INGENIERÍA BIOMÉDICA

Análisis cinemático de un miembro inferior para determinar el centro de rotación en el plano sagital

BIOMEDICAL ENGINEERING

Kinematic analysis of a lower limb to determine the center of rotation of the knee at the sagittal plane

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Resumen

En esta investigación se establece una metodología que permite describir el movimiento de miembros inferiores usando cadenas cinemáticas cerradas. Este análisis es realizado con el objetivo de determinar la posición del centro de rotación (CR) de la rodilla localizado en el plano sagital. Un paciente sano y sin antecedentes patológicos realizó pruebas de flexión-extensión con uno de sus miembros inferiores. Cuando el paciente realizo el movimiento articular (la flexo-extensión) un dispositivo de video y un programa (World In motion v4.0) determinan la posición de cuatro marcadores pasivos ubicados en el miembro inferior. Los datos obtenidos de los marcadores son utilizados en un modelo propuesto que permite localizar la posición del CR de la rodilla. En este estudio se concluye que el CR de la rodilla presenta movimiento relativo respecto a un punto fijo marcado en un miembro inferior. Los resultados comprueban que el CR de la rodilla delimitado en el plano sagital no presenta comportamiento de una junta completa (junta con un grado de libertad) como ha sido presentado en otros estudios.

Palabras clave: análisis cinemático, centro de rotación (CR), flexión-extensión.

Abstract

A methodology is established in this research which permits to describe the movement of a lower limb using closed kinematic chains. This analysis is developed with the aim to determine the location of the center of rotation (CR) of the knee joint in the sagittal plane. Flexion-extension tests were carried out on one of the lower limbs of a healthy patient without pathological antecedents. When the patient does articular movement (flexion-extension), a video equipment and a software determine the position of four passive markers installed on the lower limb. The information obtained from the markers is applied to the proposed model which allows to locate the center of rotation of the knee joint. Hence it was concluded that the CR of the knee joint undergoes a relative movement with respect to the fixed point marked on the lower limb. The results prove that the knee joint established in the sagittal plane does not show the behavior of a complete joint (a joint with one degree of freedom) as it has been described in other studies.

Keywords: center of rotation, flexion-extension, kinematic analysis, knee.

1. Introduction

As it was described by Vera (1999), normal human locomotion is a set of rhythmic and alternating movements of the extremities, which determines the forward movement of the body's center of mass. In the field of human locomotion, there are described different types of articular movement performed by the joints in the extremities. The knee joint is the widest articulation and maybe the most complex one in the body (Proubasta et al., 1997). This joint is a biarticular structure composed of the tibiofemoral and femoropatellar articulation. The knee joint can support high forces and moments since this articulation consists of femur and tibia, which are located between the two longest lever arms in the body. A detailed description of the knee joint physiology can be found in Bronzino et al. (2003). A balance between stability and mobility is needed that knee joint works normally and this depends on the interaction of the ligaments and interaction of contact surfaces and muscles that enclose the knee joint (Koo et al., 2008). The movement of a knee joint occurs simultaneously in three planes, but the whole movement of the joint can be observed only at the sagittal plane. The movement of the joint at the sagittal plane may be limited if the articulation is restricted to a movement in a two-dimensional plane (see Nordin et al., 2004; Zuppinger, 2004). A two-dimensional approximation of the movement of the knee joint may be established from the kinematic relations similar to those of a planar mechanism (see Abdel-Rahman et al., 1993). However, significant progress has been made analyzing the kinematics of the knee joint in all the planes, as it is described by Freeman et al. (2005). Nevertheless, different analyses have been made to explain the movement of the knee joint (Gerber et al., 1983; Moeinzadeh et al., 1983; Haher et al., 1992; Hemmerich et al., 2008) with the aim to describe its kinematics in all the planes (van den Bogert et al., 2008; Anderst et al., 2010.).

The movement in the knee joint is produced by resultant forces generated by various muscle groups located in each kinematic plane. These

forces may be represented by a unique resultant force which includes most of the muscle forces that act in the knee joint. In the tibiofemoral joint, the forces generate a máximum spatial movement in which the rotatory amplitudes are admisibles. As a result, kinematic approximations of the tibiofemoral joint may be delimited in the sagittal plane. Williams et al. (1991) proposed a mathematical model of the knee joint movement in the sagittal plane. The cruciate ligaments were considered as a four bar linkage. This model establishes an equation system for obtaining 11 kinematic parameters. The results depicted the slippage and rotation effects which form the complex movement of the surfaces articulated in the lateral condyle.

