

Fenómeno de transporte en superconductores: vórtices cinemáticos

Transport phenomena in superconductors: kinematic vortex

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Resumen- La teoría fenomenológica Ginzburg-Landau (FGLT) es una fuerte herramienta para entender la física de los materiales superconductores a temperaturas críticas en presencia de campos magnéticos y corrientes aplicadas. El FGLT se deriva de la teoría del segundo orden de transición de Landau basada en un fenómeno crítico, llevada a un conjunto de dos ecuaciones no lineales Ginzburg-Landau (GLE). En el presente trabajo, resolvimos las ecuaciones de GLE en una placa superconductora en presencia de una corriente aplicada a campo magnético cero. Analizamos la aparición y aniquilación de pares vórtice y anti-vórtice en la mitad de la placa con una corriente externa aplicada. Una pequeña resistividad es encontrada en el rango Meissner en la curva de corriente-voltaje.

Palabras Clave- Ginzburg-Landau, Superconductor, Vórtice.

Abstract- The phenomenological Ginzburg-Landau theory (FGLT) is a strong tool in understanding the physics of the superconductors at low critical temperature in the presence of applied fields and currents. The FGLT is derived from the second order transition theory of Landau based on critical phenomena, leading to a set of two coupled non-linear Ginzburg-Landau equations (GLE). In this paper, we solve the GLE to a superconducting slab of Al in presence of applied current j at zero magnetic fields. We have analysed the appearance and subsequent annihilation of vortex-anti-vortex pairs in the middle of the sample at an external applied current j_c . A small resistivity is found in Meissner range in the current-voltage curve at $j \leq j_c$.

Keywords- Ginzburg-Landau, Superconductors, Vortex

1. INTRODUCTION

The dynamics of vortices in low critical temperature superconductors have many technological, scientific and industrial applications from the point of view of electrical current transport. The magnetic flux penetrates in a superconductor type II in the form of quantized fluxoids called vortices Abrikosov-Shubnikov, these vortices locally destroy the superconducting state and it is only possible when the Lorentz force, due to applied currents, exceed the anchoring forces of the structural defects, magnetic or topological of the material, leading to Joule heat appearance. The control and/or manipulation of vortex state is very important to limit the loss of heat in the electronic elements and lead to the manufacture of new devices such as rectifiers of currents, logic elements, photon detectors, fabrication of SQUIDS, etc. [1]-[10].

In the absence of magnetic field is possible the existence of pairs vortex-anti-vortex, known as kinematic vortices, they appear as a result of the magnetic field originated by the applied currents (Ampere's law). The theory most commonly used to analyse the physical of the conventional superconductivity or superconductivity at low critical temperature T_c , is the phenomenological theory Ginzburg-Landau (FGLT). The FGLT is based on the second order phase transition of Landau

and describes the superconducting state through the pseudo-function of complex wave $\psi(r;t)$, whose magnitude squared represents the density of superconducting electrons and of the vector potential $A(r;t)$, related to the magnetic induction as $B = \nabla \times A$. A large amount of experimental and theoretical work has been done since the discovery of this state of matter in 1911.

One of the first applications in engineering was in nano-structures superconductor-magneto in centres production of anchoring in superconducting films, in these structures a critical current superconductor increases due to periodicity of anchor centres [11]-[12].

M. V. Milosevic, et al., studied the effect of electric current in superconductor-magneto hybrid microstructures, he found that a critical current increases with the inclusion of such defects and superconductivity persists to larger currents applied [13]. Berdiyrov G., et al., analysed the temperature dependency of an applied current to zero field on the vortex dynamics in a thin plate of Nb , in this study the state of flux-flow is dynamically stable at low temperatures, their results are in good qualitative agreement with experiments. The effect of the functionality of surface about the electronic transport properties in Ti3C2-MXene was analysed, finding that the design of materials based on MXene may be useful in energy storage where the electronic transport can be maximized. Using three-dimensional simulations the authors showed that vortices Abrikosov captured in a Josephson cavity in the presence of external current generate vortices-anti-vortex pairs, the frequency of tunnelling of these pairs increase in a band of determinate frequencies [14]-[15].

