

Simulation of photoconductive antennas for terahertz radiation

Simulación de antenas fotoconductoras para radiación terahertz

C. A. Criollo¹ and A. Ávila²

ABSTRACT

Simulation of terahertz (THz) emission based on PC antennas imposes a challenge to couple the semiconductor carrier phenomena, optical transport and the THz energy transport. In this paper a Multi-physics simulation for coupling these phenomena using COMSOL Multi-physics 4.3b is introduced. The main parameters of THz photoconductive (PC) antenna as THz emitter have been reviewed and discussed. The results indicate the role of each parameter in the resulting photocurrent waveform and THz frequency: The radiated THz photocurrent waveform is determined by the photoconductive gap (the separation between the metallic electrodes), the incident laser illumination and the DC excitation voltage; while the THz frequency depends on the dipole length. The optimization of these parameters could enhance the emission. The simulations extend the advance of compact and cost-effective THz emitters.

Keywords: Multi-physics simulation, photoconductive antennas, semiconductor physics, electromagnetics.

RESUMEN

La emisión de Terahertz (THz) empleando antenas fotoconductoras representa un reto de simulación en la integración de los fenómenos de transporte en semiconductores, de óptica y de transporte de energía por radiación THz. En el presente artículo se propone una simulación Multi-Física para integrar estos fenómenos utilizando COMSOL Multiphysics 4.3b. Los principales parámetros de las antenas fotoconductoras empleadas como emisores de THz son estudiados. Los resultados de la simulación demuestran cómo estos parámetros inciden en la fotocorriente generada y en la frecuencia de radiación THz: la abertura fotoconductoras (la separación de los electrodos metálicos de la antena), la potencia promedio del láser incidente y el voltaje de polarización, determinan la forma de onda de la fotocorriente generada; mientras que la longitud del dipolo determina la frecuencia de radiación. La emisión de las antenas fotoconductoras puede mejorarse optimizando estos parámetros. Esta simulación es útil para el diseño e implementación de antenas fotoconductoras como emisores de THz de diseño compacto y bajo costo.

Palabras clave: Antena fotoconductoras, simulación multi-física, electromagnetismo, física de semiconductores.

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Introduction

Material responses to Terahertz radiation (THz) has opened up a large range of industrial applications (Tonouchi, 2007). The THz radiation is located between the infrared and the microwaves electromagnetic spectrum (Lee, 2009). In this range of frequencies the radiation can be described in the infrared by the particle like characteristics and wave-like characteristics in the microwave. THz applications explore the unique properties of THz radiation-matter interaction: Water is highly absorptive, metals are highly reflective and nonpolar and nonmetallic materials such as paper, plastics, wood and textiles are transparent at THz frequencies. These properties have boosted the potential industrial applications of a radiation that is nonionizing, nondestructive, and noninvasive: sensitive liquid spectroscopy (Mickan, Shvartsman, Munch, Zhang, & Abbott, 2004) ultrafast time domain spectroscopy (Tang et al., 2014), explosive detectors for remote sensing (Federici et al.,

2005) and bio-imaging with nanometer resolution (150nm)(Chen, Kersting, & Cho, 2003). With these applications panorama the interest in developing compact and cost-effective THz generation and detection techniques has arisen (Berry, Hashemi, & Jarrahi, 2014; Tani et al., 2013).

THz waves generation has been achieved by solid state and optical methods. The former is limited by the generation at cryogenic temperatures (Kumar, Chan, Hu, & Reno, 2011) while the latter has been attained at room temperatures (Khiabani, Huang, Shen, & Boyes, 2011). Optical generation can be further subdivided into optical rectification and photoconductive generation. While optical rectification is well suited to generate intense THz pulses with amplified laser systems, photoconductive emission is much more efficient when standard laser oscillator systems are used (Löffler et al., 2005). Effective THz generation has been reported with photoconductive (PC) antennas with a dipole structure (Venkatesh,

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Rao, Abhilash, Tewari, & Chaudhary, 2014), with the advantage that it can be patterned on the same semiconductor substrate used for THz detection. A PC antenna consists of two metal planar electrodes deposited on a semiconductor substrate. An optical beam illuminating the gap between the electrodes generates photo-carriers that are accelerated by static bias field to produce a time-varying current that radiates THz electromagnetic waves.