In the sagittal plane, there is observed that the movement of the knee joint from extension to the complete flexion produces a rotation between 0° and 140°, approximately. In the transversal plane, the movement is influenced by the position of the joint in the sagittal plane. When the knee joint is completely extended, the rotation is almost fully restricted by the impact of femoral and tibial condyles, this happens because the medial femoral condyle is longer than the lateral condyle. The muscles and ligaments also show restrictions to the knee joint movement, this phenomenon was studied by Moeinzadeh (1983). A dynamic model of tibiofemoral joint which incorporates the restrictions of ligaments in femur and tibia was described by Wongchaisuwat (1984). Goodfellow (1978) showed some methods for analyzing the mechanics of the knee joint, among others, for example: uniplanar or sagittal methods, triplanar method and instant center of rotation (ICR) method or the Reuleaux (1875) technique. Recent studies on articular determination were also carried out by Favre et al. (2008, 2009).

A Reuleaux (1875) technique is used in this research to relate the knee joint by means of kinetic chains with fixed points established on the lower limb. Inertial effects of the lower limb are not considered in this studysince this research is based on the kinematics of the lower extremity. This means that the lower limb is analogous to two rigid and articulated bodies (a thigh and a shank with movement of the joint in the sagittal plane). The main objective of this study is to estimate the position of the center of rotation of the knee joint by experimental measurements and to show that it is not a complete joint at the sagittal plane. The suggested model may be classified within the sagittal methods.

2. Methodology

2.1 Kinematic analysis

To describe the movement of the lower limb and to carry out a kinematic analysis of it, a theoretical model should be proposed. Let's consider that the kinematic information of four points that belongs to the lower limb are known. So, Figure 1 shows a lower limb marked with four fixed points (A, B, C, D) and a point that belongs to the knee joint (JC). The points A, B, C and D are referred with regard to a fixed coordinate system O. The union between these points is represented by vectors in the following form: relative position vector $r_{B/A}$ (points A and B), relative position vector $r_{C/D}$ (points C and D), relative position vector $r_{JC/B}$ (points B and JC), relative position vector $r_{JC/C}$ (points C and JC), relative position vector $r_{B/C}$ (points B and C), r_A (position of point A with regard to the fixed frame of reference O), r_B (position of point B with regard to the fixed frame of reference O), r_C (position of point C with regard to the fixed frame of reference O), r_D (position of point D with regard to the fixed frame of reference O), l_{AB} (magnitude of the vector $r_{B/A}$ and l_{CD} (magnitude of the vector $r_{C/D}$).

The thigh and shank are considered rigid bodies which move in the sagittal plane coincident with the plane *x-y*. Therefore, the connection of vectors established in the limb is also defined in the sagittal plane. For the vectors shown in Figure 1, the relative velocity $\dot{r}_{B/A}$ of the thigh in any point in time t, $\forall t \in \mathbb{R}$, may be defined as:

$$\dot{r}_{B/A} = \dot{\theta}_{B/A} \times r_{B/A} \tag{1}$$



Figure 1. Kinetic chain established in the lower limb

where θ_{BA} is the angular velocity of the vector r_{BA} . Eq. (1) may be rewritten as:

$$\cdot \dot{r}_{\scriptscriptstyle B} - \dot{r}_{\scriptscriptstyle A} = \dot{\theta}_{\scriptscriptstyle BA} \times (r_{\scriptscriptstyle B} - r_{\scriptscriptstyle A}) \tag{2}$$

where \dot{r}_{B} is absolute velocity of the point B, \dot{r}_{A} is absolute velocity of the point A. In the same way as Eq. (1) is defined, also the relative velocity $\dot{r}_{C/D}$ corresponding to the velocity of the shank can be expressed. For any point in time *t*, the velocity $\dot{r}_{C/D}$ is given by:

$$\dot{r}_{C/D} = \dot{\theta}_{CD} \times r_{C/D} \qquad (3)$$

where θ_{CD} is angular velocity of the shank. In the same way as Eq. (1), also Eq. (3) may be determined as:

$$\dot{r}_{\scriptscriptstyle C} - \dot{r}_{\scriptscriptstyle D} = \dot{\theta}_{\scriptscriptstyle CD} \times (r_{\scriptscriptstyle C} - r_{\scriptscriptstyle D}),$$
 (4)

where \dot{r}_{c} is absolute velocity of the point C, \dot{r}_{D} is absolute velocity of the point D.

