

# STRAIGHT-LINE CONVENTIONAL TRANSIENT RATE ANALYSIS FOR LONG HOMOGENEOUS AND HETEROGENEOUS RESERVOIRS

## ANÁLISIS CONVENCIONAL PARA TRANSIENTES DE CAUDAL EN YACIMIENTOS HOMOGENEOS Y HETEROGENEOS ALARGADOS

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**ABSTRACT:** A linear flow regime is a very important flow regime presented in fractured wells, horizontal wells and long reservoirs. Either pressure-transient analysis or rate-transient analysis may be affected by a linear flow regime. In the case the case of production rate most of the analysis is conducted by decline-curve fitting and little attention has been given to rate-transient analysis. This paper presents the governing equations used for rate-transient analysis in elongated systems and provides examples using the conventional analysis. The methodology allows for the estimation of reservoir permeability, reservoir width and geometrical skin factors. If the test is long enough, reservoir drainage area and well position inside the reservoir can also be determined. The methodology was successfully verified by its application to synthetic cases.

**KEY WORDS:** Linear flow, parabolic flow, reservoir width, well-flowing pressure

**RESUMEN:** El flujo lineal es un régimen de flujo muy importante que se presenta en pozos fracturados, horizontales y yacimientos alargados. Tanto el análisis de pruebas de presión como de transitorio de caudal podrán verse afectados por la presencia del flujo lineal. Para el caso de producción a caudal variable, la mayor parte del análisis se realiza mediante ajuste de curvas de declinación y poca atención ha recibido el análisis transitorio de caudal. Este artículo presenta las ecuaciones gobernantes usadas para análisis transitorio de caudal en sistemas alargados y proporciona ejemplos mediante el método convencional. La metodología permite la estimación de la permeabilidad, el ancho del yacimiento y los factores de daño geométricos. Si la prueba es lo suficientemente larga se puede estimar el área de drenaje del yacimiento y la posición del pozo dentro del mismo. La metodología se verificó satisfactoriamente mediante su aplicación a pruebas sintéticas.

**PALABRAS CLAVE:** Flujo lineal, flujo parabólico, ancho del yacimiento, presión de fondo fluyente

### 1. INTRODUCTION

Formation linear flow in vertical wells can be due to geological events (meandering), faulting or sand lens. Recently, [4] introduced the application of the TDS technique for characterization of long and homogeneous reservoirs, presenting new equations for the estimation of reservoir area, reservoir width and geometrical skin factors. They classified the linear flow regime into two categories: (a) dual-linear, when the flow takes along both sides of the well throughout the elongated reservoir part, and (b) single-linear, when the flow comes from one side of the reservoir. [2] introduced a new flow regime exhibiting a negative half slope on the pressure derivative curve once

dual-linear flow has ended. [3] studied the impact of the geometric skin factors on elongated systems. Characterization of pressure tests in elongated systems using the conventional method was also presented by [4]. [5] presented a summary of the advances in characterization of long and homogenous reservoirs using transient pressure analysis. [6] were the first in applying rate-transient analysis to elongated systems. However, pressure and pressure derivative cases of naturally-fractured reservoir were later analyzed by [7].

### 2. MATHEMATICAL DEVELOPMENT

Define the following dimensionless quantities:

$$t_D = \frac{0.0002637kt}{\phi\mu c_i r_w^2} \quad (1)$$

$$t_{DA} = \frac{0.0002637kt}{\phi\mu c_i A} \quad (2)$$

$$\frac{1}{q_D} = \frac{kh\Delta P}{141.2\mu B} \frac{1}{q} \quad (3)$$

$$t_D = \frac{t_D}{W_D^2} \quad (4)$$

$$W_D = \frac{Y_E}{r_w} \quad (5)$$

$$X_D = \frac{2b_x}{X_E} \quad (6)$$

$$Y_D = \frac{2b_y}{Y_E} \quad (7)$$

Different simulation runs were generated using the superposition principle for elongated systems with the lateral boundaries open or closed to flow. Regression analysis was applied to the reciprocal derivative curve to develop the governing equations, and then the governing reciprocal rate equation was obtained by the integration of the derivative.