Simulation of THz generation based on PC antennas imposes a challenge to couple the semiconductor carrier phenomena, optical transport and the THz energy transport (Armstrong, 2012). Analytical equations can be applied to describe the most important properties of photoconductive antennas (Lloyd-Hughes, Castro-Camus, & Johnston, 2005), but often losses are neglected, this approach is simple to predict quantitative predictions. On the other hand, in-depth Monte-Carlo simulations describes in great detail the carrier dynamics in a photoconductive antenna (Castro-Camus, Lloyd-Hughes, & Johnston, 2005), however, without focus on effects related to antenna geometry. In the present work a multi-physics simulation for coupling these phenomena is introduced using COMSOL Multiphysics®. Results indicate that the radiated THz waveform is determined by the photoconductive gap (the separation between the metallic electrodes), the incident laser illumination and the DC excitation voltage. The emission intensity of the THz pulse depends on the dipole length. The simulation results are useful for designing THz antennas and tuning the excitation parameters for improved working of these devices.

Generation of THz radiation with PC antennas

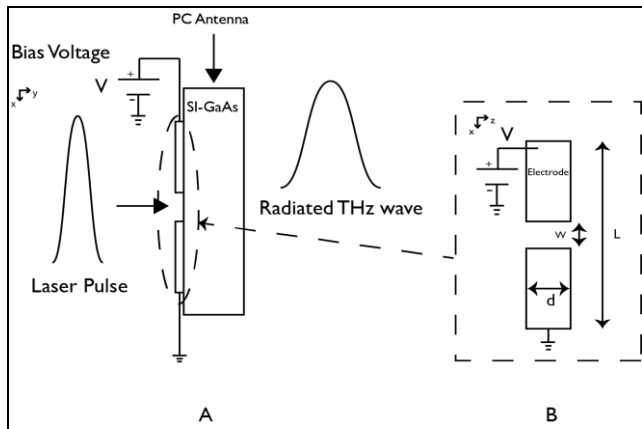


Figure 1. Schematic of the generation of THz radiation using a THz PC antenna A) Side view of a PC antenna under illumination of fs laser pulses with λ_{opt} varying from 800nm up 1500nm, and a bias voltage excitation V. B) Front view of the electrodes with PC gap w dipole length L and width d.

Figure 1 shows the schematic diagram of the PC antenna when it is employed as a THz emitter. This generation technique consists of a femtosecond (fs) laser and a micro-stripped antenna on a photoconductive material under a DC bias voltage (V). The antenna includes two planar metal electrodes deposited on a semiconductor substrate (i.e Si-GaAs) forming a dipole structure. After laser radiation on the PC gap, electron-hole pairs are accelerated in the biased semiconductor generating an ultra-short photo-current pulse ($J(t)$) that decreases with a time constant determined by the carrier lifetime in the substrate. Several photoconductive materials have been tested for photoconductive antennas, such as Si-GaAs and LT-GaAs. The advantage of Si-GaAs over LT-GaAs has been demonstrated in antennas in which the saturation effects due to field screening can be avoided (Liu, Tani, & Pan, 2003; Tani,

Matsuura, Sakai, & Nakashima, 1997). Typical lifetimes are several hundred picoseconds for Si-GaAs (Tani et al., 1997) and subpicoseconds for LT-GaAs (Gupta, Whitaker, & Mourou, 1992; Tani et al., 1994), respectively. The photo-current is directly dependent on the density of generated photo-carriers $N(t)$, the mobility of electrons μ and the static bias field between the electrodes E_b . It can be expressed by $J(t) = N(t)e\mu E_b$, where e is the electron charge (Khiabani et al., 2011). The transient current at the PC gap of the antenna radiates an electromagnetic pulse in the THz frequency.