The study of vortex-anti-vortex pair generation in the absence of applied magnetic field has been extensively studied by Berdiyrov, et al., he showed that an external current can produce these pairs in a thin plate, commonly called vortices kinematic [16]. P. Sanchez-Lotero, et al., analysed the flux-flow resistivity in superconducting films of different widths, found an anchoring vortices induced by the superficial superconductivity, this anchoring prevents a movement of the vortices and the appearance of voltage leading to a transition of the mesoscopic to macroscopic regimen [17]. J. Barba-Ortega et al., studied theoretically the dependence of the boundary conditions and

the dimensionality on the magnetic response of a low T_c superconductor, he found that a superconducting/superconducting interface at higher critical temperature T_c increases the superconductor/normal transition field and enhanced the superficial superconductivity, also he show that the upper and lower fields are independent of the dimensionality of the sample [18]-[19]. Golod T., et al., provided a proof of concept of the Abrikosov vortex as a random access memory cell, wherein a vortex is used as an informatics bit, the cells are characterized by an infinity magnetoresistance between states 0 and 1 in a time short of access and an energy extremely low recording. The non-volatility and the perfect repeatability are inherent to such device, due to the quantized nature of the vortex [20]. In this work we resolved the time dependent Ginzburg-Landau equations in an isotropic type II superconducting slab in presence of an applied electric current at zero magnetic field. For low values of the applied current a small resistivity is found due to metallic contacts where a current is applied. For a certain value of current J_c a pair vortex-anti-vortex is created in the half of the slab and the resistivity increases abruptly. Consequential creations and annihilations of vortices-anti-vortex pairs are appreciated.

2. THEORETICAL FORMALISM

The Ginzburg-Landau model take account of the superconducting electronic density and of the magnetic response of the material through of the functions ψ and A in the presence of external currents related with the electrostatic potential φ at temperature $T=0$ through (1) e (2):

$$\frac{u}{\sqrt{1 + \Gamma^2 |\psi|^2}} \left(\frac{\partial}{\partial t} + i\varphi + \frac{\Gamma^2}{2} \frac{\partial |\psi|^2}{\partial t} \right) \psi = (\nabla - iA)^2 \psi + (1 - |\psi|^2) \psi \quad (1)$$

$$\nabla^2 \varphi = \nabla \cdot J_s = \nabla \cdot (\text{Im}[\psi^* (\nabla - iA) \psi]) \quad (2)$$

J_s is the supercurrent density in units of $J_0 = C\Phi_0/8\pi^2 \lambda^2 \xi$, where λ is the penetration length and ξ the coherence length, ψ in units of $\psi_0 = (\alpha/\beta)^{1/2}$, and β are two phenomenological parameters characteristic of the material, length in units of ξ , time t in units of τ , potential

vector A in units of $H_{c2}\xi$, where H_{c2} is the second critical field, scalar potential φ in $\hbar/2et$ units. $\Gamma = 2\tau_E\psi_0/\hbar$, (τ_E is the collision inelastic electronic. For $\tau_E \sim 10ns$, so $\Gamma \cong 1000$), we choose $U=5.79$ [21]-[24]. The external electric current is applied in points where $\psi = 0$ e $\nabla\varphi = -J$ (Metallic contacts), in another points, the Neumann boundary conditions were used and $J_{\perp} = \hat{n} \cdot (-i\nabla + A)\psi|_n = 0$ [23]. The studied sample is a superconducting Al slab ($(\xi_0) = 100nm$) [25], of cross section transversal axb in the (x,y) plane. The equations (1) and (2) were numerically solved using the link variable method ($U\psi$) in a rectangle with $N_x \times N_y$ cells, grid size $\Delta_x \times \Delta_y N_x = a/\Delta_x$ e $N_y = b/\Delta_y$ [22]. If $\psi(x_i, y_j) = \psi_{ij}$, $\varphi(x_i, y_j) = \varphi_{ij}$ for $i=1, N_x+1, j=1, N_y+1$, The GLE can be written as:

$$\frac{\partial\psi_{ij}}{\partial t} = \sqrt{1 + \Gamma^2|\psi|^2} \frac{\Theta_{ij}}{u} - \frac{\Gamma^2\psi_{ij} \text{Re}(\overline{\psi_{ij}}\Theta_{ij}/u)}{\sqrt{1 + \Gamma^2|\psi|^2}} - i\varphi_{ij}\psi_{ij} \quad (3)$$

$$\Theta_{ij} = \frac{U_{ij}^x\psi_{i+1,j} - 2\psi_{ij} + \overline{U_{i-1,j}^x}\psi_{i-1,j}}{\Delta_x^2} + \frac{U_{ij}^y\psi_{i,j+1} - 2\psi_{ij} + \overline{U_{i,j-1}^y}\psi_{i,j-1}}{\Delta_y^2} + \psi_{ij} - \psi_{ij}^3 \quad (4)$$

