## EARTH SCIENCES RESEARCH JOURNAL

Earth Sci. Res. J. Vol. 20, No. 3 (September, 2016): H1-H7



## Research into the effects of seawater velocity variation on migration imaging in deep-water geology

Hui Sun<sup>1</sup>, Jianguo Sun<sup>2</sup>, Fuxing Han<sup>1</sup>, Zhangqing Sun<sup>1</sup>, Zhiqiang Liu<sup>1</sup>, Mingchen Liu<sup>1</sup>, Xingguo Huang<sup>1</sup>
College for Geoexploration Science Technology, Jilin University, Changchun, 130026
Correspondence should be addressed to Jianguo Sun, e-mail: sun jg@jlu.edu.cn

### ABSTRACT

This paper aims at the problem that the migration quality is poor in deep water. It analyzed the influence that velocity model accuracy had on migration and studied the impact that variable seawater velocity makes on movement effect. At first, variable seawater velocity affected by temperature, pressure, and salinity is defined to replace the actual seawater velocity. Then variable seawater velocity's influence on interface migration location, layer sickness and movement energy focusing degree are analyzed in theory. Moreover, finally, a deep water layered medium model containing variable seawater velocity, a syncline wedge shape model, and a complex seafloor velocity model are constructed. By changing the seawater velocity of each model and comparing migration results of constant seawater velocity model and variable seawater-velocity model, it was found the conclusion. Under the condition of deep water, variable seawater velocity's impact on the quality of seismic migration is significant, which not only can change the location of geologic body migration result but also can influence the resolution of the geologic interface in the movement section and maybe can cause migration illusion.

Keywords:Seawater velocity, Deep-water geology, Migration Imaging, Migration velocity

## Investigación de los efectos de la variación en la velocidad del agua marina sobre las imágenes de

## migración en la geología de aguas profundas

## RESUMEN

Este artículo se enfoca en el problema de la baja calidad de la migración en aguas profundas. Se analiza la influencia que tiene el modelo de precisión de velocidad en la migración y se estudia el impacto que la variación de velocidad del agua marina tiene en el efecto de movimiento. En primera instancia, se define la variación de la velocidad del agua marina afectada por la temperatura, la presión y la salinidad para reemplazar la velocidad del agua marina actual. Luego se analiza la teoría de la influencia de la velocidad del agua marina sobre la interfaz de la ubicación de migración, el grosor de la capa y la energía de movimiento de acuerdo con la inclinación. Además, finalmente, se construyó un modelo medio por capas de aguas profundas que contiene las variaciones de velocidad del agua marina, un modelo de forma de cuña sinclinal, y un modelo de complejo de velocidad se encontró la conclusión. Bajo las condiciones de agua profunda, el impacto de la variación de la velocidad del agua es significativo en la migración sísmica, lo que no solo puede cambiar el resultado de migración en la ubicación del cuerpo geológico sino que además puede influir en la resolución de la interconexión geológica en la sección de movimiento y podría causar la ilusión de migración.

Palabras clave: velocidad del agua marina, geología de aguas profundas, imágenes de migración, velocidad de migración.

Record

Manuscript received: 22/03/2016 Accepted for publication: 23/11/2016

#### How to cite item

Sun, H., Sun, J., Han, F., Sun, Z., Liu, Z., Liu, M., & Huang, X. (2016). Research into the effects of seawater velocity variation on migration imaging in deep-water geology. Earth Sciences Research Journal, 20(3), J1-J6. doi:http://dx.doi.org/10.15446/esrj.v20n3.56382

#### Introduction

As more and more offshore oil and gas fields have been discovered recently, the exploration difficulty for new ones increases sharply. Thus, growing number of human and financial resources has been invested into deep-sea oil and gas exploration worldwide (Barely, 1999). The South China Sea is rich in oil resource while 70% of that located in the deep sea (Li, 2006). During latest ten years the South China Sea oil and gas exploration experienced both more and more attention from the government and also a series of problems of which one exists in migration processing on marine seismic data. The problem can be described as the movement energy not high enough in deep water so that the real structure and stratum could not be recognized clearly and exactly. The paper aims at solving it, thus analyzes the affection of variable seawater-velocity on migration in deep water from the perspective of velocity model's accuracy.