Multi-physics simulation of PC Antenna

The “Electromagnetic Waves, Frequency Domain” interface of the “Wave optics Module” of COMSOL Multiphysics® 4.3b was used for the simulation of the PC antenna as a THz emitter. The complete structure is presented in Figure 2. It consists of three domains: air, gold microelectrodes and a 350 μ m Si-GaAs substrate with a resistivity of 3.5x10⁷ Ω -cm. These values are taken from commonly used materials in fabrication of PC antennas (Criollo, Avila, & Winnerl, 2014; Shi, Hou, & Wang, 2011).

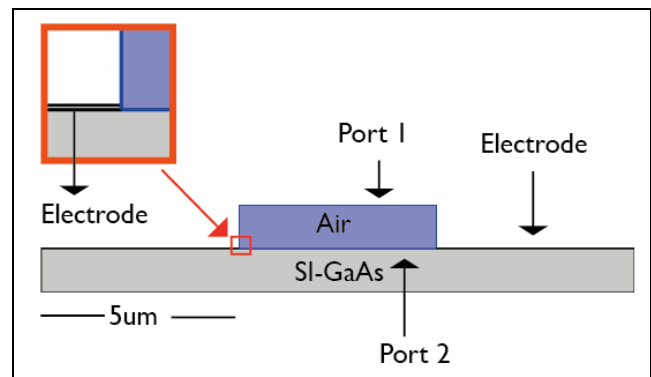


Figure 2. 2D Simulation CAD of PC antenna as a THz emitter. Port 1 input is employed for laser excitation. Port 2 input is used for the absorption of the transmitted wave in Si-GaAs substrate. Inset: metallic electrode.

Port node 1 input was used to launch the fs laser excitation with the propagation constant of the air (Hoffmann, Leuchtman, Rufenacht, & Hafner, 2009). The fs laser is modeled as a Gauss beam propagating along the z axis with an electric field distribution described by (Saleh & Teich, 1991):

$$E(r, z) = E_0 \frac{w_0}{w(z)} \exp\left(-\frac{r^2}{w^2(z)} - ikz - ik \frac{r^2}{2R(z)} + i\delta(z)\right) \quad (1)$$

$$w(z) = w_0 \sqrt{1 + \left(\frac{z}{Z_R}\right)^2} \quad (2)$$

$$Z_R = \frac{\pi w_0^2}{\lambda_{opt}} \quad (3)$$

Where $E_0 = |E(0,0)|$, r is the radial distance from the center axis of the beam, w(z) is the variation of the spot radius along the propagation axis, w₀ is the minimum value of the spot radius w(z) along the beam axis located at z = 0, called beam waist, Z_R is the Rayleigh range, R(z) is the radius of curvature of the beam’s wave fronts and $\delta(z)$ is the Gouy phase shift, an extra contribution in the phase that is seen in Gaussian beams (Feng* & Winful, 2001).

Port 2 input was used to absorb the transmitted Gaussian beam with the propagation constant of the Si-GaAs substrate (Chazan, Haelterman, & Tedjini, 1992), a wavelength of 800nm, a laser repetition rate of 80MHz, an average output power of 80mW, a pulse

width of 15fs and a spot radius of 5 μ m. The above-mentioned excitation parameters are commonly used in previously published works (Khiabani et al., 2011). Floquet periodic boundary conditions were implemented to limit the simulation to a single periodic element (Zhengqing Yun, 2000). The electric field $E(r, z)$ was employed as an input parameter to the ports and to the Floquet periodic boundary conditions. Free tetrahedral mesh was applied to all the domains with a “fine” resolution of 10nm. This mesh was set smaller than the incident wavelength to resolve the impact of the incident optical power on the PC gap. For the photo-carrier generation simulation in the Si-GaAs substrate under laser excitation, the quasi-analytical model of Duvillaret for PC antennas was employed (Duvillaret, Garet, Roux, & Coutaz, 2001). The calculations in this model are based on the Drude-Lorentz theory to simulate the dynamics of photo-generated free carriers inside the photoconductor and entail a direct proportionality between the time derivative emitter photocurrent $\frac{\partial J(t)}{\partial t}$ and the emitted THz field E_{THZ} .