Where the new variables of the method ($U\psi$) and the superconductor currents formed $\psi_{ij}^{s\alpha}$ in the axes $\alpha = x, y$ are given by:

$$U^x(x, y, t) = e^{-i\int_{x_0}^x A_y(\xi, y, t) d\xi};$$

$$U^y(x, y, t) = e^{-i\int_{y_0}^y A_x(x, \eta, t) d\eta} \quad (5)$$

$$J_{ij}^{sx} = \frac{1}{\Delta_x} \text{Im}\{\overline{\psi_{ij}} U_{ij}^x \psi_{i+1,j}\};$$

$$J_{ij}^{sy} = \frac{1}{\Delta_y} \text{Im}\{\overline{\psi_{ij}} U_{ij}^y \psi_{i,j+1}\} \quad (6)$$

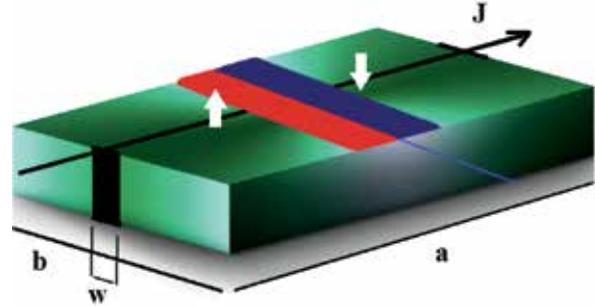
The conditions of contour out of the metallic contact of width W where the external current is applied for J^{sx} and ψ are:

$$J_{i,j}^{sx} = 0; J_{N_x,j}^{sx} = 0; \text{ para } 2 \leq j \leq N_{wi} = \frac{b-w}{2\Delta_y} + 1; N_{wf} = \frac{b+w}{2\Delta_y} + 1 \leq j \leq N_y \quad (7)$$

$$J_{i,1}^{sy} = 0; J_{N_y}^{sy} = 0; \text{ para } 2 \leq i \leq N_y \quad (8)$$

Within of metallic contact we have $\psi_{i,j} = \psi_{N_x+1,j} = 0$ for $N_{wi} \leq j \leq N_{wf}$.

Fig. 1. DIAGRAM OF THE STUDIED SAMPLE, J IS THE APPLIED CURRENT, W IS THE SIZE OF THE METALLIC CONTACT, X axb IS THE SIZE OF THE SAMPLE. THE BLUE AND RED COLOUR IDENTIFIES THE DIFFERENCE OF THE PHASE OF THE ORDER PARAMETER (KIEMATIC VORTEX)

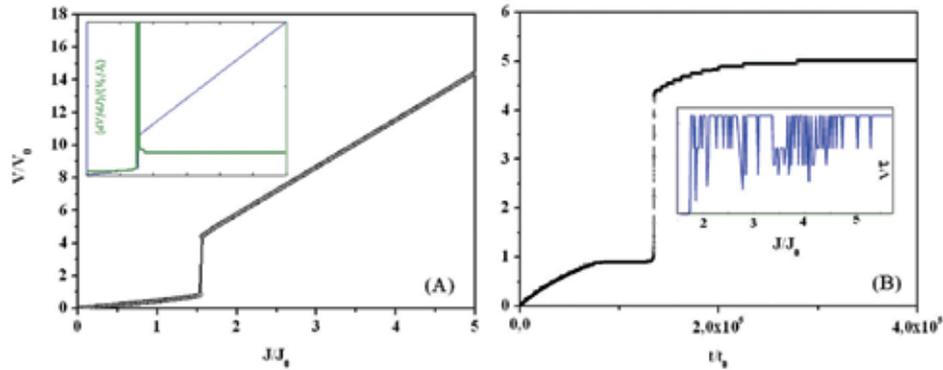


Source: authors.

3. RESULTS AND DISCUSION

The parameters used in our simulation were: sample size $a \times b = 12\xi \times 8\xi$, $\Delta_x = \Delta_y = 0.1$, $\Delta J = 10^{-3}$, $\Delta t = 0.001$, $W = 0.2$ parameter Ginzburg-Landau typical for the aluminium is $k = 1.0$. The initial conditions for the simulation are: Meissner state $\psi(x, y, 0, t = 0) = 1$ and $J_i(t = 0) = 0.0$ to $j_f(t) = 6.0$. A very interesting fact in this type of systems is the appearance of vortices in the absence of magnetic field, called kinematic vortices. Physically, these vortices, like Abrikosov vortices, are points in space-time where the pseudo-function of superconductor wave or order parameter has a degree equal to zero, and its phase changes a value $2\pi N$ around these points, N indicates the vorticity. We showed that these pairs of vortices nucleating in the sides perpendicular to the direction of application of the current at a half point of the slab; subsequently enter annihilating in the centre. In the absence of field, both vortices appear at the same time and annihilate crossing the border simultaneously in the line $x=a/2$ (Fig. 1). If you apply a magnetic field in the sample the dynamic of kinematic vortex-anti-vortex pair change considerably, the points of creation-annihilation of these pairs are determined by distribution of currents in the system [16].

