A hybrid partitioning method for multimedia databases

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Abstract
Hybrid partitioning has been recognized as a technique to achieve query optimization in relational and object-oriented databases. Due to the increasing availability of multimedia applications, there is an interest in using partitioning techniques in multimedia databases in order to take advantage of the reduction in the number of pages required to answer a query and to minimize data exchange among sites. Nevertheless, until now only vertical and horizontal partitioning have been used in multimedia databases. This paper presents a hybrid partitioning method for multimedia databases. This method takes into account the size of the attributes and the selectivity of the predicates in order to generate hybrid partitioning schemes that reduce the execution cost of the queries. A cost model for evaluating hybrid partitioning schemes in distributed multimedia databases was developed. Experiments in a multimedia database benchmark were performed in order to demonstrate the efficiency of our approach.

Keywords: hybrid Partitioning; multimedia databases, query optimization.

Un método de fragmentación híbrida para bases de datos multimedia

Resumen
La fragmentación híbrida es una técnica reconocida para lograr la optimización de consultas tanto en bases de datos relacionales como en bases de datos orientadas a objetos. Debido a la creciente disponibilidad de aplicaciones multimedia, surgio el interés de utilizar técnicas de fragmentación en bases de datos multimedia para tomar ventaja de la reducción en el número de páginas requeridas para responder una consulta, así como de la minimización del intercambio de datos entre sitios. Sin embargo, hasta ahora sólo se ha utilizado fragmentación vertical y horizontal en estas bases de datos. Este artículo presenta un método de fragmentación híbrida para bases de datos multimedia. Este método toma en cuenta el tamaño de los atributos y la selectividad de los predicados para generar esquemas de fragmentación híbridos que reducen el costo de ejecución de las consultas. También, se desarrolla un modelo de costo para evaluar esquemas de fragmentación híbridos en bases de datos multimedia. Finalmente, se presentan algunos experimentos en una base de datos de prueba con el fin de demostrar la eficiencia del método de fragmentación propuesto.

Palabras clave: fragmentación híbrida; bases de datos multimedia, optimización de consultas.

1. Introduction

Query optimization to reduce response time or to avoid the excessive use of system resources has been an active research field over the past decades [1].

Hybrid partitioning is a database design technique to improve query performance. It divides a relation or table into subsets of attributes and tuples in order to minimize the irrelevant data accessed by the queries. Hybrid partitioning has been typically applied to traditional databases (relational or object-oriented databases) to achieve query optimization.

Vertical partitioning divides a table $T$ into a set of fragments $fr_1, fr_2, ..., fr_n$, such that each fragment $fr_i$ contains a subset of the attributes and the primary key of table $T$. In contrast, horizontal partitioning splits table $T$ into a set of fragments $fr_1, fr_2, ..., fr_n$, where each fragment $fr_i$ has a subset of tuples of $T$.

There are two versions of horizontal partitioning: primary and derived. Primary horizontal partitioning of a table is performed by using predicates that are defined on that table. On the other hand, derived horizontal partitioning divides a table according to the predicates that are defined on another table. In this work, only primary horizontal partitioning is considered.

Hybrid partitioning can be accomplished in one of three ways: first, by performing vertical partitioning and then horizontally partitioning the vertical partitions (called VH partitioning), or by first performing the horizontal partitioning and then vertically partitioning the horizontal partitions (called HV partitioning), or by directly taking into consideration the semantics of the transactions [2].

Currently, multimedia applications are highly available [3-5], such as audio/video on demand, digital libraries, electronic catalogues, among others. The rapid development of multimedia applications has created a huge volume of multimedia data, which has exponentially incremented from time to time [6]. A multimedia database is crucial in these applications in order to provide efficient data retrieval.

Distributed and parallel processing on database management systems (DBMS) may improve the performance of applications that manipulate large volumes of data. This may be accomplished by removing irrelevant data accessed during the execution of the queries and by reducing the data exchange among sites, which are the two main goals of the design of distributed databases [7]. Therefore, partitioning techniques have been used in multimedia databases to improve the performance of applications.

Nevertheless, only vertical or horizontal partitioning techniques have been considered by the literature until now. Vertical partitioning reduces the irrelevant attributes accessed by the queries, but all the multimedia objects are stored in a fragment. Many of the queries issued to the multimedia databases only require some objects from the database. In order to improve the performance of the queries in multimedia databases, it is necessary to reduce access to irrelevant attributes and irrelevant objects; this is achieved with hybrid partitioning. For this reason, in this paper we propose a method for hybrid partitioning in multimedia databases. First, our method develops horizontal partitioning and then vertical partitioning, so it is therefore an HV partitioning algorithm.

This paper is structured as follows: in Section 2, the state of the art of hybrid partitioning in traditional and multimedia databases is presented. In Section 3, the Multimedia Hybrid Partitioning (MHYP) algorithm is described. In Section 4, the proposed cost model for the evaluation of different hybrid partitioning schemes is explained. Section 5 shows the performance evaluation of the queries. Finally, Section 6 presents the conclusion and future lines of research.

2. State-of-the-art

In order to clarify the difference between the related work and our approach, we classify them into two classes that are described in the following subsections.