The dependence of the THz emission spectra on the dipole length was investigated. Figure 3 shows the calculated THz emission spectra for PC antennas with dipole length from 20 μ m to 150 μ m. The peak field amplitude of the THz transients emitted significantly increases as the dipole length increases. The emitted electric field E_{THZ} which is proportional to the time derivation of the current $J(t)$ at the gap is calculated using the finite-difference time domain method. It can be seen in Figure 3 that the peak frequency of the THz transients shifts to lower frequency if the dipole length increases. This can be explained by the relationship between the geometrical parameters of the dipole antenna and the spectral shape of the input electric field that determines the characteristics of the THz emitted wave. Having into account that the input electric field (femtosecond laser) changes relatively slowly, the maximum emission intensity can be obtained using a longer dipole length which has a resonance at a lower frequency.

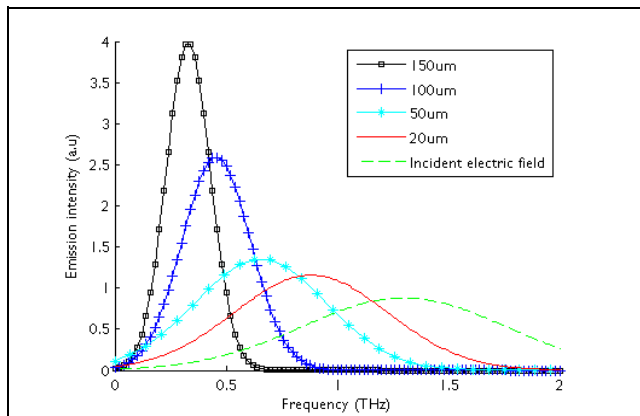
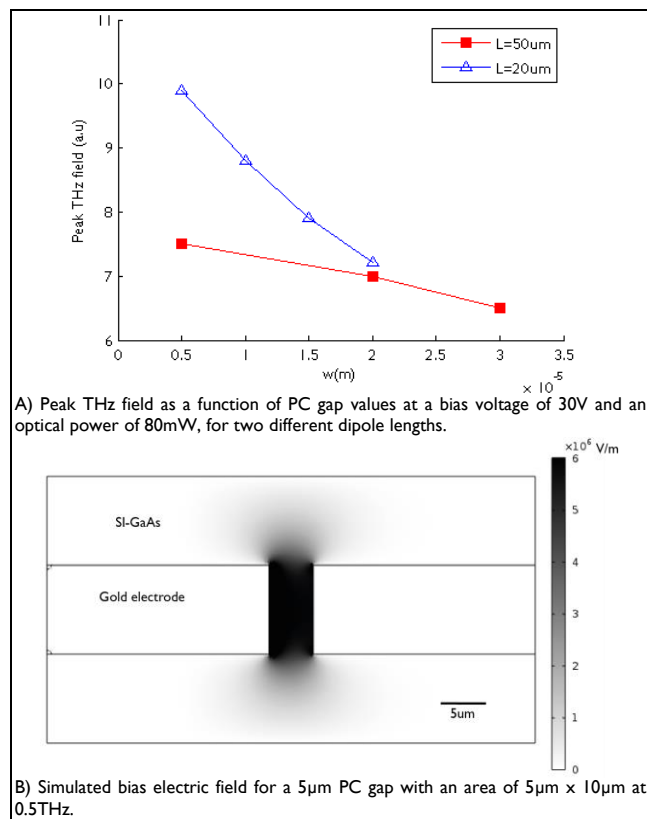


Figure 3. Calculated emission spectra for photoconductive antennas (in arbitrary units) with dipole lengths ranging from THz pulses emitted from PC antennas varying dipole lengths from 20 μ m up to 150 μ m.

To study the effects of dipole length and gap distance on the peak THz field, PC antennas with gaps varying 5 μ m up to 30 μ m was simulated. The results of this analysis are presented in Figure 4a. The radiated peak THz field from a PC antenna with a smaller gap increases because of the better overlapping of the laser spot and the region of the high electric field in the PC gap. Moreover, the increment of the electric bias field due to a reduction of the PC gap accelerates a larger concentration of photo-carriers, for example: for a PC gap of 5 μ m, the field goes up to 6MV/m, see Figure 4b. The slope of this dependence changes with the dipole length.