**2.1. Linear flow regime, homogeneous reservoirs**

Linear flow is observed when the lateral boundaries of the reservoir are closed to flow and the well is off-centered inside the reservoir. The governing equation for this behavior is

$$\frac{1}{q_D} = \frac{4\pi\sqrt{t_D}}{W_D} + s_L \quad (8)$$

where  $s_L$  is the geometrical skin factor due to the convergence from dual-linear to linear flow. Then, by replacing the dimensionless quantities in Eq. 8, it becomes

$$\frac{1}{q} = \frac{28.8137B}{h\Delta P} \sqrt{\frac{\mu t}{\phi k c_i Y_E^2}} + \frac{141.2\mu B}{kh\Delta P} s_L \quad (9)$$

which implies that a Cartesian plot of  $1/q$  vs.  $t^{0.5}$  will produce a straight line which slope  $m_{LF}$  and intercept  $b_{LF}$  allow to obtain

$$Y_E = \frac{28.8137B}{h\Delta P m_{LF}} \sqrt{\frac{\mu}{\phi k c_i}} \quad (10)$$

$$s_L = \frac{kh\Delta P b_{LF}}{141.2\mu B} \quad (11)$$

**2.2. Dual-linear flow regime, homogeneous reservoir**

Once the radial flow regime vanishes, two linear flows occur simultaneously opposite to each other inside the reservoir. The governing equation for this case is

$$\frac{1}{q_D} = \frac{5\sqrt{\pi t_D}}{2W_D} + s_{DL} \quad (12)$$

The dimensional form of Eq. 12 is

$$\frac{1}{q} = \frac{10.1602B}{h\Delta P} \sqrt{\frac{\mu t}{\phi k c_i Y_E^2}} + \frac{141.2\mu B}{kh\Delta P} s_{DL} \quad (13)$$

which also indicates that a Cartesian plot of  $1/q$  vs.  $t^{0.5}$  will produce a straight line which slope  $m_{DLF}$  and intercept  $b_{DLF}$  allow to obtain

$$Y_E = \frac{10.1602B}{h\Delta P m_{DLF}} \sqrt{\frac{\mu}{\phi k c_i}} \quad (14)$$

$$s_{DL} = \frac{kh\Delta P b_{DLF}}{141.2\mu B} \quad (15)$$

**2.3. Parabolic flow regime, homogeneous reservoirs**

This flow is the result of the simultaneous action of a near open boundary and a flow along the reservoir in the opposite direction. For further explanation the reader is referred to [2]. The dimensionless reciprocal rate governing the equation is given by

$$\frac{1}{q_D} = -\frac{W_D X_D^2}{4} \left(\frac{X_E}{Y_E}\right)^2 \sqrt{\frac{\pi}{t_D}} + s_{PB} \quad (16)$$

After plugging in the dimensionless equations, it will yield

$$\frac{1}{q} = -\frac{15411.843Bb_x^2}{h\Delta P} \sqrt{\frac{\phi\mu^3 c_i}{k^3 Y_E^2} t^{-0.5}} + \frac{141.2\mu B}{kh\Delta P} s_{PB} \quad (17)$$

Therefore, a Cartesian plot of  $1/q$  vs.  $1/t^{0.5}$  will yield a straight line which slope  $m_{PBF}$  and intercept  $b_{PBF}$  allow to determine

$$b_x = -\frac{m_{PBF}^2}{124.1444} \sqrt{\frac{h\Delta P}{B}} \frac{k^3 Y_E^2}{\phi \mu^3 c_i} \quad (18)$$

$$s_{PBF} = \frac{kh\Delta P b_{PBF}}{141.2\mu B} \quad (19)$$

#### 2.4. Dual-linear flow regime, heterogeneous reservoirs

For this case the governing dimensionless reciprocal rate and dimensional reciprocal rate equations are

$$1/q_D = \frac{9}{4} \frac{\sqrt{\pi t_D}}{\sqrt{\omega W_D}} + s_{DL} \quad (20)$$

