

# Controlling a planar temperature grid

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## Resumen

*Este artículo presenta el diseño de controladores multivariables, uno distribuido y otro centralizado, para una rejilla plana de temperatura. El objetivo es mantener una superficie de temperatura constante en la rejilla. Aquí, presentamos el modelado del sistema a partir de pruebas escalón. También, presentamos el modelado del sistema con incertidumbres paramétricas en las constantes de tiempo. Para analizar el modelo del sistema, utilizamos la descomposición de valores singulares y el arreglo de ganancias relativas. Dos estrategias de control son aplicadas a el sistema, un controlador  $H^\infty$  y un controlador multivariable PID. La rejilla de temperatura plana es útil para mostrar un sistema mal condicionado, el cual necesita análisis complejo.*

**Palabras claves:** Modelo de incertidumbres, control robusto, sistema mal condicionado, controladores multivariables.

## Abstract

This paper presents the design of multivariable controllers, one distributed and another centralized, for a planar temperature grid. The objective is to keep a constant temperature surface on the grid. Herein, we present the modeling of the system by using step tests. Also, we present the modeling of the system with parametric uncertainties in time constants. To analyze the system model, we use the singular values decomposition and the relative gain array. Two control strategies are applied to the system, an  $H^\infty$

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controller and a multivariable PID. The planar temperature grid is useful for showing an ill-conditioned system, which needs complex analysis.

**Key words:** Uncertainty model, robust control, ill-conditioned system, multivariable controllers.

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## INTRODUCTION

A planar temperature grid is an example of an ill-conditioned multivariable system useful for analyzing and designing multivariable controllers. This system is affected by disturbances like: environment temperature and wind currents, inter-zone effects, and self-induced wind currents [1].

The planar temperature grid had been used as a study case in resource allocation. Many works have applied bio-inspired solutions to achieve uniform temperature on the grid. In [2] a Honey Bee social foraging algorithm is used. An algorithm based on the Bacteria Swarm foraging is presented in [3]. An Ant Colony system is also used, for example the work presented in [4] [5]. Two papers show how allocation strategy can achieve an Ideal Free Distribution (IFD) to achieve the maximum uniform temperature on grid under multivariable saturation constrains [6] [7]. [8] presents how the foraging theory is applied to track a desired temperature. In general, these works apply intelligent control techniques to obtain uniform temperature on a planar temperature grid. Herein, we propose another way to control this system.

The objective of this paper is to present the modeling of the temperature grid by means of a transfer matrix to design controllers via modern control theory. The control theory has tools to analyze the coupling level between inputs and outputs, and indexes to calculate the robustness and the stability of the system; therefore, we chose the modern control theory to model and control the planar temperature grid.

We propose two ways to model a system by using symmetrical positions of the actuators and temperature zones. To analyze the system we use singular value decomposition (SVD), relative gain array (RGA), and optimal condition number (OCN). Also, we present two controllers, one centralized and another distributed, for an uncertainty model of a system.

This paper is organized as follows: In the system modeling section, we present the selection, identification, validation, and analysis of the model.

In the controller design section, we present the grid performance with  $H_\infty$  controller and a multivariable PID. Finally, we present the conclusions, acknowledgment, and references.

## 1. SYSTEM MODELING

In this work, we used a platform composed of a planar temperature grid and a data acquisition system. The planar temperature grid has 16 light bulbs, actuators, and 25 LM35 integrated-circuit temperature sensors. The grid is shown in Figure 1. The data acquisition system has signal conditioners connected to a computer through its serial port, and a man-machine interface called MuTEPCO designed with GUI from Matlab™. We used the interface to monitor the sensor signals, drive the actuators, show the data in screen, and define control algorithms. The detailed description of the platform appears in [2].