Angular velocity of the knee joint θ_J is defined as relative angular velocity between the angular velocity of the thigh θ_{BA} and the angular velocity of the shank θ_{CD} , such that:

$$\dot{\theta}_{J} = \dot{\theta}_{CD} - \dot{\theta}_{BA} \tag{5}$$

In this case, the flexion may be considered positive and the extension negative. The velocity of the joint (JC) \dot{r}_{JC} is determined by means of the relative velocity between the points JC and B that correspond to the thigh, then the velocity of the joint (JC) is obtained as:

$$\dot{r}_{JC} = \dot{r}_{B} + \theta_{BA} \times r_{JC/B}$$
(6)

Similarly, the velocity of the joint (JC) \dot{r}_{JC} is determined by means of the relative velocity between the points JC and C that correspond to the shank, then the velocity of the joint (JC) is obtained as:

$$\dot{r}_{JC} = \dot{r}_{C} + \dot{\theta}_{CD} \times r_{JC/C}$$
(7)

By equating Eq. (6) with Eq. (7), it is obtained that:

$$\dot{r}_{C} + \dot{\theta}_{CD} \times r_{JC/C} = \dot{r}_{B} + \dot{\theta}_{BA} \times r_{JC/B} \qquad (8)$$

The points B, C and JC are related among each other in the following way:

$$r_{JC/C} = r_{B/C} + r_{JC/B} \tag{9}$$

by replacing Eq. (9) into Eq. (8) and organizing Eq. (8), it is obtained that:

$$(\dot{\theta}_{CD} - \dot{\theta}_{BA}) \times r_{JC/B} = \dot{r}_{B} - \dot{r}_{C} - \dot{\theta}_{CD} \times r_{B/C}$$
 (10)

It can be observed that all the vectors on the right side of Eq. (10) are known, therefore the angular velocity of the center of the joint θ_J is determined by substituting Eq. (5) into Eq. (10) and into the relative velocity ($\dot{r}_{B/C} = \dot{r}_B - \dot{r}_C$) between the points B and C, such that:

$$\dot{\theta}_J \times r_{JC/B} = \dot{r}_{B/C} - \dot{\theta}_{DC} \times r_{B/C}$$
(11)

Multiplying Eq. (11) by the vector θ_j , it is obtained that:

$$\dot{\theta}_{J} \times (\dot{\theta}_{J} \times r_{JC/B}) = \dot{\theta}_{J} \times \dot{r}_{B/C} - \dot{\theta}_{J} \times (\dot{\theta}_{DC} \times r_{B/C})$$
(12)

Applying the properties of the vector triple product of Eq. (12), this equation may be rewritten in the following form:

$$\hat{\theta}_{J}(\dot{\theta}_{J}\cdot r_{JC/B}) - r_{JC/B}(\dot{\theta}_{J}\cdot \dot{\theta}_{J}) = (\dot{\theta}_{J}\times \dot{r}_{B/C}) - \dot{\theta}_{J}(\dot{\theta}_{J}\cdot r_{B/C}) + r_{B/C}(\dot{\theta}_{J}\cdot \dot{\theta}_{DC})$$
(13)

The angular velocity θ _J is perpendicular to the vectors that are located in the sagittal plane, consequently $\dot{\theta}_J (\dot{\theta}_J \cdot r_{JC/B}) = \dot{\theta}_J (\dot{\theta}_J \cdot r_{B/C}) = 0$. Relative position $r_{JC/B}$ of the center of the joint seen from B to JC may be determined from Eq. (13) as:

$$r_{JC/B} = -\frac{\dot{\theta}_J \times \dot{r}_{B/C} + r_{B/C} (\dot{\theta}_J \cdot \dot{\theta}_{DC})}{\dot{\theta}_J \cdot \dot{\theta}_J} \qquad (14)$$

Eq. (14) represents the vector or the position of the center of the joint with regard to the point B located on the thigh.