$$\frac{1}{q} = \frac{9.1442B}{h\Delta P} \sqrt{\frac{\mu t}{\omega k \phi c_i Y_E^2}} + \frac{141.2\mu B}{kh\Delta P} s_{DL} \quad (21)$$

which also indicates that a Cartesian plot of  $1/q$  vs.  $t^{0.5}$  will produce a straight line which slope  $m_{DLF}$  and intercept  $b_{DLF}$  allow to obtain

$$Y_E = \frac{9.1442B}{h\Delta P m_{DLF}} \sqrt{\frac{\mu}{\omega \phi k c_i}} \quad (22)$$

$$s_{DL} = \frac{kh\Delta P b_{DLF}}{141.2\mu B} \quad (23)$$

#### 2.5. Linear flow regime, heterogeneous reservoirs

Two cases are considered. The first one takes into account that the linear flow regime shows up once the transition period of the naturally-fractured reservoir has vanished. Therefore, the governing dimensionless and dimensional equations are

$$\frac{1}{q_D} = \frac{4\pi\sqrt{t_D}}{W_D} + s_L \quad (24)$$

$$\frac{1}{q} = \frac{28.8137B}{h\Delta P} \sqrt{\frac{\mu t}{\phi k c_i Y_E^2}} + \frac{141.2\mu B}{kh\Delta P} s_L \quad (25)$$

As for the former cases, Eq. 24 implies that a Cartesian plot of  $1/q$  vs.  $t^{0.5}$  will yield a straight line which slope  $m_{LF}$  and intercept  $b_{LF}$  allow to obtain

$$Y_E = \frac{28.8137B}{h\Delta P m_{LF}} \sqrt{\frac{\mu}{\phi k c_i}} \quad (26)$$

$$s_L = \frac{kh\Delta P b_{LF}}{141.2\mu B} \quad (27)$$

In the second case, the linear flow regime takes place before the heterogeneous transition is seen. Again, the governing equations are

$$\frac{1}{q_D} = \frac{21}{5} \frac{\sqrt{\pi t_D}}{W_D \sqrt{\omega}} + s_L \quad (28)$$

$$\frac{1}{q} = \frac{17.0692B}{h\Delta P} \sqrt{\frac{\mu t}{\omega k \phi c_i Y_E^2}} + \frac{141.2\mu B}{kh\Delta P} s_L \quad (29)$$

where  $\omega$  is the dimensionless storativity coefficient of a naturally fractured reservoir introduced by [8]. As before, a Cartesian plot of  $1/q$  vs.  $t^{0.5}$  will produce a straight line which slope  $m_{LF}$  and intercept  $b_{LF}$  allow to obtain

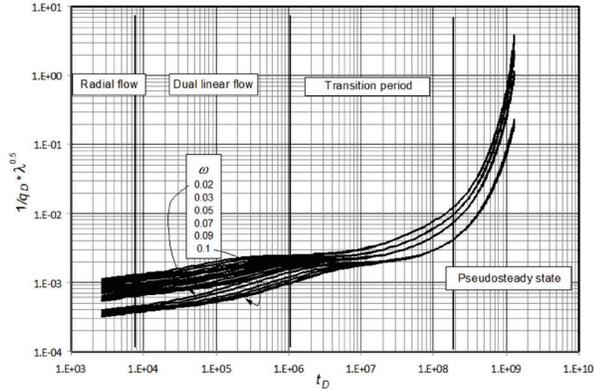
$$Y_E = \frac{17.0692B}{h\Delta P m_{LF}} \sqrt{\frac{\mu}{\omega \phi k c_i}} \quad (30)$$