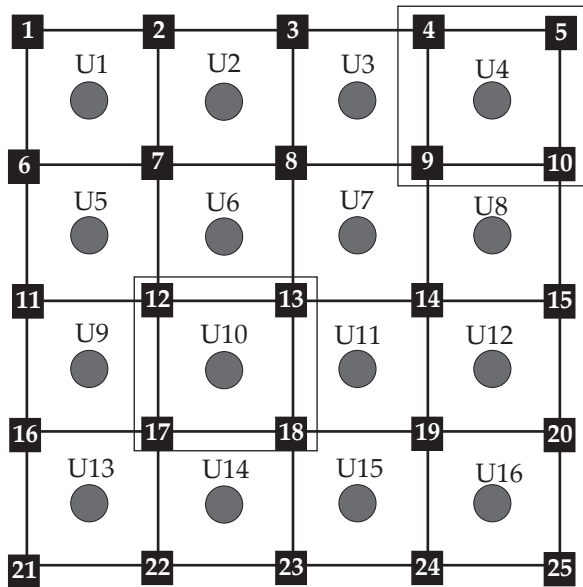


Figure 1. Planar temperature grid

This platform belongs to the research group Perception and Intelligent System (PSI) research group at Universidad del Valle in Colombia. The PSI built this platform to emulate complex processes, e.g. ill-conditioned multivariable systems, and the PSI uses the platform to design and test resource allocation algorithms.

In the next sub-sections, we present two ways to model the planar temperature grid with transfer functions. Firstly, we propose a method to model the system based on the location of sensors and actuators. Then, we model the system observing the temperature profile on the planar grid.

### 1.1. Modeling by symmetrical positions

To obtain squared transfer matrix, we defined actuator signals as inputs and the temperature average per cell as outputs. Each cell is conformed by one actuator and the four sensors around it; see Figure 1.

Each output is defined by (1).

$$y_i = (S_{i1} + S_{i2} + S_{i3} + S_{i4})/4 \tag{1}$$

Where  $y_i$  is the  $i$ -th measured average temperature corresponding to the four sensors ( $S_{ij}$  with  $j=1, 2, 3,$  and  $4$ ) of the  $i$ -th cell for  $i$ -th input. The inputs are pulse width modulation signals (PWM) and they drive the actuators. The excursion of each input signal is from 0 to 1 and corresponds to pulse width. The system has 16 inputs and 16 outputs; therefore, the multivariable system model is a  $16 \times 16$  transfer matrix that consists of 256 transfer functions.

The structure of the planar temperature grid allows deducting all transfer functions obtaining only 36 transfer functions that can be found via three step-signal tests. For example, note that the location of cell 1 is similar to location of cell 4; both have the same number of cells around them. Then, if all actuators present similar dynamics, the transfer function of cell 1 with respect to cell 2 ( $Y1/U2$ ) is similar to the transfer function between cell 4 and cell 8 ( $Y4/U8$ ), and to the transfer function between the cell 13 and cell 9 ( $Y13/U9$ ). Three experiments to find the 36 transfer function could be made; these experiments are described as follows:

In the first experiment, it is necessary to apply a step signal in  $u_1$  and to measure the  $y_1, y_2, y_3,$  and  $y_4$  outputs;  $y_5, y_9,$  and  $y_{13}$  outputs did not require to be measured because their locations with respect to  $u_1$  are similar to locations of  $y_2, y_3,$  and  $y_4$  outputs; hence, the transfer functions of  $y_5, y_9,$  and  $y_{13}$  with respect to  $u_1$  are equal to transfer functions of  $y_2, y_3,$  and  $y_4$  with respect to  $u_1$ . Next,  $y_7, y_8,$  and  $y_{12}$  outputs must be measured and  $y_{10}, y_{14},$  and  $y_{15}$  can be found by symmetry. Finally, each output on the grid diagonal must be measured separately. The dynamics obtained with respect to  $u_1$  are similar

to dynamics with respect to  $u_4$ ,  $u_{13}$ , and  $u_{16}$  inputs, *e. g.*, the  $Y_4/U_1$  transfer function is equal to the  $Y_1/U_4$  transfer function.