2.1. Hybrid partitioning methods for traditional databases

Most mixed or hybrid partitioning algorithms only consider traditional databases. In [2], algorithms to generate candidate vertical and horizontal fragmentation schemes and a methodology for distributed database design using these fragmentation schemes were proposed for relational databases. They applied vertical and horizontal fragmentation schemes together to form a grid. This grid that consisted of cells was then merged to form mixed fragments.

An analysis algorithm for assisting distribution designers in the fragmentation phase of object oriented databases was proposed in [8]. The analysis algorithm indicated the most adequate fragmentation technique (vertical, horizontal or mixed) for each class in the database schema. In [9] a strategy to carry out the fragmentation phase of the distribution design of object oriented databases was proposed. Their fragmentation strategy has three steps: 1) the analysis, 2) the vertical fragmentation phase, and 3) the horizontal fragmentation phase.

In [10] a UML-based model for mixed fragmentation was presented. They validated their model using a case study with the concepts of attribute usage matrix and predicate usage matrix. A genetic algorithm for mixed fragmentation in relational databases which provides an improvement over previous works which considered vertical and horizontal partitioning separately was discussed in [11,12]. Compared to attribute partitioning only method, the mixed fragmentation design method produced database cost savings up to 69%. A mixed partitioning approach for multi-tenant data schema was provided in [13]. Their approach made a good scalability in multi-tenant shared database, while it can meet the optimal partitioning and multi-division.

Problems of the aforementioned hybrid partitioning methods in applying them to multimedia databases are the following: 1) Some techniques [2,8-10,13] do not consider the size of the attributes in the vertical partitioning stage since multimedia databases tend to be highly varied sizes (e.g., it is not the same to access an id of 8 bytes as a video of 8 MB); it is necessary to take into account the size of the attributes; 2) Some methods [2, 10] are based on affinity, which is the sum of the frequency of the attributes or predicates that are accessed together by the queries. A cost-based method is better for multimedia databases since it can incorporate more information in the creation of a fragment, such as selectivity of the predicates and size of the attributes, as well as the frequency of the queries; 3) Some techniques [2,11,12] only consider the minimization of the number of disk accesses. It is important to also reduce the transportation cost (i.e., the data exchange among sites) in order to optimize the queries in multimedia databases.

The hybrid partitioning method for multimedia databases proposed in this paper solves these problems because it takes into account the size of the attributes, the selectivity of the predicates, and the frequency of the queries to get hybrid fragments, which reduce the number of disk accesses and the transportation cost of the queries.

2.2. Partitioning methods for multimedia databases

The partitioning algorithms that take into account multimedia data only perform vertical or horizontal partitioning. In [14], primary horizontal fragmentation in distributed multimedia databases is addressed. The authors’ partitioning strategy is based on low-level multimedia features.
In [15], semantic-based predicates implication required in current fragmentation algorithms is addressed in order to partition multimedia data efficiently. In [16], a formal approach dedicated to multimedia query and predicate implication is discussed. In [17], a horizontal partitioning algorithm for multimedia databases, called MHPA, is presented. MHPA is based on hierarchical agglomerative clustering.

A vertical partitioning technique was applied in an e-Learning video database system in [18] to achieve efficient query execution. The disadvantage was that this vertical partitioning technique did not consider the transportation cost of multimedia objects over the nodes of the network or the size of the multimedia objects. A vertical partitioning algorithm for distributed multimedia databases, called MAVP (Multimedia Adaptable Vertical Partitioning), is provided in [19], which takes into account the size of the attributes in the partitioning process. In [20], a system for dynamic vertical partitioning of multimedia databases, called DYMOND (DYnamic Multimedia ON line Distribution), is presented. It uses active rules for the dynamic vertical partitioning of multimedia databases, called DYMOND (DYnamic Multimedia ON line Distribution), is presented. It uses active rules for the dynamic vertical partitioning of multimedia databases. In [20], a system for dynamic vertical partitioning of multimedia databases, called MAVP (Multimedia Adaptable Vertical Partitioning), is provided in [19], which takes into account the size of the attributes in the partitioning process. In [20], a system for dynamic vertical partitioning of multimedia databases, called MAVP (Multimedia Adaptable Vertical Partitioning), is provided in [19], which takes into account the size of the attributes in the partitioning process. In [20], a system for dynamic vertical partitioning of multimedia databases, called MAVP (Multimedia Adaptable Vertical Partitioning), is provided in [19], which takes into account the size of the attributes in the partitioning process.

In this section, we first explain the information requirements of the horizontal partitioning process and then we present the steps of the multimedia horizontal partitioning algorithm MHPA.

3.1. Information requirements of horizontal partitioning

In this section, the Multimedia Hybrid Partitioning Algorithm (MHYP) is described in detail. MHYP consists of two phases:

1. Obtaining the horizontal fragments: The predicates of the queries are analyzed in order to obtain the initial horizontal fragments. MHPA [17] is used to obtain the horizontal fragments.

2. Generating the hybrid fragments: MAVP [19] is used to vertically fragment the horizontal fragments obtained in the first phase. As a result this gives the hybrid partitioning scheme.