$$s_L = \frac{kh\Delta P b_{LF}}{141.2\mu B} \quad (31)$$

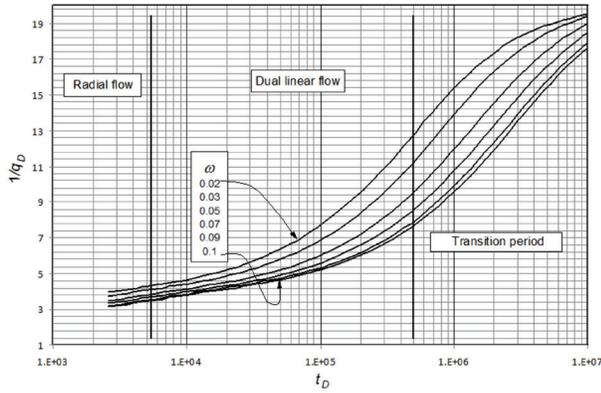
In elongated heterogeneous systems the mass transference between matrix and fractures may take place after the radial flow regime when the interporosity flow parameter  $\lambda$  is normally lower than  $1 \times 10^{-7}$ . Then either the dual-linear or the linear flow regime may be interrupted by the transition period of the naturally-fractured system. However, in any case, dual-linear flow is normally seen after the radial flow regime. Notice that  $\lambda$  was also introduced by [8].

Figure 1 shows a semilog plot of the reciprocal dimensionless rate times the square root of the interporosity flow parameter  $\lambda$  as a function of the dimensionless time for different  $\lambda$  and  $\omega$  values. As expected, a linear trend is observed during the radial flow regime. Then, dual-linear flow appears followed by the late pseudosteady-state period in which all the lines for the same value of  $\lambda$  coincide. Based on that fact, a semilog plot of the reciprocal dimensionless rate vs. dimensionless time (Fig. 2) was built for different values of the dimensionless storativity parameter. From Fig. 2, a correlation between  $\omega$  with the intercept at time of 1 hr is given as

$$\omega = \frac{a + bx + cx^2 + dy}{1 + ex + fy + gy^2 + hy^3} \quad (32)$$



**Figure 1.** Semilog plot of the dimensionless reciprocal rate times the square root of the interporosity flow parameter versus the dimensionless time for different  $\lambda$  and  $\omega$  values



**Figure 2.** Semilog plot of the dimensionless reciprocal rate versus the dimensionless time for different values of  $\omega$  and  $\lambda = 1 \times 10^{-8}$

$$\begin{aligned}
 r^2 &= 0.9999206624489242 \\
 \sigma &= 0.0003518047465261433 \\
 a &= -0.0293872506829593 \\
 b &= 0.01814676521142132 \\
 c &= -0.00294633229989956 \\
 d &= 0.0002169782577669551 \\
 e &= 0.005170615590574063 \\
 f &= -0.9359970165469937 \\
 g &= 0.2912087778421929 \\
 h &= -0.03102476190262259
 \end{aligned}$$

where

$$x = \log \frac{0.0002637k}{\phi \mu c_i r_w^2} \quad (33)$$

for homogeneous reservoirs

$$s_r = 1.1513 \left[ \frac{(1/q)_{1hr}}{m} - \log \left( \frac{k}{\phi \mu c_i r_w^2} \right) + 3.23 \right] \quad (34)$$

for heterogeneous reservoirs

$$s_r = 1.1513 \left[ \frac{(1/q)_{1hr}}{m} - \log \left( \frac{k}{\phi \omega \mu c_i r_w^2} \right) + 3.23 \right] \quad (35)$$

$$y = \frac{kh\Delta P}{141.2\mu B} \left( \frac{1}{q} \right)_{1hr} + 1.0515s_r \quad (36)$$

Eq. 35 is applied to  $-4 \leq s_r \leq 4$  and  $0.01 \leq \omega \leq 0.1$ . Also, for the semilog plot, the permeability is estimated from

$$k = \frac{162.6\mu B}{mh(P_i - P_{wf})} \quad (37)$$

As shown in Fig. 3, the intercept on the semilog plot is a function of the mechanical skin factor  $s_r$  as shown by the excellent correlation provided in Fig. 4.