Physical oceanography study reveals that the main influencing factors on the acoustic velocity of seawater are temperature, pressure, and salinity (Feng, 1999; Jones, 1999) which are also correlated with depth. Therefore, seawater acoustic velocity is a function of depth as well. It is well known that pre-stack depth migration is so sensitive to velocity model that even a tiny error could change the final result (Versteeg, 1993; Herron, 2000). The seawater velocity is always processed as constant speed during marine seismic data processing. Such processing has little affection on seismic data of shallow seawater but a big one on that of deep water which could not be neglected.

The relationship between seawater velocity and wave field propagation has been studied and concluded by many researchers as follows. Dyk and Swainson (1953) drew the conclusion from the perspective of kinematics that the seawater acoustic velocity which varies as depth has a great effect on ray path. Barley (1999) pointed out in his paper that seawater velocity variation is one of the important reasons that reduce the efficiency of marine seismic data processing. Mackey and Fried (2003) revealed further that it not only affects the event continuity of marine seismic data but also influences stack section showing inaccuracy amplitude information and wrong submarine tectonics. The similar question is put forward by Lacombe et al. (2006), that seawater velocity variation can cause seismic event dislocation. Xu and Pham (2003) and Jones (2010) studied seismic imaging and achieved the conclusion that variable seawater velocity sets back seabed imaging. Papenberg et al. (2010) and Song et al. (2010), who used seismic data to achieve the temperature and salinity variation curve form with the depth of seawater, provide the theory basis of variable seawater velocity employed in this paper. The influence of seawater velocity on seismic travel time, ray path, and amplitude is revealed based on empirical formulas of temperature, depth, and salinity (Han et al., 2012).

The paper firstly studies the practical method of seawater acoustic velocity and draws the variation curve of acoustic velocity with depth. Then based on that method, the effect of the speed is researched theoretically on interface deviation, layer thickness, and focusing of migration energy. Finally, a layered model, a syncline model, and a complex model are built to contrast movement results between variable seawater-velocity models and constant seawater-velocity models and reveal the effect of variable velocity on migration imaging in deepwater geology structure.

#### 2. Methodology

#### 2.1 Construction of seawater acoustic velocity model

Seawater velocity is a function of temperature, salinity, and pressure and always described in empirical formula. The one it was applied in this paper is the Wilson empirical formula simplified by Frye and Pughfrom (Feng, 1999).

$$c = 1449.30 + \Delta c_{t} + \Delta c_{s} + \Delta c_{p} + \Delta c_{tsp}$$

$$\Delta c_{t} = 4.587t - 5.356 \times 10^{-2} t^{2} - 2.604 \times 10^{-4} t^{3}$$

$$\Delta c_{s} = 1.19(S - 35) + 9.6 \times 10^{-2} (S - 35)^{2}$$

$$\Delta c_{p} = 1.5848 \times 10^{-1} p + 1.572 \times 10^{-5} p^{2} - 3.46 \times 10^{-12} p^{4}$$

$$\Delta c_{tsp} = 1.35 \times 10^{-5} t^{2} p - 7.19 \times 10^{-7} tp^{2} - 1.2 \times 10^{-2} (S - 35)t$$
(1)

In the above formulas c represents seawater velocity, t expresses time, S means salinity and p describes pressure. Variable seawater-velocity model intuitively reflects the position relationship between seawater velocity and depth. Thus temperature, pressure and salinity's relationship with depth are needed. The changed law of pressure with depth is quite simple in linear form as is shown in Figure 1a. Temperature and salinity variation with depth are rather complicated because of sun radiation, ocean current, water masses and so on. The temperature and salinity are assumed to change evenly with depth in different extreme sections. Then approximate variation curve of temperature and salinity with depth is formed in consideration of physical oceanography knowledge and temperature and salinity data (Jones, 1999; Chen and Wen, 2010; Zhao, 1985) collected in a region of South China Sea in summer as is shown in Figure 1b and Figure 1c. The variable seawater velocity curve with depth is obtained after the equal pressure, temperature and salinity are calculated in Equation 1.



Figure 1. The changing curve of pressure a, temperature b, salinity c and seawater velocity d in depth

#### 2.2 Effect of seawater velocity error on pre-stack depth migration

The accuracy of velocity has a direct influence on migration and even stronger impact on pre-stack depth migration. In this section, the effect of seawater velocity on seawater movement is analyzed theoretically.