In order to clarify our approach, we present the following scenario of a simple multimedia database used to manage equipment in a machinery sell company. The database consists of a table named EQUIPMENT (id, name, image, graphic, audio, video) in which each tuple describes information about a specific piece of equipment, including its image, graphic, audio, and video objects. Information regarding 10,000 pieces of equipment (four different types) is stored: 2500 push mowers, 2500 string trimmers, 2500 chain saws, and 2500 water pumps. Let us also consider the following queries:

- $q_1$: Find all chain saws images and graphics
- $q_2$: Find name, audio and video wi id "WP01"
- $q_3$: Find all graphic, audio and video
- $q_4$: Find all water pump images

Similarly to [16], we have considered that data that are stored in a table $T$ can be defined by having two kinds of attributes: atomic and multimedia attributes. Also, we have assumed a fixed attribute set $U=A \cup M$, where:
- $A=[A_1, A_2, \ldots, A_p]$ and each $A_i (i=1, 2, \ldots, p)$ is an atomic attribute associate with a set of atomic values (such as strings and numbers, among others) called the domain of $A_i$ and denoted by $dom(A_i)$.
- $M=[M_1, M_2, \ldots, M_q]$ and each $M_j (j=1, 2, \ldots, q)$ is a multimedia attribute, associated with a set of complex values (represented as sets of values or vectors) called multimedia features (such as, color, texture, shape, to mention a few). The domain of $M_j$ is denoted by $dom(M_j)$.

Thus, given a table $T$ that is defined over $U$, tuples $t$ in $T$ are denoted as $(a_1, a_2, \ldots, a_p, m_1, m_2, \ldots, m_q)$ where $a_i$ is in $dom(A_i)$ ($1 \leq i \leq p$) and $m_j$ is in $dom(M_j)$ ($1 \leq j \leq q$). Every $a_i$ (respectively $m_j$) is denoted by $t.A_i$ (respectively $t.M_j$).

3.1.1. Information requirements of horizontal partitioning

Qualitative and quantitative information about queries is required in order to develop the horizontal partitioning process [7]. Fundamental qualitative information consists of predicates used in user queries. Similarly to [16], the multimedia queries used in our approach are conjunctive projection-selection queries over $T$ of the form $\pi_{X} \sigma_{C}(T)$, where $X$ is a non empty subset of $U$ and $C$ is a conjunction of atomic select predicates, i.e., $C = P_1 \land \ldots \land P_n$ is defined as follows:

**DEFINITION 1**: An atomic selection predicate $P_i$ is an expression of the form $P_i = \theta$ where $A_i \in A$, $a \in dom(A)$ and $\theta = \{=, \leq, \geq, <, >\}$, like $\theta$. Two sets are required in terms of qualitative information regarding user queries:

<table>
<thead>
<tr>
<th>Approach</th>
<th>Multimedia Data</th>
<th>Hybrid Partitioning</th>
</tr>
</thead>
<tbody>
<tr>
<td>Navathe et al. [2]</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Baião and Mattoso [8]</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Jagannatha et al. [10]</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Ng et al. [11]</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Gorila et al. [12]</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Li et al. [13]</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Saad et al. [14]</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Getahun et al. [15]</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Chbeir and Laurent [16]</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Fung et al. [18]</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Rodriguez and Li [19]</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Rodriguez et al. [20]</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>MHYP</td>
<td>Yes</td>
<td>Yes</td>
</tr>
</tbody>
</table>

Source: the authors
1. **Predicate selectivity**: number of tuples of the relation that would be accessed by a user query specified according to a given predicate. If \( P_r = \{ P_1, P_2, \ldots, P_m \} \) is a set of predicates, \( \text{sel}_i \) is the selectivity of the predicate \( P_i \).

2. **Access frequency**: frequency with which user query access data. If \( Q = \{ q_1, q_2, \ldots, q_s \} \) is a set of user queries, \( f_k \) indicates the access frequency of query \( q_k \) in a given period.

### 3.1.2. The steps of the horizontal partitioning algorithm (MHPA)

**Inputs:** The table \( T \) is to be horizontally partitioned, and set of queries with their frequencies are the input data of the MHPA.

**Step 1:** Determine the set of predicates \( P_r \) used by queries defined in the table \( T \). These predicates are defined on a subset of attributes \( A' (A' \subseteq A) \). As in [21], we call each element of \( A' \) a relevant predicate attribute.

The third query \( q_3 \) does not have any predicate because the graphic, audio and video objects of all pieces of equipment are retrieved. Therefore, this query is not relevant for horizontal partitioning; this can be analyzed by the vertical partitioning algorithm. The predicates used by the queries \( q_1, q_2, q_4 \) in our running example are presented in Table 2.

**Step 2:** Build the predicate usage matrix (PUM) of table \( T \). This matrix presents queries in rows and predicates in columns. In this matrix \( \text{PUM}(q_k, P_i) \) is 1 if a query \( q_k \) uses a predicate \( P_i \), otherwise it is 0. PUM also contains the frequency \( f_k \) of each query \( q_k \) and the selectivity \( \text{sel}_i \) of each predicate \( P_i \). The PUM of our running example is shown in Table 3.