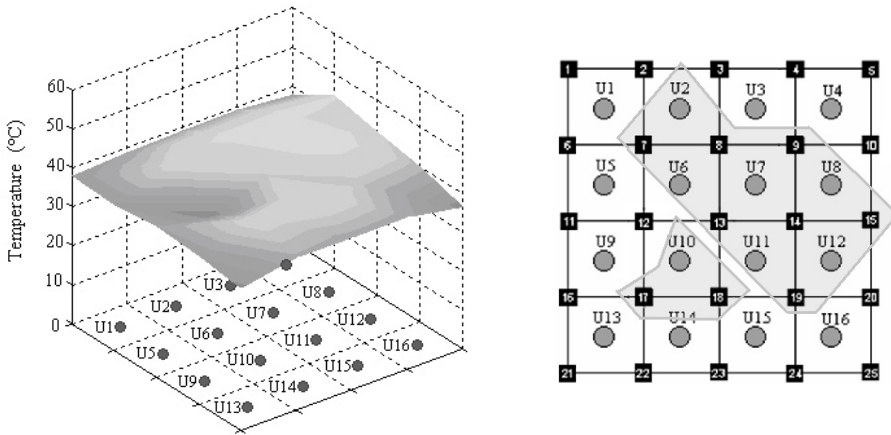
In the second experiment, a step signal is applied in  $u_8$  and each grid output must be measured separately. The sixteen outputs must be registered via this experiment. The dynamics to  $u_3$ ,  $u_2$ ,  $u_9$ ,  $u_{14}$ ,  $u_{15}$ , and  $u_{12}$  inputs can be obtained by symmetry, because the locations of these inputs are symmetric to the location of the  $u_8$ .

In the third experiment, a step signal is applied in  $u_{10}$  and the  $y_{10}$ ,  $y_9$ ,  $y_5$ , and  $y_1$  outputs must be measured;  $y_{14}$ ,  $y_{15}$  and  $y_{16}$  can be obtained by symmetry. The  $y_{11}$ ,  $y_8$ , and  $y_{12}$  outputs also require be measured and  $y_6$ ,  $y_2$ , and  $y_3$  outputs can be found by symmetry. Finally, each  $y_{13}$ ,  $y_7$ , and  $y_4$  output is measured separately. The dynamics for  $u_{10}$  are similar for the inputs  $u_{11}$ ,  $u_6$  and  $u_7$ ; *e.g.*, the transfer function  $Y_7/U_{10}$  is equal to the transfer function  $Y_{10}/U_7$ .

The previous modeling can be used as long as the dynamic characteristics of actuators are similar, otherwise, each transfer function must be obtained separately. We ran tests over actuators and noted that the dynamic characteristics of actuators are different; hence, it is not possible to use modeling by symmetrical locations. Furthermore, to calculate the overall model, getting each transfer function separately, long experimental time is necessary because each step test requires 20 minutes.

## 1.2. Modeling by temperature zones

We ran open-loop tests for different PWM percentages and actuator signals, and we observed that temperature surface conserves a distribution by regions, independent of its average temperature value. We obtained the planar temperature grid model by using two temperature zones, see Figure 2. The temperature averages on each zone are the system outputs. Therefore, the system has two outputs. The inputs are PWM percentages applied over actuators in each temperature zone. The system model was reduced from a transfer matrix with 256 elements to a transfer matrix with four elements.



**Figure 2.** Temperature Zones. Zone 1 is demarcated.

The  $u_2, u_7, u_6, u_8, u_{11}, u_{12},$  and  $u_{10}$  actuators belong to zone 1 and the others to zone 2. Sensors 7, 8, 9, 13, 14, 15, 19, 18, and 17 (Figure 1) measure the temperature in zone 1; the remaining sensors measure the temperature in zone 2. Zone 1 has 9 sensors and 7 actuators, and zone 2 has 16 sensors and 9 actuators. To obtain the system model we applied step signal in the inputs, and measured the average temperature per zone, system outputs. The step test allows defining the order of the transfer function of system model.

### 1.2.1. Selection, identification, and validation of the model

We selected a first order model for each transfer function of the transfer matrix. The transfer matrix has four components, one per input–output combination. Each block has a gain and a time constant. Figure 3 shows the links between inputs and outputs.

We saw the effect of each input over each output separately and we obtained the transfer functions observing the natural response curves of the system, see Figure 4. Transient analysis of the step test was used to estimate parameters of the transfer functions that relate each input to each output. To identify the system model, this was considered as linear plant; therefore, each plant output is the sum of outputs due to each input, see Figure 3.