2.2 Polynomial approximation

A set of N+1 data represented in Cartesian coordinate system may be adjusted or approximated by means of a polynomial of grade N. Then, for the obtained N+1 data $\{(x_0, y_0), (x_1, y_1) \dots, (x_N, y_N)\}$, a polynomial of grade N with N+1 coefficients is defined such that:

$$p_N(x) = a_0 + a_1 x^{iii} + a_2 x^2 + ... + a_N x^N$$
 (15)

Each ordered pair (x_N, y_N) is replaced in Eq. (15) and a system of linear equations is established with the aim to determine the coefficients of this polynomial. Yang . (2005) described this procedure which is applied in this study in the following form:

$$a_{0} + \alpha_{1}x_{0}^{\text{III}} + a_{2}x_{0}^{2} + \dots + a_{N}x_{0}^{N} = y_{0}$$

$$a_{0} + \alpha_{1}x_{1}^{\text{III}} + a_{2}x_{1}^{2} + \dots + a_{N}x_{1}^{N} = y_{1}$$

$$\dots \qquad \dots \qquad \dots$$

$$a_{N} + \alpha_{1}x_{N}^{\text{IIII}} + a_{2}x_{N}^{2} + \dots + a_{N}x_{N}^{N} = y_{N}$$
(16)

For determining the coefficients $\{a_0, a_1, a_2, a_3, \dots, a_N\}$ from Eq. (16), it is established that:

$$\mathbf{X}\mathbf{c} = \mathbf{Y} \tag{17}$$

Solving for \mathbf{c} from Eq. (17), the following is obtained:

$$\mathbf{c} = \mathbf{X}^{-1}\mathbf{Y} \tag{18}$$

where X is the matrix of all the ordered pairs x, **c** is the coefficients vector and Y is the vector of ordered pairs y. The coefficients **c** are determined for positions obtained from each marker. For the determined polynomials, the derivative may be obtained numerically by means of an inclination established between two points in time t_i and t_{i+1} that pertain to each function of position $X_n(t)$, $\forall n$ = 1,2,3 y 4. The derivative approximated from X_n (t), when $\Delta t \rightarrow 0$, is defined by:

$$\frac{dX_n(t)}{dt} = \frac{X_n(t_{i+1}) - X_n(t_i)}{t_{-i+1} - t_i}$$
(19)

The lineal velocity of the points marked on the lower limb (points A, B, C and D) may be obtained from Eq. (19). The derivative proposed in Eq. (19) is a numerical approximation that works well if the data not present perturbations of high frequency, this is not the case of this study. But when the first derivative is applied to the set of data (x_N, y_N), this is reduced to N - 1 data and the reduction will not affect the analysis because these are obtained in low frequency.

2.3 Experimental method

Figure 2 shows the methodology established for obtaining the position of four passive markers attached to the lower limb of a male patient of the age of 23 years, healthy and without any motional pathological antecedents which might affect the testing. The procedure for detection of the movement of lower limb was established in the following form: in the right lower limb, markers 1 and 2 were placed on the right shank and markers 3 and 4 on the right thigh (Figure 3) with a fixed relative position and a distance between markers 1 and 2 corresponding to $d_{12} = 193 mm$ and a distance between markers 3 and 4 corresponding to $d_{34} = 118 \text{ mm}$. The position of the markers is caught by a digital video device (Casio Exilim EX-FH20 camcorder) which provides the information on the movement in a commercial video format, this information is read by World In Motion v4 (2007) software. The software World In Motion v4 (2007) allows for determining, in a discrete form, the position of the passive markers when low frequency movements are carried out, and at the same time, it corrects the camera's perspective of projection adjusting a projection plane to the plane of position measures.

For evaluation of the characteristic movements of the four markers (see Figure 3), the patient was positioned in such a way that the flexion-extension exercise was done without kinematic restrictions in sagittal plane however a guideline was put in place to ensure a standard initial stance for the exercise. This was done with the aim to avoid indiscriminate movements in lateral and transversal plane as the



Figure 2. a) Process of obtaining the position of the markers on the lower limb. b) Markers for evaluation of the flexion-extension.

movement of sagittal plane should be projected into the plane of the camera during the flexionextension. The above mentioned exercise was carried out taking into account the considerations and parameters done by Kankaanpa *et al.* (1998), Roy *et al.* (2003) and Bronzino *et al.* (2003). Since, the flexion-extension is not a simple movement of the joint around a transversal axis neither it is a simple movement done in one single plane. When the patient performed the exercise for kinematic evaluation, the video capturing was programmed at 3.3330s as the sequence of the patient's movement was done in a shorter time interval.