**Step 3:** Construct a partition tree. MHPA is based on a bottom-up approach. It first begins with single predicate fragments. It then, forms a new fragment by selecting and merging two of their fragments. This process is repeated until a fragment composed of all predicates is made. This kind of bottom-up approach generates a binary tree, which is called a partition tree (PT) [22]. Fig. 1 shows the PT of the table \( \text{EQUIPMENT} \) obtained by MHPA.

When two fragments are merged, the amount of remote tuples (i.e., tuples located in another fragment) accessed is decreased while the amount of irrelevant tuples accessed by the queries is increased. For example, in Fig. 1 we can observe that in the step 0 each predicate is located in a different fragment. Therefore, in the first fragment there are 2500 tuples (the selectivity of \( P_1 \), i.e., \( \text{sel}_1 \)), in the second one there are only 1 tuple (\( \text{sel}_2 \)), and in the third fragment there are 2499 tuples (\( \text{sel}_3 - \text{sel}_1 \)). Query \( q_1 \) has to access the first fragment, which has the 2500 relevant tuples needed to answer the query. Therefore, it does not have to access any irrelevant tuple and any remote tuple. The same happens to query \( q_2 \). Nevertheless, query \( q_3 \) has to access the second and the third fragments in order to retrieve the tuples with the name "WATER PUMP". It has to access one remote tuple (assuming that the tuple with the id="WP01" is going to be transported from the second fragment to the third fragment).

If the predicates \( P_1 \) and \( P_2 \) are merged into a fragment (as in the step 1 of Fig. 1), query \( q_1 \) now would have to access 1 irrelevant tuple and query \( q_2 \) would have to access 2500 irrelevant tuples.

### Table 2. Predicates used by queries

<table>
<thead>
<tr>
<th>( Q )</th>
<th>( Pr )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( q_1 )</td>
<td>10</td>
</tr>
<tr>
<td>( q_2 )</td>
<td>0</td>
</tr>
<tr>
<td>( q_4 )</td>
<td>20</td>
</tr>
<tr>
<td>( sel )</td>
<td>2500</td>
</tr>
</tbody>
</table>

Source: the authors

### Table 3. Predicate usage matrix.

<table>
<thead>
<tr>
<th>( Q )</th>
<th>( P_1 )</th>
<th>( P_2 )</th>
<th>( P_3 )</th>
<th>( f_k )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( q_1 )</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>15</td>
</tr>
<tr>
<td>( q_2 )</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>10</td>
</tr>
<tr>
<td>( q_4 )</td>
<td>0</td>
<td>0</td>
<td>20</td>
<td></td>
</tr>
<tr>
<td>( sel )</td>
<td>2500</td>
<td>1</td>
<td>2500</td>
<td></td>
</tr>
</tbody>
</table>

Source: the authors

Figure 1. Partition tree of the \( \text{EQUIPMENT} \) table, obtained by MHPA. Source: the authors

If \( P_1, P_2, \) and \( P_3 \) are merged (as in the step 2) \( q_4 \) does not have to access 1 remote tuple (i.e., the tuple with the id "WP01" located in the second fragment). On the other hand, queries \( q_1 \) and \( q_4 \) now would have to access 2500 irrelevant tuples, and query \( q_2 \) now would access 4999 irrelevant tuples. Therefore, the merged fragment will increase the amount of accesses to irrelevant tuples and it will reduce the amount of access to remote tuples.

In MHPA, in each step during the construction of a PT, two nodes (fragments) are selected that maximize the merging profit that is defined below, when they are merged into a node (fragment).

\[
\text{Merging Profit}(H) = DRT - IIT \quad (1)
\]

Where,  
- **DRT**: the decreased amount of remote tuples accessed.  
- **IIT**: the increased amount of irrelevant tuples accessed.

In each step during the construction of a PT, MHPA produces an horizontal partitioning scheme \( ps_i \) which merges two fragments that maximize the merging profit function defined in equation 1. Therefore, when the PT is finished, we have a set of horizontal partitioning schemes \( P = \{ ps_1, ps_2, \ldots, ps_m \} \), and every \( ps_i \) has a set of fragments \( ps_i = \{ f_1, f_2, \ldots, f_r \} \). To select two fragments of \( i \) fragments that can maximize the merging profit (\( \frac{1}{2} \binom{m}{2} \)) pairs should be examined. For example in step 0 \( ps_1 = \{ f_1, f_2, f_3 \} \) of Fig. 1 \( i = m \) (where \( m \) is the number of predicates) because each predicate...
generates the table that were obtained using MHPA.

EQUIPMENT shows the horizontal partitioning schemes of the
and generates a set of initial horizontal fragments. Table 5
end

is located in a different fragment. Therefore, there are three
fragments in Step 0 of Fig. 1 and it is necessary to examine
the merging profits of \( \binom{3(3-1)}{2} = 3 \) pairs and merge one pair
with the maximum merging profit among them. This
generates the \( ps \) of Step 1 in Fig. 1.

Table 4 shows MHPA Merging Profit Matrix (MPM) of
the EQUIPMENT table in Step 0. In Algorithm 1, we show
the process taken to get the MPM.