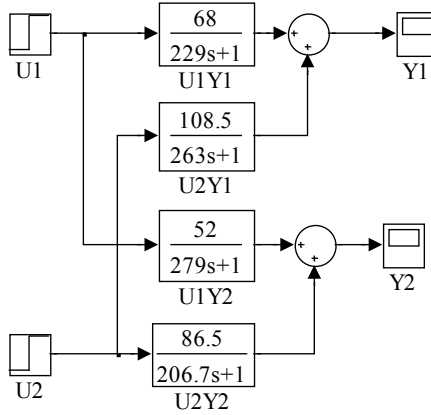


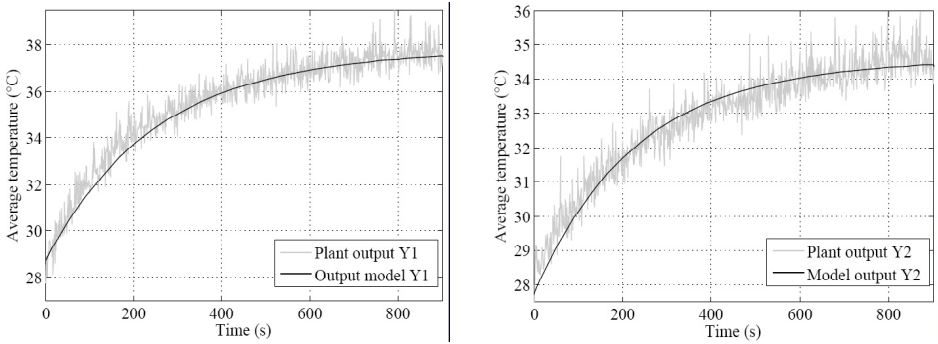
Figure 3. Block diagram of model

A step signal was applied to each input and each output signal was recorded. The parameters for each block were calculated from the curves obtained by using 'ident' from MATLAB™. Before the identification of the model, the curves were adjusted with the curve-fitting tool from MATLAB™ because these had much noise. Figure 4 shows the Y1 and Y2 outputs for the step applied in the U2 input. The step signal was applied in steady state. The delay was not taken into account, because the time constant is large. The four transfer functions obtained are presented in Table 1. The scaling transfer matrix was calculated with maximum temperature achieved during the experiment, 61.5° C.

Table 1  
Transfer Matrix

	Non-scaling		Scaling	
	U1	U2	U1	U2
Y1	$\frac{68}{229s+1}$	$\frac{108.5}{263s+1}$	$\frac{0.1106}{229s+1}$	$\frac{0.1756}{263s+1}$
Y2	$\frac{52}{279s+1}$	$\frac{86.5}{206.7s+1}$	$\frac{0.0846}{279s+1}$	$\frac{0.1407}{206.7s+1}$

To validate the model, we compared model responses to the responses of the real system. Figure 4 shows system and model response by step signal applied on U2 input.



**Figure 4.** Y1 and Y2 outputs for the model and plant

### 1.3. Uncertainty Modeling

To design controllers, it is necessary to obtain a model of a system coherent with the control objective. In practice, the model is different from the real system for many reasons, i.e., system parameters change, there are mistakes in sensor measurements, or the model does not include all dynamics (non-modeled dynamics). Some differences between the system modeled and the real system can be included in an uncertainty model. Therefore, to design controllers the use of models with uncertainties is recommended. We defined that said system has parametric multiplicative uncertainties (2) over time constants.

$$\frac{[G_{pij} - G_{oij}]}{G_{oij}} \tag{2}$$

Initially, we obtained a model per input-output pair, see Table 2, but we observed that uncertainty models are similar; then, we decided to find a general uncertainty model (structured multiplicative uncertainty model), based on the result presented by [10].