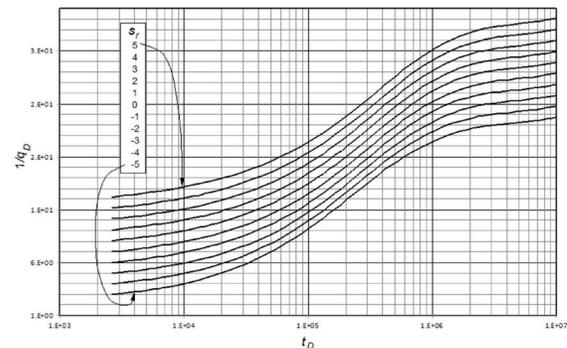
In this study, the equation provided by [9] is used to estimate the interporosity flow parameter

$$\lambda = \frac{3792(\phi c_i)_i \mu r_w^2}{k \Delta t_{inf}} \left[ \omega \ln \left( \frac{1}{\omega} \right) \right] \quad (38)$$

where  $\Delta t_{inf}$  is the inflection point at which the minimum (trough) of the reciprocal rate derivative takes place during the transition period of the heterogeneous system. As a recommendation, the derivative plot should be used for reading that value.

### 3. EXAMPLES

The information data for all the examples is reported in Table 1.



**Figure 3.** Semilog plot of the dimensionless reciprocal rate as a function of the dimensionless for  $\omega = 0.01$ ,  $\lambda = 1 \times 10^{-8}$  and different mechanical skin factors

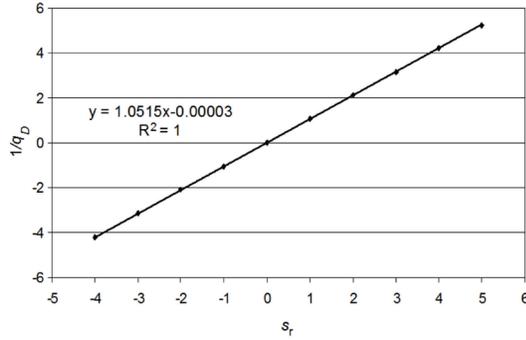


Figure 4. Relationship of the dimensionless reciprocal rate versus the mechanical skin factor for  $\omega = 0.01$  and  $\lambda = 1 \times 10^{-8}$

### 3.1. Synthetic example 1, homogeneous case

A production test for a rectangular-shaped reservoir was simulated with the information provided in Table 1. It is requested to estimate the reservoir width and dual-linear skin factor.

**Solution.** Figure 5 displays a plot of the reciprocal flow rate against time. From this plot, the following information was read:

$$m_{DLF} = 2.01024 \times 10^{-5} \text{ D/STB}$$

$$b_{DLF} = 7.0995 \times 10^{-5} \text{ D/STB/hr}^{0.5}$$

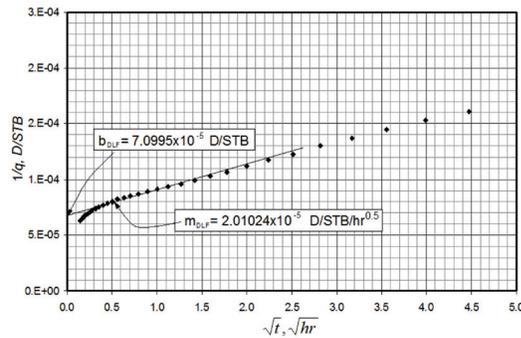


Figure 5. Cartesian plot of the reciprocal rate versus the square root of time for example 1

Table 1. Input data for the examples

Parameter	Synthetic example 1	Synthetic example 2	Field example 1
$\Delta P$ , psi	2500	2500	2800
$\mu$ , cp	2	2	1.52
$\phi$ , %	20	20	13
$B$ , rb/STB	1.2	1.2	1.04
$c_r$ , psi <sup>-1</sup>	$1 \times 10^{-6}$	$1 \times 10^{-6}$	$4.34 \times 10^{-5}$
$r_w$ , ft	0.5	0.5	0.3

Parameter	Synthetic example 1	Synthetic example 2	Field example 1
$h$ , ft	100	100	100
$X_E$ , ft	4000	20000	
$Y_E$ , ft	500	1000	
$k$ , md	50	50	65
$\lambda$		$5 \times 10^{-8}$	$4 \times 10^{-8}$
$\omega$		0.02	0.21
$s_p$		0.02	-2.3