In migration, imaging  $\mathcal{V}_m$  is assumed to be constant seawater movement velocity and  $\mathcal{V}(\mathbf{Z})$  is the function of actual seawater velocity with depth. In seawater velocity model including horizontally stratified medium, each interface can still be recognized in migration section even when there is a significant difference between  $\mathcal{V}_m$  and true seawater velocity. However, the position of each interface changes as well as the layer thickness. The following part will discuss the influence of seawater velocity on interface position and layer thickness quantitatively.



Figure 2. The sketch map of layers

The Figure 2 shows the seawater velocity model including the horizontally stratified medium in which  $h_1$  describes seawater layer's thickness while  $h_{n+1}$  represents the *n*th horizontal stratified medium's thickness. Zero offset time of geophone through single pass from interface one can be described as follows.

$$t_{securater} = \int_{0}^{h} \frac{1}{\nu(z)} dz, \quad \mathbf{v}_{average} = \frac{h_{1}}{t_{securater}}$$
(2)

 $t_{seawater}$  and  $\mathbf{V}_{average}$  respectively represents zero offset time of single pass and average seawater velocity. The whole layer position will climb when migration velocity  $\mathcal{V}_m$  is lower than  $\mathbf{V}_{average}$ . Meanwhile, each layer is assumed to be thick enough to acquire the exact position and climbing height of each one as is shown below.

$$\dot{h}_{1} = t_{seawater} * v_{m}, \quad \Delta h_{1} = h_{1} - \dot{h}_{1} = (\frac{h_{1}}{v_{m}} - t_{seawater}) * v_{m}$$
  
$$\dot{h}_{2} = h_{1} + h_{2} - (\frac{h_{1}}{v_{m}} - t_{seawater}) * v_{2}, \quad \Delta h_{2} = (\frac{h_{1}}{v_{m}} - t_{seawater}) * v_{2}$$
(3)

$$h_n = h_1 + h_2 + \dots + h_n - \left(\frac{h_1}{\nu_m} - t_{secawater}\right) * \nu_n, \quad \Delta h_n = \left(\frac{h_1}{\nu_m} - t_{secawater}\right) * \nu_n$$

In the function,  $h_n$  means the migration depth of the *n*th interface and  $\Box h_n$  demonstrates the difference between migration depth and real depth. As is shown in Equation 3 migration position error of the *n*th interface correlates with seawater migration velocity  $v_m$  and velocity in the overlying layer  $v_n$ , which decreases with  $v_m$  and increases with  $v_n$ . Because of different speed in overlaying layers for a different interface, thus the climbing height of each layer is different in migration section. Therefore, movement thickness is different from the true layer thickness.

$$h_{n,n-1} = h_n - (\frac{h_1}{v_m} - t_{sequencer}) * (v_n - v_{n-1})$$
(4)

In the above function,  $h_{n,n[1]}$  means the thickness of the horizontal layer between nth and n[1th interface. The average geological structure enjoys bigger velocity in the downside strata. When  $\mathcal{V}_m$  is lower than  $\mathbf{V}_{average}$ , the thickness of horizontal stratified medium decreases. Furthermore, the more significant the overlying stratum velocity is, the less the migration thickness of the layer is.

When  $\mathcal{V}_m$  is higher than  $\mathbf{V}_{average}$ , Migration location of each interface will fall.

$$\dot{h_1} = h_1 + (t_{seawater} - \frac{h_1}{v_m}) * v_2, \quad \Delta h_1 = (t_{seawater} - \frac{h_1}{v_m}) * v_2$$
(5)

$$\dot{h_n} = h_1 + h_2 + \dots + h_n + (t_{seawater} - \frac{h_1}{v_m}) * v_{n+1}, \quad \Delta h_n = (t_{seawater} - \frac{h_1}{v_m}) * v_{n+1}$$

It can be seen from the functions that migration position error is directly proportional to movement velocity in seawater. Different from the condition when movement velocity in seawater is lower than average speed, it is velocity in the strata below the interface that affects migration location error as well as the thickness of each horizontal layers.

$$h_{n,n-1} = h_n + (t_{seawater} - \frac{h_1}{\nu_m}) * (\nu_{n+1} - \nu_n)$$
(6)

The Equation 6 shows that when migration velocity is higher in seawater, the movement thickness of the horizontal layer will increase.