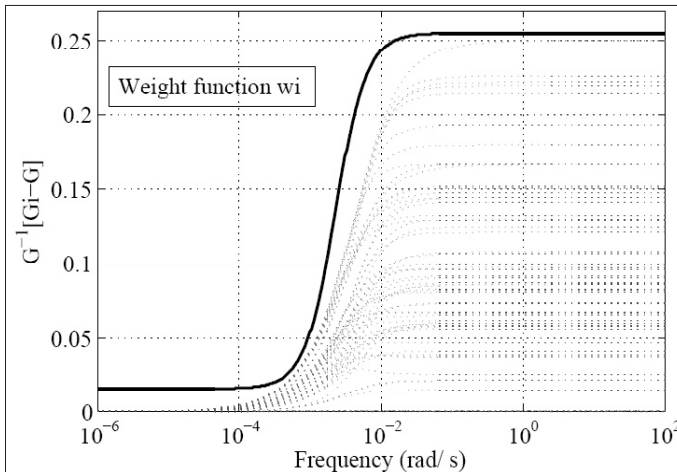
**Table 2**  
Uncertainties

	U1	U2
Y1	$\frac{0.5012s + 0.0012}{s + 0.0046}$	$\frac{0.4970s + 0.0009}{s + 0.0036}$
Y2	$\frac{0.5013s + 0.0010}{s + 0.0038}$	$\frac{0.5003s + 0.0012}{s + 0.0049}$

This model is obtained with minimum singular value of relative error  $\sigma[G\phi^{-1}[Gp - Go]]$ , varying the parameters of interest, in this instance the time constants of transfer functions. The uncertainty function is defined by (3).

$$\omega_i(s) = \frac{0.2670s + 0.000036}{s + 0.002279} \tag{3}$$

We obtained the frequency response of minimum singular value of the system through variation of 20% on time constants. We defined a weight function that covers the sweep of frequency response or the uncertainty region for minimum singular value, see Figure 5.



**Figure 5.** Uncertainty weight function for  $\sigma[G\phi^{-1}[Gp - Go]]$

#### 1.4. System analysis

To analyze the system, we used the condition number,  $CN$ , the optimal condition number,  $OCN$ , and the relative gain array, RGA. These indexes were obtained by the plant model.

The steady state transfer matrix was decomposed in singular values, the minimum singular value is  $\underline{\sigma} = 0.0027$  and the maximum singular value is  $\overline{\sigma} = 0.2646$ . The condition number is  $CN = \overline{\sigma}/\underline{\sigma} = 99.2181$ . This value indicates that the system is ill-conditioned and presents sensitivity among outputs and inputs.

The input-output pairs were determined from the relative gain array. These pairs were used to design the decentralized feedback control. The relative gain array ( $\Lambda$ ) was obtained for two frequencies  $\omega = 0$  and  $\omega = \infty$ . The relative gain arrays analyzed are in (4) and (5).

$$\Lambda(\omega = 0) = \begin{bmatrix} 22.0523 & -21.0523 \\ -21.0523 & 22.0523 \end{bmatrix} \quad (4)$$

$$\Lambda(\omega = \infty) = \begin{bmatrix} -2.6030 & 1.6030 \\ 1.6030 & -2.6030 \end{bmatrix} \quad (5)$$

Based on useful properties of the relative gain array  $\Lambda(\omega=0)$  to control, the input-output pairs corresponding to positive values of relative gain array should be selected; therefore, we selected  $Y1/U1$  and  $Y2/U2$ .

The condition number is also calculated. This was obtained from model for scaling plant. The minimized or optimal condition number is a more reliable factor. This number was calculated from the relative gain array on steady state. The sum-norm of the relative gain array in  $\omega = 0$  calculates the optimal condition number (6).

$$\sigma^*(\omega = 0) = \|\Lambda(\omega = 0)\|_{sum} = 86.2092 \quad (6)$$

By comparing the optimal condition number to the condition number obtained from singular values, we observed that these are closed and concluded that the system is ill-conditioned.

## 2. controller design

Herein, we present two multivariable controllers, one centralized controller and another distributed controller. The design of the two controllers is based on the analysis of the system. To design the controllers, we used a weight function that includes the requirements for each controller. Performance and stability of the plant with each controller were evaluated by using the  $\mu$  analysis. To validate the controllers, we present the simulation results for one tracking test and one regulation test.

### 2.1. Decentralized controller design

We selected a K-diagonal controller, which is a decentralized controller. To design the controller, we used relative gains array (RGA) in  $\omega = 0$ . We chose input-output pairs for non-negative elements of the RGA from (4), [11]. The input-output pairs chosen are  $Y1/U1$  and  $Y2/U2$ , obtaining a diagonal transfer matrix.