Algorithm 2 presents MHPA, it uses the PUM of the \( T \)
and generates a set of initial horizontal fragments. Table 5
shows the horizontal partitioning schemes of the
EQUIPMENT table that were obtained using MHPA.

Data: PUM of the table \( T \) (a set of predicates \( Pr = \{ P_1, P_2, \ldots, P_n \} \), the
selectivity \( sel \) of each predicate \( P_0 \), a set of queries \( Q = \{ q_1, q_2, \ldots, q_s \} \), the
frequency \( f_k \) of each query \( q_k \).

Result: MPM: Merging Profit Matrix
for each \( P_i \in Pr \) \( 1 \leq m \) do
for each \( P_i \in Pr \) \( 1 \leq m \) do
    \( DRT = 0; \)
    \( IIT = 0; \)
    merging profit = 0;
    for each \( q_k \in Q \) \( 1 \leq k \leq s \) do
        if \( PUM(q_k, P_i) = 1 \) & \( PUM(q_k, P_j) = 1 \) then
            \( DRT = DRT + f_k * (sel + sel); \)
        else
            \( IIT = IIT + f_k * sel; \)
        end
    end
    merging profit = \( DRT + IIT; \)
    \( MPM(P_i, P_j) = \text{merging profit}; \)
end
Algorithm 1. getMPM

Data: PUM
Result: initial horizontal partitioning schemes \( PS = \{ ps_1, ps_2, \ldots, ps_m \} \)
for each \( x \in PT \) do
    getMPM(PUM, MPM)
    select two nodes with maximum merging profit;
    merge the nodes;
end
Algorithm 2. MHPA

Table 5.
Resulting horizontal fragments of the table EQUIPMENT

\[
\begin{array}{c|c|c|c|c}
\text{PS} & \text{fr}_1 & \text{fr}_2 & \text{fr}_3 \\
\hline
ps_1 & (P_1, P_2, P_3) & & \\
ps_2 & (P_1, P_2) & (P_3) & \\
ps_3 & (P_1) & (P_2) & (P_3) \\
\end{array}
\]

Source: the authors

3.2. Vertical Partitioning Process

MHYP uses the MAVP algorithm to achieve a vertical
partitioning scheme (VPS). MAVP requires an Attribute
Usage Matrix (AUM) as input, which has a set of atomic and
multimedia attributes \( U = \{ A_1, A_2, \ldots, A_p, M_1, M_2, \ldots, M_q \} \). The maximum size \( s_i \) of each attribute \( a_i \) is \( \in U \), it has a set of queries \( \Omega = \{ q_1, q_2, \ldots, q_s \} \), the frequency \( f_k \) of each
query \( q_k \), and it has a set of elements \( AUM(q_k, a_i) \), where
\( AUM(q_k, a_i) = 1 \) if query \( q_k \) uses the attribute \( a_i \) or, if not, \( AUM(q_k, a_i) = 0 \). The AUM of the EQUIPMENT table
is presented in Table 6. MAVP takes into account the size of
the attributes due to its importance in the vertical partitioning
process because it is not the same to access a remote or
irrelevant atomic attribute as it is to access a remote or
irrelevant multimedia attribute. Multimedia attributes tend to
be of a lot larger size. For further details, consider [19].

MAVP finds an optimal VPS when the number of fragments
is equal to two \( vps_2 = \{ \text{id}, \text{audio}, \text{video}, \} , \text{fr}_3 = \{ \text{name, image, graphic} \} \).

3.3. Hybrid partitioning scheme generation

Algorithm 3 shows the MHYP algorithm. MHYP takes
the PUM as an input as well as AUM of table \( T \) of
the multimedia database and generates the optimal hybrid
partitioning scheme (optimal_hps). Algorithm 3 presents the
MHYP algorithm. MHYP obtains an optimal hybrid
partitioning scheme (optimal_hps) based on the PUM and
the AUM of the table \( T \). MHYP uses the PUM to obtain a set of
hybrid partitioning schemes \( PS = \{ ps_1, ps_2, \ldots, ps_m \} \).
In contrast, MAVP only generates one optimal vertical
partitioning scheme (VPS).

HPS_Generator combines the initial horizontal partitioning
schemes generated by MHPA and the VPS
obtained by MAVP. The number of hybrid partitioning
schemes produced by the HPS_Generator is \( m \), i.e., the
number of horizontal partitioning schemes obtained by
MHPA. Therefore, the HPS_Generator obtains a set of
hybrid partitioning schemes \( HPS = \{ hps_1, hps_2, \ldots, hps_m \} \).
Every \( hps \) has a set of fragments \( hps_i = \{ \text{fr}_1, \text{fr}_2, \ldots, \text{fr}_l \} \). Each
fragment \( \text{fr}_k \) has \( m \) attributes. We suppose that the network
has nodes \( N_1, N_2, \ldots, N_l \), the allocation of the fragments to
the nodes gives rise to a mapping \( \lambda : \{ 1, \ldots, l \} \rightarrow \{ 1, \ldots, l \} \), which
is called location assignment [23]. Table 7 depicts the
definition of the \( hps_1 \) fragments.