Fig. 2. (A) CURVE VOLTAGE V/V_0 IN FUNTION OF THE APPLIED CURRENT J/J_0 AND THE RESISTIVITY AS THE DERIVATIVE $\partial V/\partial J$ (WINDOW). (B) VOLTAGE IN FUNSION OF THE TIME t AND FREQUENCY $\nu\tau$ IN FUNSION OF THE APPLIED CURRENT

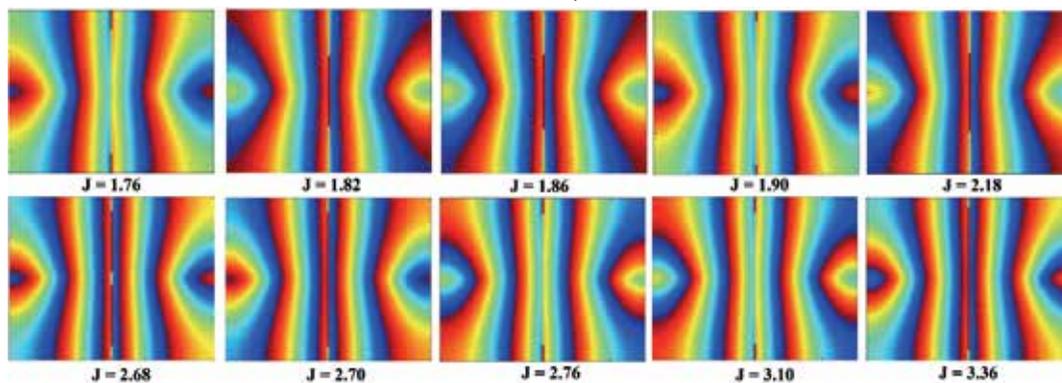


Source: authors.

Fig. 2(A) shows the voltage curve V/V_0 and the resistivity obtained by the derivative $\rho = \partial V/\partial J$ as a function of applied current J/J_0 (window), for mesoscopic regime this resistivity shows that the presence of the superficial barrier allow a little resistivity at low applied currents. FIG. 2 (B) shows the voltage as a function of the time and frequency $\nu\tau$ a function of applied current (window). As can be seen, for low values of the applied current, the superconducting material experiences a slight resistance, this can be explained by the resistivity of the metallic contacts where the current is applied ($\psi = 0$), in these points is zero superconductivity (ohmic material). Increasing the current at a determinate value $J_1 = 1.76$ appears a discontinuity in the resistivity curve (window, Fig. 2 (A)) representing the entry of a pair of vortices kinematic in the plate, likewise can to observe the abrupt leap of the voltage as function of time (Fig. 2 (B)). In Fig. 3 we have graphically the phase of

order parameter $\Delta\phi$ for several applied currents. A circulation of the phase of the order parameter through an enclosed path that has N vortices will be equal to $2\pi N$. In this figure we appreciated that the entry of vortex occurs in the middle part of sample $x = a/2$ and phase variation goes from red to blue $\Delta\phi = \pi$ and from blue to red $\Delta\phi = -\pi$, that is total vorticity $\Delta\phi = 0$ and $N = 0$, then we have a pair vortex-anti-vortex that nucleates by the half of the sample. The pairs of kinematic vortices enter in the sample overcoming the Beam-Livington barrier energy and annihilating in the centre of the material. Of Up to bottom and from left to right the settings of phase are given for currents $J=1.76, 1.82, 1.86, 1.90, 2.18, 2.68, 2.70, 2.76, 3.10, 3.36$, in all of them we have pairs vortex-anti-vortex and $\Delta\phi = 0$. Superconductivity is completely destroyed at the points where the electric current is applied, so we cannot have accurate information of the phase changes present.

Fig. 3. PHASE OF THE ORDER PARAMETER $\Delta\phi$ FOR SEVERAL CURRENTS APPLIED



Source: authors.

4. CONCLUSION

We solved the time dependent Ginzburg-Landau equations to study the appearance and subsequent annihilation of vortices-anti-vortex kinematics pairs in a superconducting slab at zero magnetic field and with a applied external current J . We note that for $J < J_I$ a small resistivity appears due to the presence of metallic contacts, but at $J = J_I$ at a time t_I , abrupt jumps in the resistivity of the slab occur due to entrance of pairs vortex-anti-vortex. Increasing the applied current the superconductivity is destroyed and an ohmic behaviour is observed in the voltage-current curve.

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