al. 1993; Knick & Rotenberry, 1998). Finally, the technique does not assume a normal distribution of the data, which, for most species, is not satisfied (Austin & Smith, 1989).

The model developed here is based on niche theory (Hutchinson, 1959; MacArthur, 1968; Whitaker, 1975), which has a strong background in ecological theory. However, it is important to clearly differentiate the fundamental versus the realised niche of species (Hutchinson, 1959) and to understand further that the predictions developed here represent neither of these, but rather a subset of the fundamental niche which is limited to the distribution of the species within the environments present (and studied) in Colombia. The approach is also limited due to the fact that only a few environmental variables are considered and others may be just as important but without readily available data such as for example historical

or paleoclimatic data. No vegetation data, potential or current, has been incorporated in the model and neither has the current state of the ecosystems been considered, including deforestation, or other threats. Also no subgrid scale variability is taken into account which, at a spatial resolution of 1 km over heterogeneous mountain terrain means that the environmental properties distributed here and those experienced by individual trees on the ground may be quite different.

When many variables are involved, the Mahalanobis approach requires some kind of a priori manual data reduction to identify the most important input parameters for the model specially where there is significant correlation between the variables (Knick & Rotenberry, 1997; De Maesschalck *et al.* 2000; Wilds *et al.* 2000)

Data reduction

The most parsimonious model at a given level of prediction accuracy is always the best model (Mulligan & Wainwright, 2003). The data reduction results (Tables 3 and 4) lead to a considerable reduction of possible variables to be used in the model. Temperature variables were clearly collinear, since they are all modelled from linear regressions between station meteorological data and elevation. Similarly, potential evapotranspiration was derived from temperature using the Thornthwaite methodology (Section 3.3) in which temperature is a key variable. It turns out that no extra important information was provided through modelling these secondary variables since mean temperature remained as the best predictor. Temperature and precipitation were highly correlated at presence sites of P. angustifolia (probably because both are functions of elevation. though temperature is a nonlinear function). Due to the importance of precipitation in the physiology and distribution of species (Begon et al. 1990; Richerson & Lum, 1980; Brown & Gibson, 1983; Turnerl *et al.* 1988; Wright *et al.* 1993; Gaston, 2000), we did not rule out the incorporation of this data, alongside temperature, in the preliminary tests of the algorithm performance.

The predictive accuracy of the models in which we incorporated the precipitation data was substantially lower than more limited combinations of variables (Tables 3 & 4) such as mean temperature, solar radiation, soil type, and slope gradient. The Slope aspect was not incorporated into the modelling approach due to its tested irrelevance to the distribution of *P. angustifolia*. This is likely due to the fact that representation of the slope aspect experienced by trees in the field is rather difficult at a 1 km grain, and the same probably holds true for slope gradient.

Harrel *et al.* (1996) suggest that the number of final predictors in modelling should be m/10, where m is the total number of observations. In this analysis, and considering that the number of presence records is 55 for *P. angustifolia* and 60 for *P. guianensis*, 5 variables would be suggested, and 4 to 6 were tested with the best model resulting from 4 variables (Table 5).

Errors and accuracy

Several questions arise when looking at the issue of accuracy assessment. The first is that although the importance of understanding error in models is clear (Rykiel, 1996; Boone & Krohn, 2002; Elith et al. 2002; Guisan & Zimmermann 2000; Guisan et al. 2002), there is still some extent of subjectivity in the interpretation of model accuracy, specially for species' distribution models (Guisan & Zimmermann, 2000). Different measures of model performance have been proposed (Rykiel, 1996; Fielding & Bell, 1997; Guisan & Zimmermann, 2000; Anderson et al. 2003). For any given threshold, there are locations with values below it where the species is present (true positives) and absent (false positives). Similarly, there are sites that the model predicts as unsuitable (above the threshold) that are occupied (false negatives) and where the species is absent (true negatives). We chose to use error matrices and four measures of accuracy that required absence data (not required for the prediction, but useful in validation).

This leads to the question of how accurate it was to use other species' localities records as absence sites for the species that were modelled. In herbarium and collection datasets, "real" absence data does not exist, and this was partly the justification for undertaking a modelling approach which can use only presence data. However, wherever clearly related species are collected during the same collection missions by the same collectors, sites where P. angustifolia had not been collected but where P. guianensis had been, could be considered absence sites for *P.angustifolia*. Some 11 sites had collection records of both species at the same time suggesting that the species do overlap in distribution (7 out of 9 are located in overlapping distribution areas). This reaffirms the fact that the definition of absence sites for validation purposes was appropriate. One of the specimens collected for P. angustifolia (NO. 1275705, MO) was not predicted by the model to be present in the locality collected (Table 7). This might suggest either the lack of inclusion of an important variable in the modelling exercise or some kind of interpolation error in the GIS databases, significant unmeasured subgrid variability in the environmental variables, or georeferencing error in the records. This record, which is less than 2 pixels away (2 km) from areas that were modelled as overlapping distribution areas for the species, seems to suggest the latter as a possibility. The other specimen of P. angustifolia (NO. 2469, HAFP) has a distance of over 15 km to the overlapping area. Both the localities which were incorrectly predicted in the model for P. angustifolia, were correctly predicted in the

distribution model for *P. guianensis*. However, the localities where the *P. angustifolia* HAFP specimen is recorded has an elevation of 160 m, which is outside the natural range of the species. Arguably this might be probably a collection/measurement error, a typing error, or a species determination error. In general, observation or measurement errors lead to reduced predictability of models (Boone and Krohn, 2002)

