

## Compensation of DC-link voltage oscillations in grid connected PV systems

## Compensación de oscilaciones de voltaje en el enlace DC de sistemas fotovoltaicos conectados a la red

*Carlos Andrés Ramos Paja<sup>1\*</sup>, Giovanni Petrone<sup>2</sup>, Andrés Julián Saavedra Montes<sup>1</sup>*

<sup>1</sup>Universidad Nacional de Colombia. Carrera 80 No 65-223. Medellín, Colombia.

<sup>2</sup>University of Salerno. Via Ponte Don Melillo 84084. Fisciano - Salerno - Italy.

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### Abstract

This paper presents a compensation technique to mitigate the effect of DC-link voltage oscillations on PV systems. The main features of the technique are: the compensation is applied directly to the duty cycle, so it is simple to integrate with traditional maximum power point tracking systems; and the compensation calculation does not depend on the systems parameters, so its design is general. Explicit equations are provided for PV systems based on Boost, Buck and Buck-Boost dc/dc converters. Finally, the proposed approach is experimentally verified.

----- *Keywords:* PV system, dc/dc converter, grid connection, maximum power point tracking

### Resumen

Se presenta una técnica para compensar el efecto de las oscilaciones en el enlace DC en sistemas fotovoltaicos. Las principales características de la técnica son: la compensación se aplica directamente al ciclo de trabajo, por tanto es simple de integrar con sistemas tradicionales de maximización de potencia; y el cálculo de la compensación es independiente de los parámetros del sistema, por tanto el diseño es general. Se proveen ecuaciones explícitas para sistemas fotovoltaicos basados en convertidores dc/dc tipo Boost,

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\* Autor de correspondencia: teléfono: + 57 + 4 + 4255345, fax: +57 + 4 + 2341002, correo electrónico: caramosp@unal.edu.co (C. Ramos)

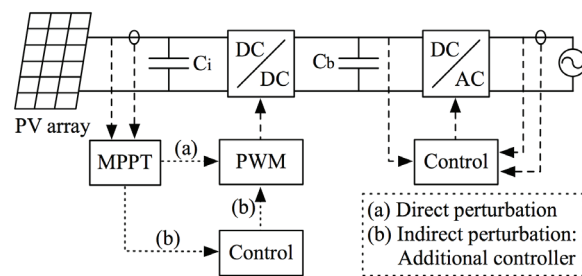
Buck y Buck-Boost. Finalmente, la solución se valida a través de resultados experimentales.

----- *Palabras clave:* Sistemas fotovoltaicos, convertidores dc/dc, conexión a la red, seguimiento de punto de máxima potencia distribuida

### Introduction

Photovoltaic (PV) applications are assuming a significant relevance in the production of worldwide energy, especially for the capability to produce energy in hostile contexts, like in emergent countries or in extreme environmental conditions. In such a cases small PV plants (lower than 10 kW), which are characterized by an extreme modularity and flexibility, are widely used for both stand-alone and grid-connected applications. The market of small PV systems is supported also by the increase of PV plants integrated in the urban context, installed with the aim of supplying energy locally. Such applications mainly include the Building Integrated PV (BIPV) systems, where the PV source contributes to make the buildings self-contained from the energetic point of view. Nonetheless in such a cases the probability of partial shading of the PV field might be not negligible and for this reason the PV field is decomposed in sub-modules, each one equipped with own power stage and Maximum Power Point Tracking (MPPT) controller [1]. As a consequence, the PV inverters dedicated to the small PV plants must be characterized by a large range for the input voltage in order to accept different configurations of the PV field. This capability is assured by adopting inverters based on a double stage architecture where the first stage, which usually is a dc/dc converter, can be used to adapt the PV array voltage in order to meet the requirements of the dc/ac second stage, which is used to supply an ac load or to inject the produced power into the grid. This configuration is effective also in terms of controllability because the first stage can be devoted to track the maximum power from the PV array, while the second stage is used to produce ac current with low Total Harmonic Distortion (THD).

The double-stage PV system presented in figure 1 is typically operated in two modes: (a) perturbing the duty cycle of the dc/dc converter to track the PV Maximum Power Point (MPP) [2], or (b) perturbing the reference of a control loop designed to regulate the PV voltage [3].