Figure 3. The sketch map of simple layers

In the Figure 3, the horizontal strata below the seawater have the velocity of 2500m/s and the thickness of 1000m while the second horizontal stratified medium enjoys the velocity of 3500m/s. Velocity in seawater varies with depth and velocities at different depth can be matched in Figure 1d. Table 1 shows the location error of interface one and thickness error of layer one in corresponding migration velocity at a different depth.

 
 Table 1: The location error of interface one (m) and thickness error of layer one (m)

	Migration location error of interface					Migration thickness error of layer					
depth( m)	one(m)					one(m)					
	v= 1460	v= 1480	v= 1500	v= 1520	v= 1540	v= 1460	v= 1480	v= 1500	v= 1520	v= 1540	
	(m/s)	(m/s)	(m/s)	(m/s)	(m/s)	(m/s)	(m/s)	(m/s)	(m/s)	(m/s)	
2600	-100	-48	-14	+34	+90	-74	-36	-12	+10	+32	
2800	-106	-52	-14	+38	+98	-80	-36	-10	+14	+38	
3000	-114	-54	-14	+44	+108	-82	-38	-10	+14	+40	
3200	-120	-56	-14	+48	+116	-88	-40	-10	+16	+44	
3400	-128	-60	-14	+50	+124	-94	-42	-12	+18	+46	

Remarks: + means the falling of migration location and the increase of migration thickness of the 1th layer. Otherwise,

#### shows the climbing of migration area and the decrease of migration thickness of 1st layer

The data given in Table 1 are consistent with the analysis conclude before. The effect of variable seawater velocity on interface location and layer thickness has been taken into consideration. However, its influence on migration energy focusing can not be neglected as well.

Supposing v represents Seawater acoustic velocity and  $v_m$  is the applied migration velocity, the function of migration depth is obtained of common imaging point gathers by Zhu (1998).

$$z_m^2 + (1 - \beta^2) x^2 = \beta^2 z^2$$
<sup>(7)</sup>

In Equation 7,  $z_m$  acts as migration depth and  $\mathbf{b} = v_m / v$  exists. When migration velocity is smaller,  $\mathbf{b}$  is less than 1, otherwise  $\mathbf{b}$  is more than 1. After then  $\mathbf{d} = \prod v_m / v$  and  $z_m = z + \prod z$  are calculated in Equation 7, the Equation 8 is acquired.

$$2z\Delta z + \Delta z^2 = 2\delta z^2 + \delta^2 z^2 + \delta^2 x^2 + 2\delta x^2$$
(8)

In marine data processing,  $\Delta z$  is less than z and velocity variation is much lower than true velocity. The Equation 9 can be obtained after second order term of

 $\Delta z$  and  $\delta$  are omitted.

$$\Delta z = \frac{\Delta v_m z}{v} \left( 1 + \frac{x^2}{z^2} \right) \tag{9}$$

Based on functions above, the CIGs of an impulse response was drawn in Figure 4 to illustrate velocity error's impact on CIGs. Figure 4 shows that when seawater migration velocity is quite low, the orbit of pulse imaging points is the one above the true orbit. When the seawater movement speed is higher, the orbit of pulse imaging points is the one below the true orbit. What's more, depth error of the migration will increase with the growth of horizontal distance to object point. The velocity will affect the focusing of the movement energy and lower the effectiveness of migration imaging of marine geology structure.



#### 3. Examples and Results

A layered model, a syncline model, and a complex model were built and then it was simulated to acquiring the seismic record. The effect of variable velocity on geology structure migration in deep water is achieved after the contrast between true velocity model and different constant seawater velocity model. Seawater velocity in the three models all takes temperature, pressure, and salinity into consideration. The Figure 1d describes variable seawater velocity curve with depth.

# 3.1 Influence of variable seawater velocity on migration of horizontally stratified medium

The Figure 5 demonstrates the horizontally stratified medium model in deep water with the size of a 1501 x 1601, grid spacing of  $4m \times 4m$  and seawater depth of 3500m at which the data is collected in a region of South China Sea. The horizontally stratified medium can be divided into three layers whose velocity are respectively 3250m/s, 4000m/s and 4750m/s from up to down.