We made an experimental design of PID controllers for input-output pair and took into account the uncertainty models. The requirements for the controller design decrease the system's stabilization time and allow acceptable overshoot. We defined the new time constant as half of system time constant in open loop. We chose the minimum time constant, the transfer matrix, to define the new time constant ( $\tau_{ij} = 0.8 \tau_{ij}$ ). We used a damper factor  $\rho = 0.7$ . This damper factor establishes an overshoot under 25%. The controller transfer functions calculated are presented below:

$k_{11}$  controller function for  $Y1/U1$  is:

$$k_{11} = \frac{154.9 s + 8.392}{s} \quad (7)$$

$k_{22}$  controller function for  $Y2/U2$  is:

$$k_{22} = \frac{121.7 s + 7.308}{s} \quad (8)$$

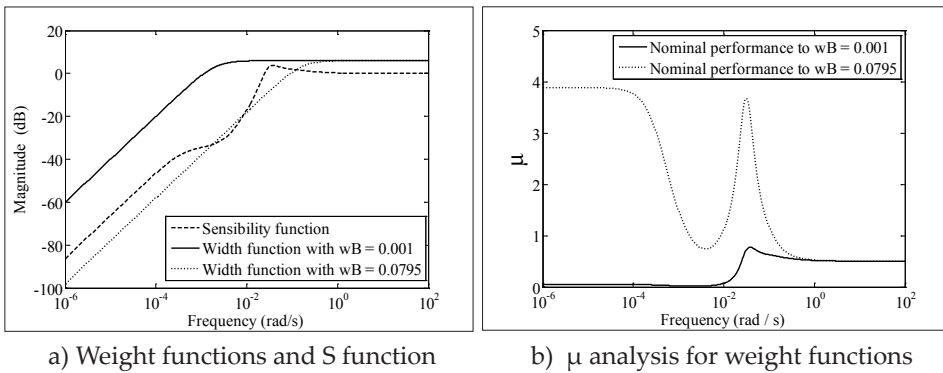
To evaluate the performance of the controllers, we chose a weight for the sensitivity function (S). The sensitivity function is a good indicator of close-loop performance for multivariable systems. The weight chosen is represented by (9):

$$\Omega_p(s) = \frac{s/M + \omega_B}{s + \omega_B A} = \frac{0.5012s + 0.0795}{s} \quad (9)$$

Where,  $\omega_B = 0.0795$  is the minimum natural frequency between  $Y1/U1$  and  $Y2/U2$  transfer functions. We selected the sensitivity function magnitude  $M=1.9953$  for all outputs, and maximum steady state error  $A=0$  to ensure integral action. To complement the performance evaluation, we also used the  $\mu$  analysis.

Figure 6a shows two weight functions and the sensitivity function of system with K-diagonal controller. The weight function with  $\omega_B = 0.0795$  is less than the sensitivity function at some frequencies. This weight function is restrictive for the system; hence, we chose a less restrictive minimum natural frequency  $\omega_B = 0.001$ . See Figure 6a.

Figure 6b shows the nominal performance of the K controller by  $\mu$  analysis. For the weight function with  $\omega_B = 0.0795$ , the controller does not have good performance since the nominal performance is greater than one in most frequencies. With a less restrictive weight function, e.g., using  $\omega_B = 0.001$ , nominal performance improves.



**Figure 6.** Performance evaluation for the K-diagonal controller.

For  $\omega_B = 0.0795$ , robust performance and robust stability of the system are shown in Figure 7. The nominal and robust performances are greater than one for most frequencies; however, the robust stability is less than one, i.e. the system presents robust stability for the full range of frequencies.