**Figure 1** Double stage PV grid-connected system

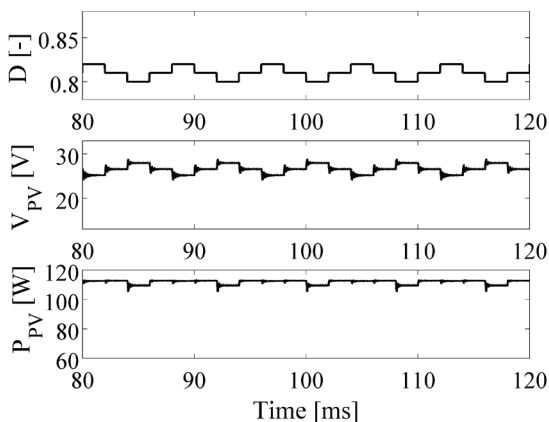
The mode (a) is simpler from the implementation point of view because the MPPT is able to track the MPP for any uniform irradiance condition, but it is sensible to disturbances at the dc/dc converter output. Instead, mode (b) is able to reject load perturbations, but classically its design depends on the system parameters [3], so it is difficult to guarantee the designed behavior for all the operating range, and also it is not possible to provide a general controller for any application. Therefore, PV systems based on mode (a) are more general than those ones based on mode (b). Figure 2 presents the simulation of the PV system of figure 1 operating in mode (a) without any perturbation on the dc/dc converter output, namely the DC-link voltage  $V_b$ , considering also a Boost converter and a Kyocera KC120 PV panel [4]. In such a simulation the MPPT controller, which is based on a P&O algorithm [2], defines a three points behavior on the dc/dc converter duty cycle  $D$ , which denotes a correct MPPT operation and a stable profile [1, 2, 3].

Moreover, such stable D waveform is propagated to the PV voltage  $V_{pv}$  since

$$V_{pv} = V_b / M(D) \quad (1)$$

where  $M(D) = 1/(1-D)$  represents the Boost converter voltage conversion ratio in Continuous Conduction Mode (CCM) [5]. From (1) it is noted that stable D profiles generate stable  $V_{pv}$  profiles and consequently, if the D profile is settled on the basis of an MPPT algorithm [3], the power  $P_{pv}$  generated by the PV module, will assume values near the maximum one. Such conditions are illustrated in figure 2, where D,  $V_{pv}$  and  $P_{pv}$  exhibit stable profiles, and the power extracted from the PV panel is 112 W, which corresponds to the KC120 maximum power at 35° temperature and 1000 W/m² irradiance. In the simulation the PV module is modeled by the non-linear equation given in (2), where the PV current  $I_{pv}$  and voltage  $V_{pv}$  are reported.  $I_{sc}$  is the PV short-circuit current and A and B are parameters [6] extracted from the datasheet.

$$I_{pv} = I_{sc} - A(1 - e^{B \cdot V_{pv}}) \quad (2)$$

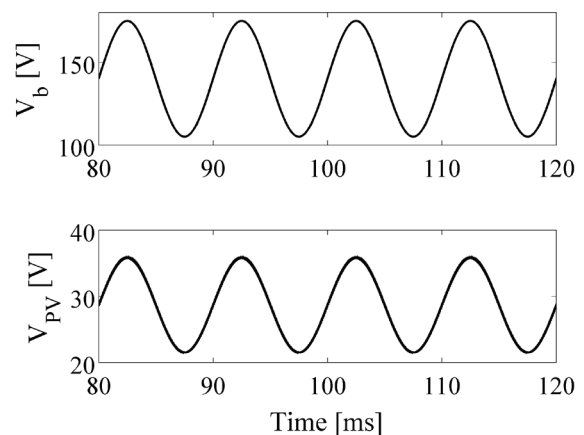


**Figure 2** MPPT operation without  $V_b$  perturbation

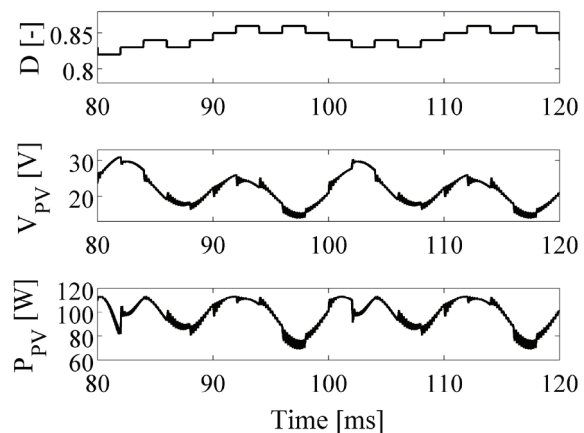
In mono-phase applications, and in non-balanced three-phase ones, the double stage architecture presented in figure 1 exhibits voltage oscillations at the DC-link capacitor  $C_b$ , thus at the dc/dc converter output terminals. Such oscillations are caused by the difference between the sinusoidal

power injected into the grid and the DC power extracted from the PV panel [3]. Moreover, such DC-link voltage  $V_b$  oscillations exhibit a sinusoidal profile with a frequency equal to the double of the grid frequency, and their amplitude is inversely to  $C_b$  [7].