Data on the position of the markers estimated from World In Motion v4 (2007) were exported



Figure 3. a) Displacement in x for the markers $1 (\nabla)$, $2(\triangle)$, $3(\blacksquare)$ and $4(\bullet)$. *b)* Displacement in y for the markers $1 (\nabla)$, $2(\triangle)$, $3(\blacksquare)$ and $4(\bullet)$.

to MatLAB for kinematic analysis. Numerical derivation functions were applied to estimate, by means of interpolation, the velocities of the markers located on the analyzed lower limb (see section 2.2). Eq. (14) including all the estimated kinematic information is shown in section 2.1 and it is used to determine relative position of the rotary knee joint in the sagittal plane.

3. Results and discussion.

Figure 6a shows the position coordinates obtained from markers 1, 2, 3 and 4 as rigid links; these coordinates are simulated and coupled with in the following way: marker 1 and 2 (link 1) and marker 3 and 4 (link 2). The simulation is carried out for different time increments ($\Delta t = 0.067$ s) during all the patient's exercise which consisted in the simultaneous movement of the shank and thigh until the complete extension of the right lower limb. In Figure 6a, it can be observed that the link 1 presents a wider movement than the link 2. It is caused because of the fact that link 1 represents the shank which is flexed towards the thigh and therefore it presents higher mobility. The movement of the link 2 consists of the translation and slight rotation since this link (thigh) is restricted by the support (chair) used during the performance of this exercise. No noise or perturbations were observed in the results of this simulation due to the relatively low velocity of the exercise (flexion - extension) which contributes to the fact that the obtained measurements are of low frequency.

The coordinates of the markers' displacement are approximated by a polynomial of grade N - 1 for a set of N determined data (see Eq. (16), Eq. (17) and Eq. (18)). Table 1 shows the coefficients of correlation for every approximation done for each coordinate x and y corresponding to the markers 1, 2, 3 and 4. An interpolation process was implemented because the time intervals between two consequent images were 0.067s. Within this time interval, the information about the position of the center of rotation of the knee joint might be lost, however the implemented process of interpolation allowed to obtain more reliable

| 50 | · |
|-------------|-------------------------------|
| Variable | Correlation (R ²) |
| Position x1 | 0,9888 |
| Position x2 | 0,9963 |
| Position x3 | 0,9865 |
| Position x4 | 0,9656 |
| Position y1 | 0,9806 |
| Position y2 | 0,9834 |
| Position y3 | 0,9952 |
| Position y4 | 0,9958 |

Table 1. Coefficients of correlation

results. The results listed in Table 1 show that the obtained coefficients of correlation indicate high reliability with the obtained approximations since the values of R^2 are very close to 1.

3.1 Results for position

The displacement of the four markers in directions x and y with regard to a fixed coordinate system O may be observed in Figures 3a and 3b. This coordinate system was established by an experimental measurement. First, a scene where the patient did the exercise was delimited with the aim to establish the reference axes x and y. Then the reference limits were calibrated by the camera obtaining in this way a mobility plane of the patient.

Figure 3a shows the displacement of each marker in x (1, 2, 3 and 4). In this figure, it can be observed that the markers located on the thigh (3 and 4) did not evince big displacements. On the other hand, the markers 1 and 2 located on the shank showed greater displacements than markers 3 and 4, especially the marker 1 recorded bigger movement in this direction. It is consistent that the marker 1 evince greater displacement as the lower point on the shank is the one which does biggest movement. Figure 3b shows the displacements of the markers 1, 2, 3 and 4 in y. The markers 3 and 4 did not evince big mobility in the axis y because the patient did the exercise while sitting and the thigh was restricted by the platform of the stance. However, the markers located on the shank (1 and 2) recorded great mobility, especially the marker 1.



Figure 4. a) Velocity x as a function of time for the markers 1 (∇), 2(\triangle), 3(\blacksquare) *and 4*(\bullet). *b) Velocity y as a function of time for the markers 1* (∇), 2(\triangle), 3(\blacksquare) *and 4*(\bullet).

3.2 Results for velocity

Figures 4a and 4b show numerically calculated velocities of each marker in directions x and y. The velocity of the markers is obtained by the numerical derivative of the polynomials determined from the position. The numerical derivative was solved by means of Eq. (19) and applying an incremental algorithm written in MatLAB. It is important to mention that the process of differentiation was carried out on the polynomials determined from the position of each marker and therefore the noise generated during the differentiation process was controlled by means of the intervals evaluated by the polynomials.