HPS_Generator obtains two matrices: a Fragment-Attribute
Usage Matrix (FAUM) and a Fragment-Predicate Usage Matrix
(FPUM). FAUM contains a set of atomic and multimedia
attributes \( U = \{ A_1, A_2, \ldots, A_p, M_1, M_2, \ldots, M_q \} \).
..., $M_4\}$, the set of fragments of a hybrid partitioning scheme $hps:=\{fr_1, fr_2, \ldots, fr_t\}$, the sum of the size of the attributes $sfr_k$ of each fragment $fr_k$, and a set of elements $FAUM(fr_k, a_i)=1$ if fragment $fr_k$ has the attribute $a_i$, or, if not, $FAUM(fr_k, a_i)=0$. For instance, Table 8 shows the FAUM of the $hps:=\{fr_1, fr_2, fr_3, fr_4\}$, $sfr_1=saudio+svideo=8+4100+39518=43626$. FPUM presents the fragments in rows and the predicates in columns. In this matrix, $FAUM(fr_k, P_i)=1$ if the fragment $fr_k$ contains the tuples of the predicate $P_i$, or if not, it is 0. In addition, FPUM presents information about the cardinality $cfr_k$ of a fragment $fr_k$. Table 9 presents the FPUM of the $hps_1$, every fragment stores 5000 tuples.

**Data:** PUM, AUM

**Result:** optimal_hps

1. $optimal\_hps=0$
2. $MHPA(PUM, PS)$
3. $MAVP(AUM, VPS)$
4. $HPS, \text{Generator}(PS, VPS, HPS, FAUM, FPUM)$
5. for each $hps \in HPS$ do
   a. $cost(hps)=IDAC(hps)+TC(hps)$
   b. if $cost(hps)<best\_cost$ then
      c. $best\_cost=cost(hps)$
   d. $optimal\_hps=hps$
6. end

Algorithm 3. MHYP

### 4. Cost model

The cost of a $hps$ is composed of two parts: irrelevant data access cost and transportation cost.

<table>
<thead>
<tr>
<th>Table 7.</th>
<th>Fragments of the first hybrid partitioning scheme</th>
</tr>
</thead>
<tbody>
<tr>
<td>$hps_1$</td>
<td>$fr_1=\pi_{s1}, s5, a6 \left(\sigma_{P1 \wedge P2 \wedge P3}(T)\right)$</td>
</tr>
<tr>
<td></td>
<td>$fr_2=\pi_{s1}, s5, a6 \left(\sigma_{\neg P1 \wedge P2 \wedge P3}(T)\right)$</td>
</tr>
<tr>
<td></td>
<td>$fr_3=\pi_{s1}, s2, a3, a4 \left(\sigma_{P1 \wedge P2 \wedge P3}(T)\right)$</td>
</tr>
<tr>
<td></td>
<td>$fr_4=\pi_{s1}, s2, a3, a4 \left(\sigma_{\neg P1 \wedge P2 \wedge P3}(T)\right)$</td>
</tr>
<tr>
<td>$a_i=id, a_i=name, a_i=image, a_i=graphic, a_i=audio, a_i=video, T=EQUIPMENT$</td>
<td></td>
</tr>
</tbody>
</table>

Source: the authors

<table>
<thead>
<tr>
<th>Table 8.</th>
<th>FAUM</th>
</tr>
</thead>
<tbody>
<tr>
<td>$hps_1$</td>
<td>$id$</td>
</tr>
<tr>
<td>fr_1</td>
<td>1</td>
</tr>
<tr>
<td>fr_2</td>
<td>1</td>
</tr>
<tr>
<td>fr_3</td>
<td>1</td>
</tr>
<tr>
<td>fr_4</td>
<td>1</td>
</tr>
</tbody>
</table>

Source: the authors

<table>
<thead>
<tr>
<th>Table 9.</th>
<th>FPUM</th>
</tr>
</thead>
<tbody>
<tr>
<td>$hps_1$</td>
<td>$P_i$</td>
</tr>
<tr>
<td>fr_1</td>
<td>1</td>
</tr>
<tr>
<td>fr_2</td>
<td>1</td>
</tr>
<tr>
<td>fr_3</td>
<td>1</td>
</tr>
<tr>
<td>fr_4</td>
<td>0</td>
</tr>
</tbody>
</table>

Source: the authors

The transportation cost provides a measure for transporting the relevant data and irrelevant tuples accessed during the queries. The transportation cost is given by:

$$cost(hps_i) = IDAC(hps_i) + TC(hps_i)$$

IDAC measures the amount of data from both irrelevant attributes and irrelevant tuples accessed during the queries. The transportation cost provides a measure for transporting between the nodes of the network.