Figure 3(a) presents a  $V_b$  perturbation caused by a small  $C_b$  capacitor, which generates a sinusoidal profile in the panel voltage  $V_{pv}$  if mode (a) is adopted. Such a  $V_{pv}$  profile confuses the MPPT algorithm [2, 3] leading to a sinusoidal power production far from the maximum power as depicted in figure 3(b), 112 W in this case.



(a) Perturbation transmission to PV terminals



(b) MPPT operation

**Figure 3** PV system operation with  $V_b$  perturbation

Contrasting  $P_{pv}$  in figure 2 and figure 3(b), it is evident that higher energy is produced with the MPPT operating without any  $V_b$  perturbation.

To address this problem, there are two classical approaches: adopt large electrolytic capacitors  $C_b$  to reduce  $V_b$  perturbations [7], or adopt mode (b), as in figure 1, to mitigate the DC-link voltage oscillations [3]. The use of electrolytic capacitors introduces reliability problems [7], and the use of classical controllers reduces the solution generality since their design depends on the system parameters and operating point. Therefore, this paper proposes a compensation technique, independent from the system parameters, to mitigate the DC-link voltage oscillations generated by using non-electrolytic capacitors with the dc/dc converter operating in CCM. In addition, the proposed solution can be easily integrated in classical mode (a) PV systems since it considers the compensation of the duty cycle instead of the PV voltage as in mode (b).

### PV systems small-signal models

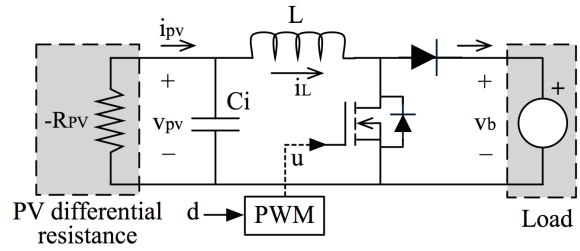
In the PV system presented in figure 1, the PV panel small-signal model corresponds to a differential resistance  $R_{pv}$  [2, 3] as in (3). Moreover, the closed loop inverter of figure 1 regulates the DC component of the DC-link voltage to ensure the required input voltage for its operation, and it is typically modeled by a voltage source acting as a load for the dc/dc converter [1, 3].

$$R_{pv} = V_{pv} / I_{pv} \quad (3)$$

In the following, the small-signal models of step-up, step-down, and step-up-down PV systems, without the MPPT controller, are analyzed considering dc/dc converters operating in CCM.

#### Boost based PV system

The electrical scheme of a step-up PV system based on a Boost converter is presented in figure 4, where  $u$  represents the Mosfet gate signal and  $i_L$  the inductor current.



**Figure 4** Boost based PV system: circuitual scheme

The PV system is modeled in state space representation (4) considering the states vector  $\mathbf{X}$ , inputs vector  $\mathbf{U}$ , and output vector  $\mathbf{Y}$  as in (5). Using the average modeling approximation [5], the state spaces matrices  $\mathbf{A}_m$ ,  $\mathbf{B}_m$ ,  $\mathbf{C}_m$ , and  $\mathbf{D}_m$  are given in (6) and (7).

$$\dot{\mathbf{X}} = \mathbf{A}_m \mathbf{X} + \mathbf{B}_m \mathbf{U}, \quad \mathbf{Y} = \mathbf{C}_m \mathbf{X} + \mathbf{D}_m \mathbf{U} \quad (4)$$

$$\mathbf{X} = [i_L \quad v_{pv}]^T, \quad \mathbf{U} = [d \quad v_b]^T, \quad \mathbf{Y} = [v_{pv}] \quad (5)$$

$$\mathbf{A}_m = \begin{bmatrix} 0 & 1/L \\ -1/C_i & -1/(R_{pv} \cdot C_i) \end{bmatrix}, \quad (6)$$