Figure 4a shows the velocity component in x for each marker. All the markers experienced velocities with different amplitudes, this effect takes place because the patient not only turned the lower part of the shank, but at the same time, he also moved the thigh to perform the rotation of the lower part. The marker 1 underwent higher velocity amplitude in x due to its location on the lower part of the shank.

Figure 4b shows the velocity component in y for each marker. The markers 3 and 4 in fact evince zero velocity because the thigh is restricted in its movement by the supporting platform on which the patient was sitting. The markers 1 and 2 recorded higher velocity magnitudes caused by the movement of the lower shank at the moment of performing the flexion.

3.3 Determination of the knee joint position

The results obtained in figures 3 and 4 are used in eq. (14). this equation represents the magnitude of the vector $R_{JC/B}$ established from the point b to the point jc (the distance from the point b to the center of rotation of the knee joint). the obtained data are shown in figure 5. in this figure, there can be observed the change in magnitude of the vector $r_{JC/B}$ determined on the basis of an experimental data and included in the proposed model (see eq. (14)).



Figure 5. Magnitude of the $r_{JC/B}$ as a function of time



Figure 6. a) Simulation of the flexion-extension in MatLAB for the shank (A) and the thigh (B). b) Position of the center of rotation (CR) with regard to the shank (A) and the thigh (B).

The magnitude of the center of rotation of the knee joint increases in the interval $t \in 0.6, 0.8$ s and becomes to decrease in $t \in 0.8, 2$ s. it can be observed that the magnitude of the vector $r_{\rm IC/B}$ shows a maximum change of 12 mm with respect to the marker b. the values of the magnitude of $r_{\rm IC/B}$ change in every point in time, therefore the magnitude to the center of rotation is not constant with regard to the point b. this result shows that the knee joint does not act as a simple rotary joint (a joint with one degree of freedom) as it was mentioned by koo et al. (2008); hemmerich et al. (2008) and favre et al. (2008), because the joint located in the knee evinces more complex movements which are a combination of translation and rotation when the articulation is moving.

The data shown in Figure 5 may be affected by the experimental measurement, however the results obtained by the proposed model do not show big deviations with regard to the reference point established on the thigh ($r_{JC/B}$, see Figure 1). The influence of small errors on the results is detected in the measurement plane of (sagittal plane) shown in Figure 6b. The errors produced in the measurement are caused because the patient possibly did small movements perpendicular to the sagittal plane when he was performing the flexion-extension exercise. The position of the center of rotation through the x - y space may be observed in Figure 6b. In this figure, the CR is being moved 15 cm approximately in y because the patient starts to turn the entire lower limb and makes the center of rotation moves linearly in y. On the other hand, the coordinate x has only been moved 12 cm, approximately.

The displacements of 15 and 12 cm can be observed when the patient carries out the flexion-extension exercise with his lower limb. The changes in the position of the CR indicate a composed movement. It can also be observed in Figure 6b that the obtained points do not generate a defined contour since some errors as small movements were produced in other planes.

4. Conclusions

It is possible to determine the kinematics and the position of the rotary knee joint from the results obtained for the position and velocity of the markers located on the lower limb. In the measurement plane parallel to the system of measurement (sagittal plane), the results showed that the rotary knee joint evinces mobility between a fixed marker located on the thigh and the rotary joint estimated from the magnitude $r_{JC/B}$, which is not constant. The results determined in this study indicate that the rotary knee joint is not a simple joint (a joint with one degree of freedom) since the articulation undergoes sliding and rolling movements.

The position of the obtained CR is coherent with the kinematics of the lower limb as it is found in a feasible region and not in regions out of the projections for the shank and the thigh. It is important to point out that this study does not analyze the position reliability in a quantitative form since there is no parameter for comparison. The strategy of establishing a relation between a lower limb of a disabled patient by means of a kinetic chain may be an option for analyzing the kinematics of a healthy lower limb. This is proposed with the aim to simulate a behavior of the articulations in amputated limbs.

For a plane study, the experimental measurement system adds errors to the results given that the information on the movement in the plane perpendicular to the sagittal plane is not caught by the video camera. This study may be extended to a two-plane system with the aim to determine the movement of the joint in three dimensions. It also may be adapted to the studies on the walk analysis as a supporting tool for identification of natural displacement gestures with such objectives as to identify movement pathologies or to improve the design of a knee immobilizer and an artificial limb.

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