**The irrelevant data access cost is given by:**

$$IDAC(fr_k) = \sum_{k=1}^{t} IDAC(fr_k)$$

In order to obtain the cost of an $hps_i$, it is necessary to use the PUM and the AUM of a table $T$. The irrelevant data access cost of each hybrid fragment $fr_k$ is given by:

$$IDAC(fr_k) = IAAC(fr_k) + ITAC(fr_k)$$

IAAC is the irrelevant attribute access cost. ITAC is the irrelevant tuple access cost. IAAC is defined as:

$$IAAC(fr_k) = \sum_{q_j \in IQ_k} IAAC(q_j)$$

$$IAAC(q_j) = \begin{cases} \sum_{a_i \in \Lambda q_j, P_j \in PUM} s_i \cdot cfr_k & \text{if } q_j \in PUM; \\
\sum_{a_i \in \Lambda q_j, P_j \in PUM} \sum_{P_j \in PUM} s_i \cdot cfr_k & \text{otherwise} \end{cases}$$

where $IQ_k$ is a set of queries that uses at least one attribute and accesses at least one irrelevant attribute of the fragment $fr_k$. This is:

$$IQ_k = \{q_j\}_{AUM(q_j, a_i) \neq 0 \wedge AUM(q_j, a_i) = 1 \wedge \{a_i, a_i\} \in fr_k}$$

$$\{a_i, a_i\} \in fr_k \Rightarrow FAUM(fr_k, a_i) = 1 \wedge FAUM(fr_k, a_i) = 1$$

IA is the set of attributes that is not used by query $q_j$ in IQ_k. This is defined as:

$$IA_k = \{a_i\}_{AUM(q_j, a_i) \neq 0 \wedge FAUM(fr_k, a_i) = 1}$$

In the example $\{q_3\}$ because $q_3$ does not use the attribute $id$ but it needs the attributes $audio$ and $video$ from the fragment $fr_1$ of the $hps_1$. Therefore, $IA_k=\{id\}$.

$PQ_j$ is the predicates used by a query $q_j$ and is located in the fragment $fr_k$.

$$PQ_j = \{P_i\}_{PUM(q_j, P_i) \neq 0 \wedge FPUM(fr_k, P_i) = 1}$$

For $fr_1$, $PQ_1=\{P_1\}$, $PQ_2=\{P_2\}$, $PQ_3=\{\emptyset\}$, $PQ_4=\{P_3\}$ because the predicates $P_1$, $P_2$, $P_3$ are accessed by the queries $q_1$, $q_2$, $q_4$ and the tuples required by the predicates are located in the fragment $fr_1$.

ITAC can be written as:
to a given location assignment. Since transportation costs depend on the number of relevant remote tuples accessed by the query, which are the sizes of the relevant remote attributes, squared, i.e.

\[ \text{ITAC}(q_j) = \begin{cases} f_j \left( sf_{fr_k} \left( cf_{fr_k} - \sum_{p \in P(j)} sel_t \right) \right) & \text{if } n_p \geq 1; \\ 0 & \text{otherwise} \end{cases} \]  

(12)

where \( n_p \) is the number of predicates in \( P[q_j] \), and \( AQ_j \) contains the queries that access at least one attribute of the fragment \( fr_k \).

\[ AQ_j = \{ q_j | AUM(q_j, a_i) = 1 \land FAUM(fr_k, a_i) = 1 \} \]  

(13)

In the example for the fragment \( fr_1 \), \( AQ = \{ q_2, q_3 \} \), since the query \( q_2 \) accesses all the attributes of the fragment \( fr_1 (id, audio, video) \) and \( q_3 \) accesses the attributes audio and video of \( fr_1 \). Due to the fact that \( PQ_1 = \{ P_2 \} \) and \( PQ_2 = \{ \Omega \} \), only the query \( q_2 \) contributes to the access to irrelevant tuples.

The transportation cost of an \( hps \), is computed according to a given location assignment. Since transportation costs dominate the execution cost of a query [7], the TC of \( hps \) is the sum of the costs of each query multiplied by its frequency squared, i.e.

\[ TC(hps_i) = \sum_{j=1}^{4} TC(q_j) \cdot f_j^2 \]  

(14)

The transportation cost of query \( q_j \) depends on the size of the relevant remote attributes and on the assigned locations, which decide the transportation cost factor between every pair of sites. It can be expressed by:

\[ TC(q_i) = \sum_{h} c_{k,h} \cdot h^{\lambda(h)} \cdot s(h) \cdot sel(h') \]  

(15)

where \( h \) ranges over the nodes of the network for \( q_i \), \( s(h') \), which are the sizes of the relevant remote attributes, \( sel(h') \) is the number of relevant remote tuples accessed by the query, \( q_i \), \( \lambda(h) \) indicates the node in the network at which the query is stored, and \( c_{h} \) is a transportation cost factor for data transportation from node \( N_i \) to node \( N_j \) \( \{ i, j \in \{1, \ldots, t\} \} \) [23]. For instance, Table 10 presents the IAAC, ITAC, and IDAC of the \( hps_1 \) in megabytes. \( \text{IAAC}(fr_1)=\text{IAAC}(q_1) \), \( \text{IAAC}(q_3)=h' \cdot sf_{fr_1} \cdot cf_{fr_1} \cdot sel_t \cdot s(name) = 1 \) million of bytes=1 MB. \( \text{ITAC}(fr_1)=h' \cdot cf_{fr_1} \cdot sel_t \cdot s(name) = 10^{4} \cdot 3626 \cdot 5000 \cdot 1=2180.86 \) MB.