$$\mathbf{B}_m = \begin{bmatrix} v_b / L & -(1-d)/L \\ 0 & 0 \end{bmatrix}$$

$$\mathbf{C}_m = [0 \quad 1], \quad \mathbf{D}_m = [0 \quad 0] \quad (7)$$

In order to analyze the small-signal behavior and stability, the previous model is linearized around an arbitrary desired operating point. This is done by considering the DC-link voltage equal to its DC component  $V_0$  and the PV voltage equal to the desired one  $V_{pv0}$ . Moreover, the system equilibrium point is found from (4) by considering null the states derivatives, obtaining the following steady state duty cycle  $D_0$  and inductor current  $I_L$ :

$$D_0 = 1 - V_{pv0} / V_0, \quad I_L = V_{pv0} / R_{pv} \quad (8)$$

The small-signal transfer functions between  $v_{pv}$  and  $d$ ,  $G_{pvd}(s)$ , and  $v_b$ ,  $G_{pvb}(s)$ , are:

$$G_{PVd}(s) = \frac{R_{PV} \cdot V_0}{L \cdot R_{PV} \cdot C_i \cdot s^2 + L \cdot s + R_{PV}}, \quad (9)$$

$$G_{PVb}(s) = \frac{R_{PV} \cdot V_{PV0} / V_0}{L \cdot R_{PV} \cdot C_i \cdot s^2 + L \cdot s + R_{PV}}$$

### Buck based PV system

The electrical scheme of a step-down PV system based on a Buck converter is presented in figure 5 with the same considerations previously used for the Boost case.

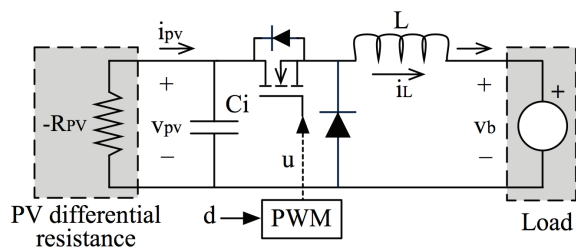


Figure 5 Buck based PV system: circuitual scheme

The state space representation (4) of the PV system, considering  $\mathbf{X}$ ,  $\mathbf{U}$ , and  $\mathbf{Y}$  as in (5) is given by the matrices  $\mathbf{A}_m$ ,  $\mathbf{B}_m$ ,  $\mathbf{C}_m$ , and  $\mathbf{D}_m$  reported in (10) and (11).

$$\mathbf{A}_m = \begin{bmatrix} 0 & d/L \\ -d/C_i & -1/(R_{PV} \cdot C_i) \end{bmatrix}, \quad (10)$$

$$\mathbf{B}_m = \begin{bmatrix} v_{PV}/L & -1/L \\ -i_L/C_i & 0 \end{bmatrix}$$

$$\mathbf{C}_m = [0 \ 1], \quad \mathbf{D}_m = [0 \ 0] \quad (11)$$

The equilibrium point is defined by the steady state duty cycle and inductor current given in (12). Moreover, the transfer functions between  $v_{PV}$  and  $d$ ,  $G_{PVd}(s)$ , and  $v_b$ ,  $G_{PVb}(s)$ , are given in (13).

$$D_0 = V_0 / V_{PV0}, \quad I_L = V_{PV0} / (R_{PV} \cdot D_0) \quad (12)$$

$$G_{PVd}(s) = \frac{(V_{PV0}^2 / V_0) \cdot (V_{PV0}^2 \cdot L \cdot s - V_0^2 \cdot R_{PV})}{V_{PV0}^2 \cdot L \cdot R_{PV} \cdot C_i \cdot s^2 + V_{PV0}^2 \cdot L \cdot s + V_0^2 \cdot R_{PV}}, \quad (13)$$

$$G_{PVb}(s) = \frac{R_{PV} \cdot V_{PV0} \cdot V_0}{V_{PV0}^2 \cdot L \cdot R_{PV} \cdot C_i \cdot s^2 + V_{PV0}^2 \cdot L \cdot s + V_0^2 \cdot R_{PV}}$$

### Buck-Boost based PV system

The electrical scheme of a step-up-down PV system based on a non-inverting Buck-Boost converter is presented in figure 6 with the same considerations adopted for the Boost case.