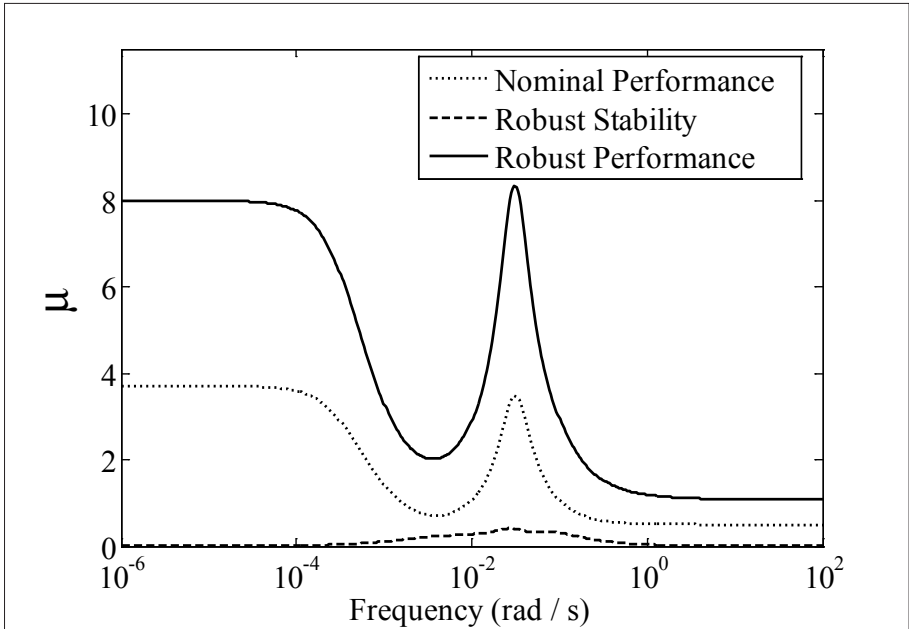
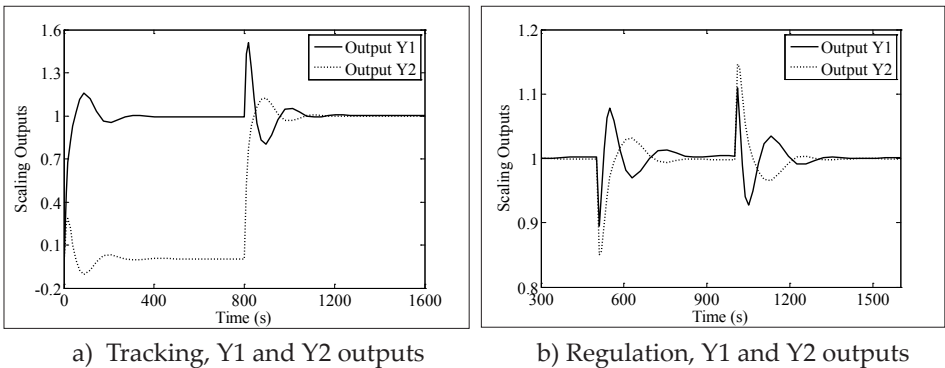


Figure 7. Performance and robust analysis for decentralized or K-diagonal controller.

The controllers were tested separately for each input-output pair and achieved desired specifications. When we tested the controlled system, the stabilized time was less than the specified time. The controllers have good regulation and track the reference correctly. See Figure 8.



a) Tracking, Y1 and Y2 outputs

b) Regulation, Y1 and Y2 outputs

Figure 8. Controlled outputs system for K-diagonal controller

## 2.2. Design of robust H $\infty$ controller

The other control strategy chosen was an H $\infty$  control. A generalized plant model P was obtained and a controller was designed from the algorithms proposed in [11]. The generalized plant order is 6 inputs, 6 outputs, and 8 states. The H $\infty$  controller dynamic has 2 outputs, 2 inputs, and 2 states.

To evaluate the performance of the controllers, we used the  $\mu$  analysis. Figure 9 shows the robust stability, robust performance, and nominal performance of the system with an H $\infty$  control. Performance evaluation was made for  $\omega_B = 0.0795$  and  $\omega_B = 0.001$ .

Figure 9a shows that the robust and nominal performances are greater than one at low frequencies, which is bad performance at these frequencies. For  $\omega_B = 0.001$ , the nominal performance has been improved, but robust performance remains greater than one. See Figure 9b.