The reservoir width is found by means of Eq. 14 using the slope of the dual-linear flow regime

$$Y_E = \frac{10.1602B}{h\Delta P m_{DLF}} \sqrt{\frac{\mu}{\phi k c_i}}$$

$$Y_E = \frac{10.1602(1.2)}{(100)(2500)(2.01024 \times 10^{-5})}$$

$$\sqrt{\frac{2}{(0.2)(50)(1 \times 10^{-6})}} = 1083.8 \text{ ft}$$

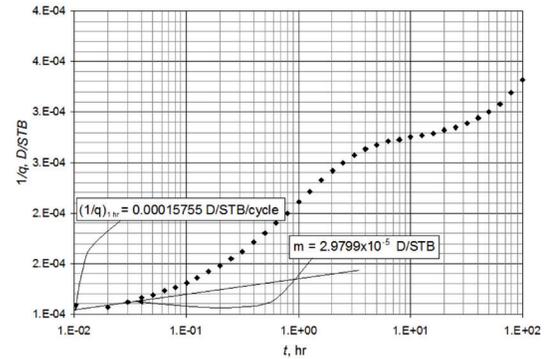


Figure 6. Semilog plot of reciprocal rate versus time for example 2

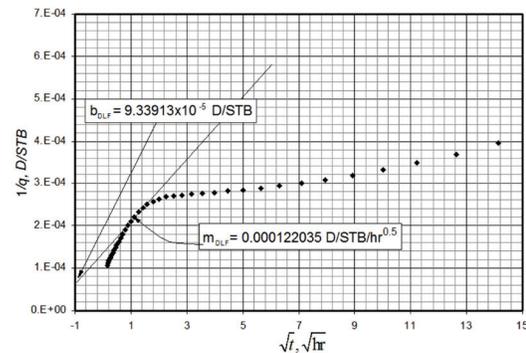


Figure 7. Cartesian plot of the reciprocal rate versus the square root of time for example 2

The geometrical skin factor was calculated with Eq. 15,

$$s_{DL} = \frac{kh\Delta P b_{DLF}}{141.2\mu B}$$

$$s_{DL} = \frac{(50)(100)(2500)(7.0995 \times 10^{-5})}{141.2(2)(1.2)} = 2.62$$

### 3.2. Synthetic example 2, heterogeneous reservoir

A simulated test was run with information given in Table 1. From the semilog plot, Fig. 6, a value of the slope and intercept of  $3.1 \times 10^{-5}$  D/STB/cycle and 0.0002 D/STB, respectively, were read and the mechanical skin factor was estimated from Eq. 34

$$s_r = 1.1513 \left[ \frac{(1/q)_{hr}}{m} - \log \left( \frac{k}{\phi\omega\mu c_t r_w^2} \right) + 3.23 \right]$$

$$s_r = 1.1513 \left[ \frac{0.0002}{3.1 \times 10^{-5}} - \right.$$

$$\left. \log \left( \frac{50}{(0.2)(0.02)(2)(1 \times 10^{-6})(0.5^2)} \right) + 3.23 \right]$$

$$s_r = -0.825$$

Parameters  $x$  and  $y$  from Eqs. 32 and 35 are, respectively,

$$x = \log \frac{0.0002637k}{\phi\mu c_t r_w^2}$$

$$x = \log \frac{0.0002637(50)}{(0.2)(2)(1 \times 10^{-6})(0.5^2)} = 5.120045$$

$$y = \frac{kh\Delta P}{141.2\mu B} \left( \frac{1}{q} \right)_{1hr} + 1.0515s_r$$

$$y = \frac{(50)(100)(2500)}{141.2(2)(1.2)} (0.00015755) +$$

$$1.0515(-0.825) = 6.5097$$

Application of Eq. 31 leads one to find

$$\omega = \frac{a + bx + cx^2 + dy}{1 + ex + fy + gy^2 + hy^3} = 0.01$$

A Cartesian plot of the reciprocal rate versus the square root of time is given in Fig. 7. From this plot a slope of  $m_{DLF} = 0.000128792$  D/STB/hr<sup>0.5</sup> and an intercept of  $b_{DLF} = 9.03618 \times 10^{-5}$  D/STB were read, which are then used to estimate reservoir width and the dual-linear skin factor with Eqs. 21 and 22, respectively.