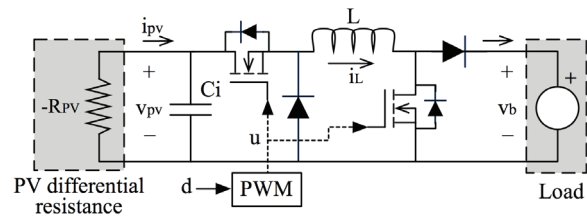


Figure 6 Buck-Boost based PV system: circuitual scheme

The state space representation (4) of the PV system, considering  $\mathbf{X}$ ,  $\mathbf{U}$ , and  $\mathbf{Y}$  as in (5), is given by the matrices  $\mathbf{A}_m$ ,  $\mathbf{B}_m$ ,  $\mathbf{C}_m$ , and  $\mathbf{D}_m$  reported in (14) and (15).

$$\mathbf{A}_m = \begin{bmatrix} 0 & d/L \\ -d/C_i & 1/(R_{PV} \cdot C_i) \end{bmatrix}, \quad (14)$$

$$\mathbf{B}_m = \begin{bmatrix} (v_{PV} + v_b)/L & -(1-d)/L \\ -i_L/C_i & 0 \end{bmatrix}$$

$$\mathbf{C}_m = [0 \ 1], \quad \mathbf{D}_m = [0 \ 0] \quad (15)$$

The equilibrium point is defined by its duty cycle and inductor current given in (16), and the transfer functions between  $v_{PV}$  and  $d$ ,  $G_{PVd}(s)$ , and  $v_b$ ,  $G_{PVb}(s)$ , are given in (17).

$$D_0 = V_0 / (V_0 + V_{PV0}), \quad I_L = V_{PV0} / (R_{PV} \cdot D_0) \quad (16)$$

$$G_{PVd}(s) = \frac{V_{PV0} \cdot (\lambda \cdot V_0 + 3 \cdot \psi \cdot V_0 + 3 \cdot \psi \cdot V_{PV0}^2 + \delta \cdot V_{PV0}) \cdot s - (\phi \cdot V_0^2 - 2 \cdot \phi \cdot V_0 \cdot V_{PV0} - \phi \cdot V_{PV0}^2)}{V_0 \cdot (\alpha + \beta_i + \phi) \cdot s^2 + V_0 \cdot (\lambda + 2 \cdot \psi + \delta) \cdot s + V_0 \cdot \phi},$$

$$G_{PVb}(s) = \frac{R_{PV} \cdot V_{PV0} \cdot V_0}{(\alpha + \beta_i + \phi) \cdot s^2 + (\lambda + 2 \cdot \psi + \delta) \cdot s + \phi}, \quad (17)$$

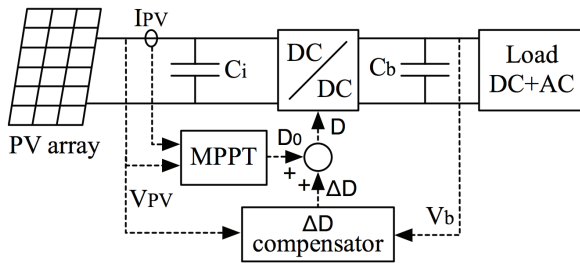
$$\alpha = V_0^2 \cdot L \cdot R_{PV} \cdot C_i, \beta = 2 \cdot V_0 \cdot L \cdot R_{PV} \cdot V_{PV0} \cdot C_i, \phi = L \cdot R_{PV} \cdot V_{PV0}^2 \cdot C_i$$

$$\lambda = V_0^2 \cdot L, \psi = V_0 \cdot L \cdot V_{PV0}, \delta = L \cdot V_{PV0}^2, \phi = V_0^2 \cdot R_{PV}$$

### DC-link voltage oscillations compensator

From the basic relation between the input and output ports of the dc/dc converter given in (1), it is noted that any oscillation at  $V_b$  is transmitted to  $V_{PV}$  if the converter input/output voltages ratio  $M(D)$  is constant. Moreover,  $M(D)$  is a non-linear function that depends exclusively on the duty cycle  $D$  if parasitic losses are not considered. Therefore, constant  $D$  generates constant  $M(D)$ .

Since the MPPT controller provides the steady state duty cycle  $D_0$  aimed at maximizing the PV power production, as in mode (a) of figure 1, an additional component  $\Delta D$  must be added to the duty cycle to compensate the voltage oscillations  $\Delta V_b$  at the DC-link. Such compensation architecture is presented in figure 7.