Figure 5 Layered model in deep water

Firstly, the migration of true velocity model is obtained and then the seawater velocity is substituted with different constant seawater velocities, 1450m/s, 1470m/s, 1500m/s, 1520m/s, 1570m/s, to get similar constant velocity model and migration section of each one as is shown in Figure 6. The contrast of movement results in different models shows that when seawater velocity is 1450m/s the lower the layer is, the higher the horizontal interface climbs. Though three interfaces can be demonstrated in migration section, movement energy can not be entirely focused on each interface but both on the interface and the area above it. The more shallow the interface location is, the less focused the energy is in the interface. As the increase of migration velocity of seawater, the upward movement of each interface decreases and migration energy focus strengthens. When seawater velocity is 1500m/s, the movement result which still has some difference with the one achieved at variable velocity is most similar to the original model. As the increase of migration velocity of seawater, the downward movement of each interfaces and is directly proportional to the depth of interface. Movement energy mainly distributes on the interface and in the region below it.



Figure 6. Migration results of layered model in deep water, the corresponding seawater velocity of **a**, **b**, **c**, **d**, **e**, **f** is true seawater velocity 1450m/s, 1470m/s, 1500m/s, 1570m/s

# 3.2 Influence of variable seawater velocity on migration of syncline model

The Figure 7 shows the syncline model in deep water with the size of  $1501 \\ 1601$ , grid spacing off  $4m \\ 4m$  and seawater depth of 3500m. The horizontally stratified medium can be divided into three layers whose velocity are respectively 2500m/s, 3000m/s and 3500m/s. The velocity of wedge geologic body is 5500m/s.



Figure 7. Syncline model in deep water

The Figure 8 demonstrates the variable seawater velocity model of syncline and migration corresponding to constant seawater velocity model at the speed of 1450m/s, 1470m/s, 1500m/s, 1520m/s and 1570m/s. The contrast of migration results in different models reveals that when seawater velocity is 1450m/s all movement location are higher than true interface position. The distance between two horizontal layers decreases as well as the angle of wedging geology body. Migration interface of syncline is steeper than original interface. Movement energy is not well focused on interfaces but also distributed in the region above migration interface. As the increase of seawater velocity, the location of movement section and radian of syncline interface decreases. The distance between two layers increases and the focus of migration energy is improved. When seawater velocity is 1520m/s, the movement result is most similar to the one applying real seawater velocity. When seawater velocity is as high as 1570m/s, radian of syncline interface and distance between two horizontal layers decreases and migration section moves downside. Meanwhile, energy is scattered both above and under movement interface. Therefore, the shape of movement interface is a quite different from that of the true interface.



Figure 8. Migration results of syncline model in deep water, the corresponding seawater velocity of **a**, **b**, **c**, **d**, **e**, **f** is true seawater velocity, 1450m/s, 1470m/s, 1500m/s, 1570m/s

#### 3.3 Effect of variable seawater velocity on complex seabed geology structure model in deep water

The Figure 9 displays the complex seabed geology structure model in deep water with the size of  $1501 \hfill 1601$  and grid spacing of  $4m \hfill 4m$ . Velocities of layer in the model are respectively 2500m/s, 2700m/s, 2900m/s, 3000m/s, 3100m/s, 3300m/s and 3500m/s from up to down. The velocity of embed body on the right side is 3300m/s.



Figure 9. Complex model in deep water

Figure 10 illustrates migration results of complex model in deep water at constant seawater velocity of 1450m/s, 1470m/s, 1500m/s, 1520m/s, 1570m/s. It can be concluded from the contrast of these migration sections that when seawater velocity is 1450m/s all interfaces move upward in the migration section. At different depth, different horizontal position in migration section moves upwards in different distances which increase with deeper depth of the sea. Furthermore, movement energy of interfaces cannot be well focused mainly on interface two and interface three whose interfaces can not be recognized clearly in migration section. Meanwhile, the up and down interfaces are also unable to be connected to embed layer. When seawater velocity is 1470m/s or 1500m/s, the problem is partially improved in contrast with the condition when the velocity is 1450m/s but still having a severe influence on migration results. Then when the seawater velocity is as high as 1520m/s, movement achieves the best result among ones of constant seawater velocity. However, migration energy still can not be well focused. Afterward, when the velocity is 1570m/s, the up and down interfaces can not be connected to embed layer. Interfaces can be recognized reluctantly but in low resolution. In comparison with a true condition, there is a marked difference in space position and geometry.