$$Y_E = \frac{9.1442B}{h\Delta P m_{DLF}} \sqrt{\frac{\mu}{\omega\phi k c_t}}$$

$$Y_E = \frac{9.1442(1.2)}{(100)(2500)(0.000128792)}$$

$$\sqrt{\frac{2}{(0.02)(0.2)(50)(1 \times 10^{-6})}} = 1077.70 \text{ ft}$$

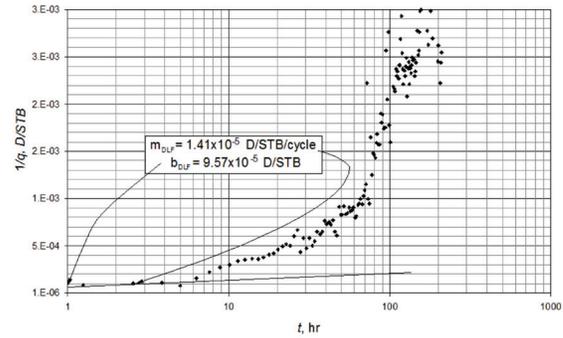


Figure 8. Semilog plot of reciprocal rate versus time for the field example

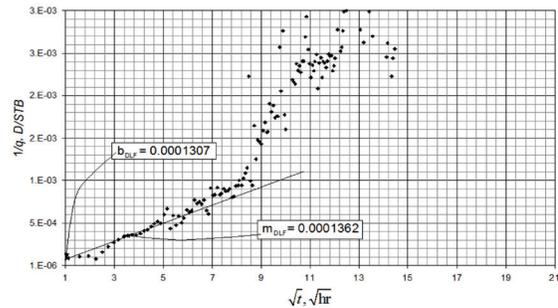


Figure 9. Cartesian plot of the reciprocal rate versus the square root of time for field example

$$s_{DL} = \frac{kh\Delta P b_{DLF}}{141.2\mu B}$$

$$s_{DL} = \frac{(50)(100)(2500)(9.03618 \times 10^{-5})}{141.2(2)(1.2)} = 3.33$$

Finally, the interporosity flow parameter is estimated with Eq. 37 using a value of  $\Delta t_{inf} = 10.047$  hr, obtained from the reciprocal derivative plot, not shown here.

$$\lambda = \frac{3792(\phi c_t)_i \mu r_w^2}{k \Delta t_{inf}} \left[ \omega \ln \left( \frac{1}{\omega} \right) \right]$$

$$\lambda = \frac{3792(0.2)(1 \times 10^{-6})(2)(0.5^2)}{(50)(10.047546)} \left[ 0.02 \ln \left( \frac{1}{0.02} \right) \right]$$

$$\lambda = 5.906 \times 10^{-8}$$

### 3.3. Field example, homogeneous reservoir

[10] provided a field case which input information is given in Table 1 and production vs. time is given in the semilog plot of Fig. 8. Using the permeability, given in Table 1, the slope was estimated from Eq. 36 to be  $1.42 \times 10^{-5}$  D/STB/cycle. With the first point in Fig. 8 and the intercept  $(1/q)_{1hr}$  of  $9.57 \times 10^{-5}$  D/STB, the parameters  $x$  and  $y$  are estimated using Eqs. 32 and 36, respectively, such as

$$x = \log \frac{0.0002637k}{\phi \mu c_t r_w^2}$$

$$x = \log \frac{0.0002637(65)}{(0.13)(1.52)(4.34 \times 10^{-5})(0.3^2)} = 4.698$$

$$y = \frac{kh\Delta P}{141.2\mu B} \left( \frac{1}{q} \right)_{1hr} + 1.051s_r$$

$$y = \frac{(65)(100)(2800)}{141.2(1.52)(1.04)} 9.75 \times 10^{-5} + 1.051(-2.3) = 3.49$$