A) Peak THz field as a function of PC gap values at a bias voltage of 30V and an optical power of 80mW, for two different dipole lengths.

B) Simulated bias electric field for a 5 μ m PC gap with an area of 5 μ m \times 10 μ m at 0.5THz.

Figure 4. Simulation of the average output power of the PC antenna for different gap lengths and the surface electric field at the PC gap.

The voltage bias dependence of the generated photocurrent in the PC antenna with 5 μ m gap length is presented in Figure 5. For higher bias fields, the photo-current pulse shape displays an increase due to the increment in the concentration of accelerated photo-carriers. A current difference of 10.2 μ A is estimated between the photocurrent peaks of 10V and 30V bias. In these experimental observations, the timescale of the photocurrent peak is associated to the carrier acceleration in the external bias field followed by the transfer from the high mobility r-valley to the low mobility L-valley and hence a stronger deceleration which results in a photocurrent overshoot. The intervalley scattering effect is expected to be more significant in materials with hundred of picosecond carrier life times since the photo carriers would be enough time to be scattered into the L-valley (Liu et al., 2003; Ludwig & Kuhl, 1996).

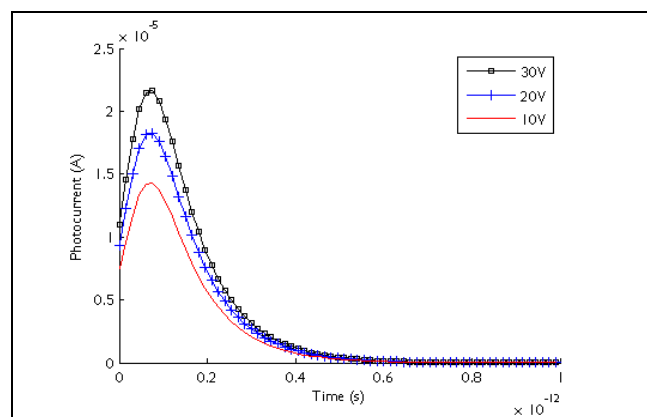


Figure 5. THz Temporal photocurrent for PC antenna with a PC gap of 5 μ m at three different biases: 10V, 20V and 30V. In the simulation the average laser power was kept constant in 80mW.

Another important parameter in the design of PC antennas is the influence of the average laser power on the waveform and the peak current of the generated photo-current, see Figure 6. The laser power was varied from 10mW to 80mW, these values are the reference power from lasers Commercially Available (Spence & Sibbett, 1991).

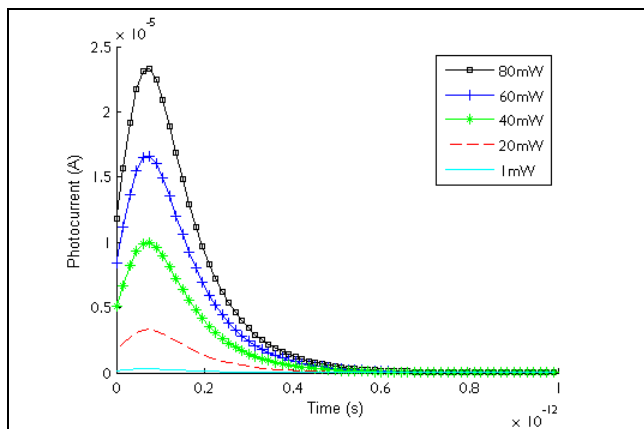


Figure 6. THz temporal photocurrent for a PC antenna with a PC gap of 5µm at different laser power levels and a constant applied bias of 30V.

From Figure 6 it can be noted that there is an amplitude increment in the THz pulse shape at higher excitation densities due to an increment in the density of photo-carriers at the PC gap. The saturation behavior reported in experimental works (Loata, Thomson, Löffler, & Roskos, 2007; Tani et al., 1997), that is presented at high fluences of photo-generated carriers in photoconductive antennas is not evident in the Figure 6 because screening effects are not included in the simulation, therefore the results are valid only for low laser power levels. The smallest optical power level at which the PC antenna generates a pulse of photocurrent is below 20mW, where the peak current of the pulse shape is reduced at 0.09µA.