Geographic distribution

Despite the propagation of measurement and systematic errors, effective prediction of test localities for both species could be achieved in all 3 significant models. Judgement by experts also gave a positive assessment of the resulting distribution patterns corresponding fairly well to the knowledge of the species and recorded records (C.M.Taylor, E. Calderon, pers. comm; Jimenez 2002, Rangel 1995, 2000). P. angustifolia shows a clear Andean distribution with presence in lower and upper montane areas but neither in the highlands nor in the inter-Andean valleys. The best fitted model also predicts the potential distribution of the species in both the upper mountain areas of Sierra Nevada de Santa Marta and the Serrania de La Macarena. Taylor (1997a, b) states that this species belongs to the subgenus Montanae, a notion that is in agreement with the modelling results obtained for this species.

On the other hand, *P. guianensis* was predicted throughout most lowland areas of Colombia including the lowland Amazon forests and most of the tropical savannas of Orinoquia. The few highland areas in the Amazon such as around the Araracuara formation and the hill complex of Mitu were unsuitable for the species. This species is a widespread lowland species (Taylor, 1997a,b). Taylor (1997a, b) classifies this species to the subgenus *Palicourea* and describes it as generally found at lower elevations, 0–1,200 (1,500) m, throughout the range of the genus. Again, this is consistent with the prediction of the obtained in this modelling effort.

CONCLUSIONS

Modelling of species' responses to static or changing environmental conditions has become an increasingly important part of modern ecology and biogeography. This kind of modelling can save time and money in the formulation and execution of biological inventories, a task which Colombia, along with other countries, is carrying out in fulfilment of its obligations to the Convention on Biological Diversity. Particularly in the tropics, modelling can provide a quicker and potentially more reliable approximation for identifying areas with high biological diversity when lack of resources or time constraints are in place, and complement small-area field inventory that might take longer to achieve. By limiting and approximate habitat niche of a species (with limitation since not all ecological or phylogenetic aspects are included), it is possible to predict its distribution-at least for environmentally determined, structural organisms like trees. However, the originality of the present approach lies in the fact that not only it is based on the concept of ecological niche, but in contrast to many statistical techniques, it needs only presence data sets. This property is very important because most currently available data for the tropical taxa are still of this kind. The focus on presence data is partly due to the fact that until recently the emphasis was to obtain site inventories instead of regional statistical analysis, so data were collected in a nonstratified or without concerns to sampling desing, in terms of spatial coverage.

The Mahanalobis technique provides key information about the niche of the species being modelled and allows comparisons on species distributions. Further, the methodology is well-suited for application in conservation biology i.e. the use of this kinf od models may have many applications such as the quick prediction of invasive species potential distribution or finding the best locations to reintroduce individuals of endangered species, the prioritisation of direct inventory efforts toward areas with high presence probability of a species, prediction of species' redistribution due to climate change. Further along the trophic chain, these models can help predict the distribution of animals that use these trees as a source of food, bearing in mind that are not indicative of healthy or viable populations at all, or perhaps most importantly in terms of Colombia's commitments to the CBD, to identify gaps for conservation priorities.

The approach adopted here, however, is rather simple. A more comprehensive model of the potential distribution of species involve considering competitive would interactions between species and the effects of disturbance or population dynamics. Also, the present approach assumes that the species have a unimodal response to environmental conditions. Further, this modelling approach relies on the assumption that the general form of species' response to environmental gradients is an optimum where the species is most likely to occur; the likelihood of occurrence decreases with distance from that optimum. However, also it has to be taken into account the factg taht this approach does not take into account interaction or changes in the interlinkages amongst factors, that is, parameter interaction would need to be incorporated in the future. In addition, the climatic fields used here are representative for canopy-level tree species only, whereas subcanopy species will experience a much altered microclimate. Nevertheless, the current need of tropical countries like Colombia is to have at least a basis from which to optimise available data to facilitate better geographical targeting of inventory and the spatially explicit prioritisation of conservation at the national scale. By building upon the techniques described here, we hope to provide a basis for the rapid identification of species-rich areas and areas in which particular species may be threatened or be best conserved,. This will contribute toward the national biodiversity conservation and management strategy.

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Modelling the Potential Distribution of trees

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Modelling the Potential Distribution of trees

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