Figure 10. Migration results of complex model in deep water, the corresponding seawater velocity of **a**, **b**, **c**, **d**, **e**, **f** is true seawater velocity 1450m/s, 1470m/s, 1500m/s, 1520m/s, 1570m/s.

### 4. Conclusions

Acoustic velocity of seawater is mainly influenced by temperature, pressure, and salinity and is also correlated with depth. The seawater acoustic velocity is always processed as constant velocity during marine seismic data processing. Such processing has a severe effect on seismic data of deep seawater which can not be neglected. Meanwhile, the accuracy of velocity model can influence accuracy and results of migration. This paper begins with improving the weaker movement field and worse migration results in deep water region of South China Sea and then analyzes effects of seawater velocity on migration results. It can be concluded from layer model and syncline including wedge model that variable velocity has an adverse influence on interface location, the shape of geology body and focusing on migration energy. The analysis of complex seabed geology model reveals that variable seawater velocity can make interfaces of geology body hard to be distinguished in movement section. Furthermore, variable speed even leads movement section to show wrong geology structure. Therefore, seawater velocity should not be only taken as constant in deep-water seismic data processing.

#### 5. Acknowledgments

This study was supported financially by the National Natural Science Foundation of China (42174120, 41404085, 41504084). We are grateful to Danian Huang of Jilin University, Changchun, for his kind computer supporting.

#### References

- Barley, B. (1999). Deepwater problems around the word. The Leading Edge, 18(4), 488-493. DOI: 10.1190/1.1438319
- Chen, J., & Wen, N. (2010). The geophysical atlas of the South China Sea. Science Press, Beijing.
- Dyk, K., & Swainson, O. W. (1953). The velocity and ray paths of sound waves in deep sea water. Geophysics, 18(1), 75-103. DOI: 10.1190/1.1437867
- Feng, S. Z. (1999). Marine science introduction. Higher Education Press, Beijing.

- Han, F. X., Sun, J. G., & Wang, K. (2012). The influence of seawater velocity variation on seismic traveltimes, raypaths, and amplitude. Applied Geophysics, 9(3), 319-325.
- Herron, D. A. (2000). Pitfalls in seismic interpretation: Depth migration artifacts. The Leading Edge, 19(9), 1016-1017. DOI: 10.1190/1.1438756
- Jones, E. J. W. (1999). Marine Geophysics. John Wiley & Sons, England.
- Jones, S. M., Sutton, C., Hardy, R. J. J. & Hardy, D. (2010). Seismic imaging of variable water layer sound speed in Rockall Trough, NE Atlantic and implications for seismic surveying in deep water. Geological Society, London, Petroleum Geology Conference series 7, 549-558. DOI: 10.1144/0070549
- Lacombe, C., Schultzen, J., Butt, S., & Lecerf, D. (2006). Correction for water velocity variations and tidal statics. 68th EAGE Conference & Exhibition. DOI: 10.3997/2214-4609.201402385
- Li, Q. P. (2006). The situation and challenges for deepwater oil and gas exploration and exploitation in China. China Offshore Oil and Gas, 18(2), 130-133.
- MacKay, S., Fried, J., & Carvill, C. (2003). The impact of water-velocity variations on deepwater seismic data. The Leading Edge, 22(4), 344-350
- Papenberg, C., Klaeschen, D., & Krahmann, G. (2010). Ocean temperature and salinity inverted form combined hydrographic and seismic data. Geophysical Research Letters, 37(4). DOI: 10.1029/2009GL042115
- Song, Y., Song, H. B., Chen, L. (2010). Seawater thermohaline structure inversion from seismic data. Chinese Journal of Geophysics, 53(11), 2696-2702. DOI: 10.1002/cjg2.1569
- Versteeg, R. J. (1993). Sensitivity of prestack depth migration to the velocity model. Geophysics, 58(6), 873-882. DOI: 10.1190/1.1443471
- Xu, S., & Pham, D. (2003). Global solution to water column statics: A new approach to an old problem. 73rd Ann. Internat. Mtg.: Soc. Expl. Geophys.
- Zhao, X. Y. (1985). The comprehensive research report of the South China Sea. Science Press, Beijing.
- Zhu, J., Lines, L., & Gray, S. (1998). Smiles and frowns in migration/ velocity analysis. Geophysics, 63(4), 1200-1209.