The radiation patterns of the simulated PC Antenna with a phase of 45° for different frequencies (ranging from 0.3THz to 1 THz) are illustrated in Figure 7. The main pattern direction of the antenna is towards “y” axe with the maximum directivity of 3.89 dBi. At 0.5THz the radiation pattern is dipolar, and above it, it starts to have side lobes as the frequency increases.

Conclusions

In this paper, a Multi-physics simulation for coupling all the phenomena involved in the generation of THz radiation with PC antennas is implemented using COMSOL Multiphysics 4.3b. Through this simulation, interesting characteristics of the antenna design and excitation parameters were obtained. Results indicate the role of each parameter in the resulting photocurrent waveform and THz frequency: the radiated THz photocurrent waveform is determined by the photoconductive gap (the separation between the metallic electrodes), the incident laser illumination and the DC excitation voltage; while the THz frequency depends on the length of the dipole. Thus this simulation should serve as a useful tool in designing PC antennas and tuning the excitation parameters for improving the operation of these devices.

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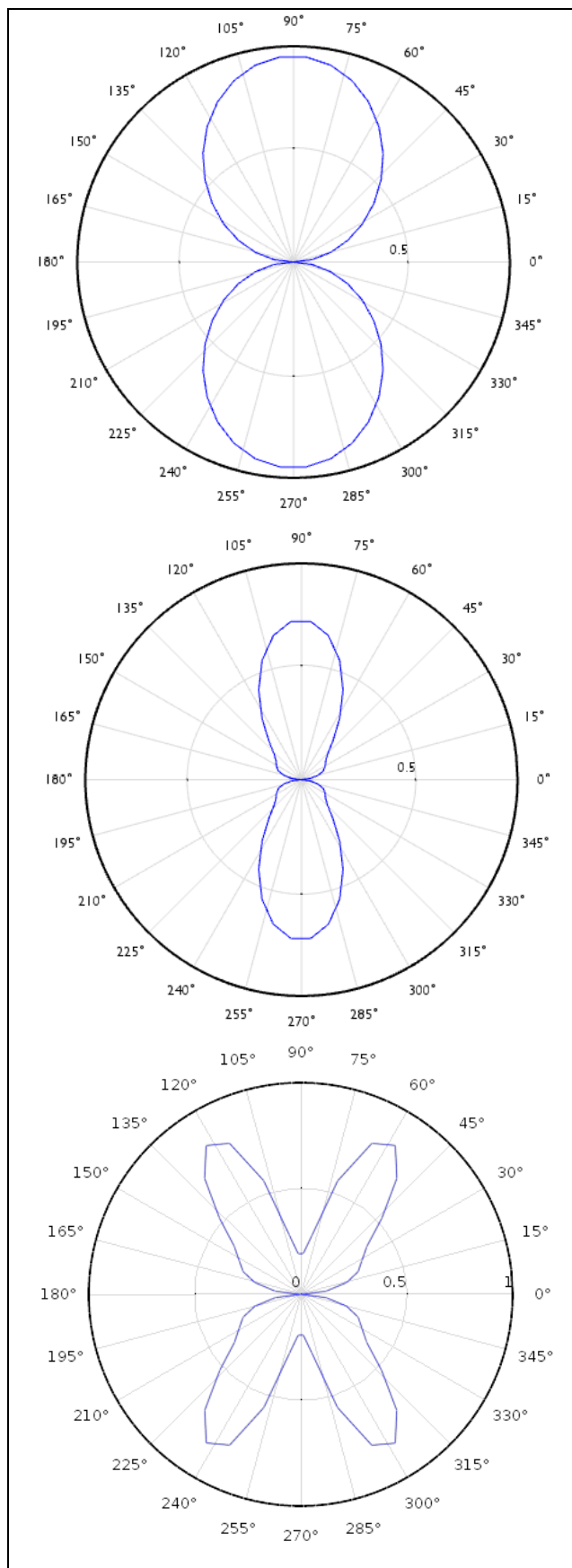


Figure 7. Radiation patterns of a single PC antenna at different frequencies in (xoy) plane.

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