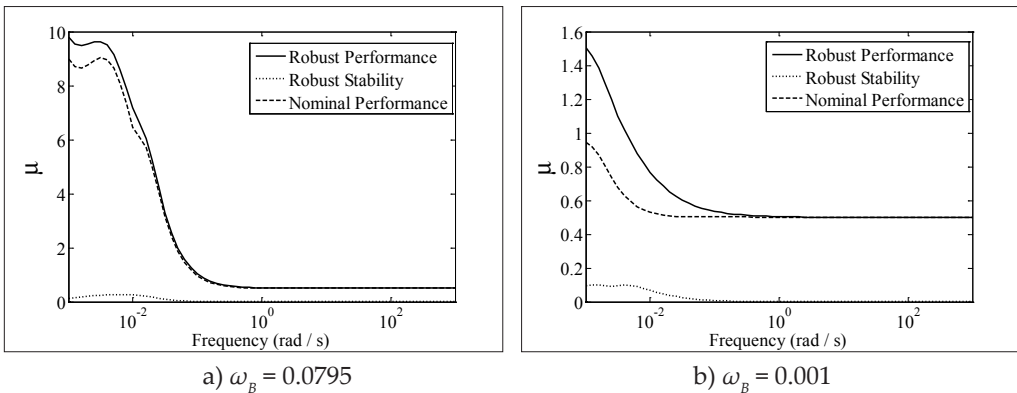
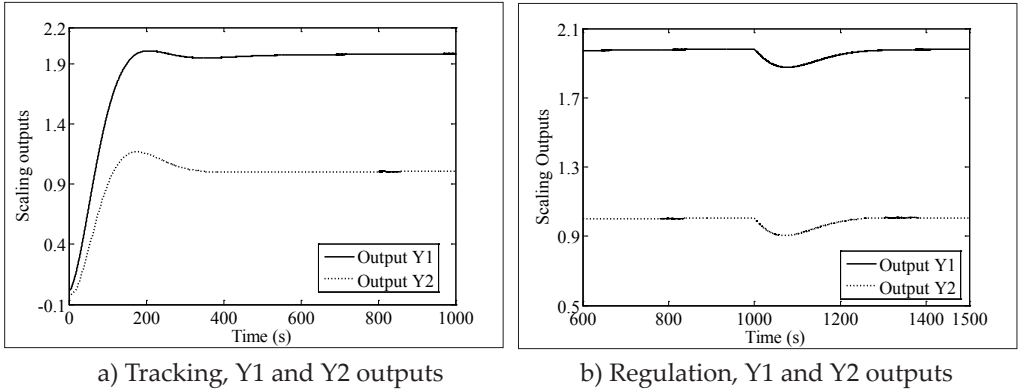


Figure 9.  $\mu$  analysis for H $\infty$  controller.

The H $\infty$  controller responses for the tracking and regulation tests are shown in Figure 10. In the regulation test, the temperature grid model with H $\infty$  controller presents an overshoot of about 12%. In the same test, the model with the K-diagonal controller presents an overshoot of about 16%. In the regulation test, the grid model with the H $\infty$  controller presents a stabilization time of 200s. See Figure 10b. This time is less than the stabilization time presented by the model with the K-diagonal controller, which was approximately 300s.



**Figure 10.** Controlled system outputs for the  $H^\infty$  controller with  $\omega_b = 0.0795$ .

### 3. CONCLUSION

An ill-conditioned multivariable system was identified by using transient analysis of step response. We chose a model based on temperature distribution, obtained matrix transfer parameters through experimental tests, and validated the model by comparing real response to simulated response. The model considers parametric uncertainties over time constants.

The system was analyzed from singular value decomposition and relative gain array. We calculated the condition number and optimal condition number, which showed that the system is ill-conditioned. The frequency response analysis of RGA elements allowed selection input-output pair to design PI decentralized controllers.

When the temperature grid was represented with a model in the Laplace domain, then, we could apply the analysis tools to evaluate the robust stability and the nominal and robust performance, we used the  $\mu$  analysis. We compared the decentralized control strategy with  $H^\infty$  centralized control strategy through  $\mu$  analysis and controller response to track and regulate the nominal model. This comparison shows a compromise between response speed and robust performance and stability.

The measured signals have noise; this makes it difficult to identify the model. Other identification techniques can be used to obtain more accurate models. To improve the model presented in this paper, more temperature zones can be defined, but this implies an increase in the order of the transfer matrix of the system and complexity of its analysis.

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