The TC(hps_1) of MHYP is calculated as follows: there are four fragments, so we suppose that there are four nodes \( N_1 \), \( N_2 \), \( N_3 \), \( N_4 \), and each fragment \( fr_1 \) is located in each node \( N_i \). We also assume that each query is located in the node in which the larger attribute that it uses is located, and \( c_{h}=1 \).

Table 11 contains the costs of the hybrid partitioning schemes generated by MHYP. The optimal scheme is \( hps_3 \) and has a cost of 139691.31 MB.

### 5. Evaluation

This section presents and compares the hybrid partitioning schemes obtained using MHYP, the vertical partitioning scheme generated by MAVP, and the horizontal partitioning generated by MHPA. The benchmark used for the comparison was the database of a machinery sales company used in [19, 20] and described in Section 3. Some hybrid partitioning methods, such as [2, 11, 12] consider that the response time of a query is strongly affected by the amount of data accessed from secondary storage (disk). Hence, the objective functions of these methods are to minimize the number of disk accesses. The cost model proposed in this paper is used to compare the schemes obtained by MHPA, MAVP and MHYP since the cost to perform queries in distributed systems is dominated by the remote network communication as well as by local disk accesses.

Table 12, 13 and 14 compare the costs of the queries of MHPA, MAVP and MHYP. As it can be observed, the scheme obtained with MHYP has a lower cost in most queries. This is because MHPA only takes into account

Table 10.

<table>
<thead>
<tr>
<th>hps_1</th>
<th>IAAC (fr_1)</th>
<th>ITAC (fr_1)</th>
<th>IDAC (fr_1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>fr_1</td>
<td>1</td>
<td>2180.86</td>
<td>2181.86</td>
</tr>
<tr>
<td>fr_2</td>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>fr_3</td>
<td>141.71</td>
<td>196.34</td>
<td>338.05</td>
</tr>
<tr>
<td>fr_4</td>
<td>116.00</td>
<td>0.00</td>
<td>116.00</td>
</tr>
</tbody>
</table>

Source: the authors

Table 11.

<table>
<thead>
<tr>
<th>hps</th>
<th>Cost</th>
<th>TC</th>
<th>ITAC</th>
</tr>
</thead>
<tbody>
<tr>
<td>hps_1</td>
<td>2636.91</td>
<td>139431.25</td>
<td>142068.16</td>
</tr>
<tr>
<td>hps_2</td>
<td>1386.50</td>
<td>139431.62</td>
<td>140818.12</td>
</tr>
<tr>
<td>hps_3</td>
<td>259.70</td>
<td>139431.61</td>
<td>139691.31</td>
</tr>
</tbody>
</table>

Source: the authors

Fig. 2 illustrates the local assignment of \( hps_1 \). The query \( q_2 \) requires one tuple with the attribute \( name \), which is located in the fragment \( fr_3 \). Therefore \( TC(q_2)=s_{name} \cdot sel_t \cdot sf_{fr_1} = 20 \times 1 \times 10^{4} = 2000 \) bytes.
information about the irrelevant tuples accessed by queries, MAVP focuses on the reduction of irrelevant attributes, and MHYP considers the size of the irrelevant attributes and the selectivity of the predicates in order to reduce both irrelevant attributes and tuples accessed by the queries. Using this information, MHYP considerably reduces the cost of the queries.

The cost of the query \( q_3 \) is increased in MHYP because it needs all graphic, audio and video of the multimedia database. In the scheme of MHPA, this query only accesses 5000 remote graphic objects. The transportation cost of this query is considerably reduced in the MAVP scheme because it only has to access 10000 remote graphic objects. The scheme obtained by MHYP accesses 5000 remote audio and video objects and 10000 remote graphic objects, so its transportation cost is increased. Most of the queries executed in multimedia databases tend to access only a subset of attributes and tuples of the database; therefore, hybrid partitioning is suitable for these databases in order to reduce query execution cost.

6. Conclusion and future work

Hybrid partitioning optimizes query execution cost because it reduces the irrelevant data accessed by the queries. The novel aspects of our work include the following research contributions: first, a hybrid partitioning algorithm for distributed multimedia databases has been developed, which takes into account the size of the attributes and the selectivity of the predicates to generate an optimal hybrid partitioning scheme. Second, a cost model for distributed multimedia databases has been proposed. This cost model considers that the overall query processing cost in a distributed multimedia environment consists of irrelevant data access cost and transportation cost. An experimental evaluation shows that the algorithm proposed in this paper outperforms both a horizontal and a vertical partitioning only algorithm in most cases.

In this research we assumed that the queries that run against the multimedia database are static. Distributed multimedia databases are accessed by many users simultaneously, therefore queries tend to change over time and a good hybrid partitioning scheme can be degraded, resulting in very long query response time. Present research could be extended to derive the hybrid partitioning dynamically in multimedia databases (MMDBs) based on the changes in the queries. Thus, the hybrid partitioning scheme of the multimedia database can be adaptively modified to always achieve efficient retrieval of multimedia objects.

In the future, we also wish to consider low-level features of multimedia data and similarity-based (range and \( k \)-nearest neighbor) queries in the hybrid partitioning process. These kinds of queries are needed for content-based retrieval, which consists of obtaining information from the MMDB according to the characteristics of the multimedia objects, such as color, texture, and shape (in the case of images).

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