Then, Eq. 31 allows for one to obtain a value of the dimensionless storativity coefficient  $\omega$  of 0.06. From Fig. 9, the slope  $m_{DLF} = 1.362 \times 10^{-4}$  D/STB/hr<sup>0.5</sup> and intercept  $b_{DLF} = 1.307 \times 10^{-4}$  D/STB allow for one to determine reservoir width and geometrical skin factor, respectively, from Eqs. 21 and 22

$$Y_E = \frac{9.1442B}{h\Delta P m_{DLF}} \sqrt{\frac{\mu}{\omega \phi k c_t}}$$

$$Y_E = \frac{9.1442(1.04)}{(100)(2800)(1.363 \times 10^{-4})}$$

$$\sqrt{\frac{1.52}{(0.06)(0.13)(65)(4.34 \times 10^{-5})}} = 122.7 \text{ ft}$$

$$s_{DL} = \frac{kh\Delta P b_{DLF}}{141.2\mu B}$$

$$s_{DL} = \frac{(65)(100)(2800)(8.837 \times 10^{-4})}{141.2(1.52)(1.04)} = 72.05$$

Again, Eq. 37 is used to estimate  $\lambda$ ,

$$\lambda = \frac{3792(\phi c_t)_i \mu r_w^2}{k \Delta t_{mf}} \left[ \omega \ln \left( \frac{1}{\omega} \right) \right]$$

$$\lambda = \frac{3792(0.13)(4.34 \times 10^{-5})(1.52)(0.3^2)}{(65)(39.3)} \left[ 0.06 \times \ln \left( \frac{1}{0.06} \right) \right]$$

$$\lambda = 1.94 \times 10^{-7}$$

### 4. ANALYSIS OF RESULTS

It is observed from the simulated examples that the estimated parameters obtained with the equations

developed in this study agree quite well with the input data. However, for the case of a heterogeneous reservoir there is a need to obtain the mechanical skin factor from other sources, so that, dimensionless storativity coefficient,  $\omega$ , which is also required for estimating the skin factor, can be estimated from the correlation (Eq. 31) developed in this study. This manipulation was performed in the field case example. The Warren and Root parameters estimated in this paper do not agree well with those estimated by [10]; however, we consider that they are in an adequate range since these parameters can be within a difference of one order of magnitude.

### 5. CONCLUSION

The straight-line conventional method for rate-transient analysis was complemented with new equations for long and narrow homogeneous and naturally fractured reservoirs. The equations were successfully applied to synthetic examples. A field example for a heterogeneous reservoir was presented to demonstrate the application of the proposed solution.

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### NOMENCLATURE

$B$	Oil formation factor, rb/STB
$b$	Intercept
$b_x$	Well position inside the reservoir
$c_t$	Total system compressibility, 1/psi
$h^t$	Formation thickness, ft
$k$	Permeability, md
$m$	Slope
$P$	Initial reservoir pressure, psi
$P^i$	Well-flowing pressure, psi
$P^{wf}$	Pressure, psi
$s$	Skin factor
$s_r$	Mechanical skin factor
$t$	Time, hr
$W_D$	Dimensionless reservoir width
$X_D$	Dimensionless well position along the x-axis
$X_D^E$	Reservoir length, ft
$Y_D^E$	Dimensionless well position along the y-axis
$Y_D^E$	Reservoir width, ft
$1/q$	Reciprocal flow rate, D/STB
$1/q_D$	Dimensionless reciprocal flow rate

## Greek

$\omega$	Dimensionless storativity coefficient, $(\phi c_t)_f / [(\phi c_t)_m + (\phi c_t)_f]$
$\Delta$	Change, drop
$\phi$	Porosity
$\lambda$	Interporosity flow parameter
$\rho$	Densidad, lbm/ft <sup>3</sup>
$\mu$	Oil viscosity, cp

## Suffices

$e$	External
$D$	Dimensionless
$DL$	Dual linear, dimensionless based on width
$DLF$	Dual-linear flow
$L$	Linear
$LF$	Linear flow
$min$	Minimum
$PB$	Parabolic
$PBF$	Parabolic flow
$w$	Well

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