**Figure 7** Compensator architecture

From the analyses of Boost, Buck and Buck-Boost PV systems previously presented,

$$\Delta D = \begin{cases} (V_{PV} \cdot \Delta V_b) / (V_b \cdot V_0), & \text{for Boost} \\ \Delta V_b / V_{PV}, & \text{for Buck} \\ (V_{PV} \cdot \Delta V_b) / [(V_b + V_{PV}) \cdot (V_0 + V_{PV})], & \text{for Buck - Boost} \end{cases} \quad (22)$$

assuming the states derivatives equal to zero to obtain the steady state relations for any  $V_{PV}$  and  $V_b$  conditions, the duty cycle for the Boost, Buck and Buck-Boost converters are:

$$D = \begin{cases} 1 - V_{PV} / V_b, & \text{for Boost} \\ V_b / V_{PV}, & \text{for Buck} \\ V_b / (V_b + V_{PV}), & \text{for Buck - Boost} \end{cases} \quad (18)$$

In addition, the duty cycle of the converters to obtain the desired  $V_{PV0}$  voltage at the PV panel terminals from the DC component  $V_0$  of the DC-link voltage, are:

$$D_0 = \begin{cases} 1 - V_{PV0} / V_0, & \text{for Boost} \\ V_0 / V_{PV0}, & \text{for Buck} \\ V_0 / (V_0 + V_{PV0}), & \text{for Buck - Boost} \end{cases} \quad (19)$$

Since the DC-link voltage exhibits both  $V_0$  and  $\Delta V_b$  components (20), the duty cycle must to exhibit the additional  $\Delta D$  component given in (21) to mitigate the DC-link oscillations. Such a duty cycle compensation for Boost, Buck and Buck-Boost converters is given in (22).

$$V_b = V_0 + \Delta V_b \quad (20)$$

$$\Delta D = D - D_0 \quad (21)$$

### Stability analysis

To provide a stability analysis, the small-signal models of the PV systems, considering the duty cycle compensation, are obtained. Moreover, the oscillation component  $\Delta V_b$  of the DC-link must be obtained by means of an arbitrary order band-pass filter. The duty cycle compensation  $\Delta d$  is calculated by considering a correct operation of

the compensation technique, so  $v_{PV} = V_{PV0}$ , and a small-signal perturbation  $\Delta v_b$ , therefore  $V_b \approx V_0$ . The band-pass filter used to obtain  $\Delta v_b$  is:

$$\Delta v_b(s) = G_{nf}(s) \cdot v_b(s) \quad (23)$$

From such considerations, and replacing (23) in (22), the small-signal compensations  $\Delta d$  are:

$$\Delta d(s) = K_{sa} \cdot G_{nf}(s) \cdot v_b(s), \quad \begin{cases} K_{sa} = V_{PV0}/V_0^2 \text{ for Boost} \\ K_{sa} = 1/V_{PV0} \text{ for Buck} \\ K_{sa} = V_{PV0}/(V_{PV0} + V_0)^2 \text{ for Buck - Boost} \end{cases} \quad (24)$$

Figure 8 presents the block diagram of the small-signal model, where the compensated transfer

functions from  $d_0$  and  $v_b$  to the output  $v_{PV}$ ,  $T_{PVd}(s)$  and  $T_{PVb}(s)$  respectively, are given in (25).

$$\begin{aligned} T_{PVd}(s) &= v_{PV}(s)/d_0(s) = G_{PVd}(s), \\ T_{PVb}(s) &= v_{PV}(s)/v_b(s) = G_{PVb}(s) + G_{PVd}(s) \cdot G_{nf}(s) \cdot K_{sa} \end{aligned} \quad (25)$$

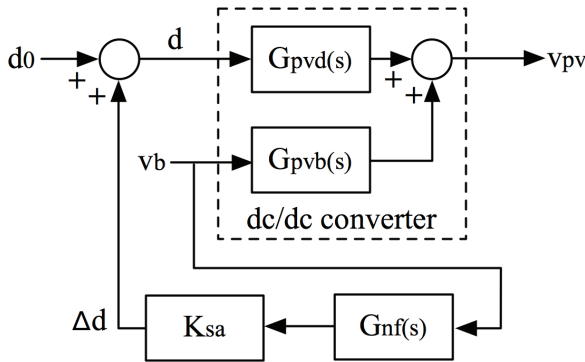


Figure 8 Small-signal block diagram

Generalizing the transfer functions of the dc/dc converter and filter as in (26), the compensated transfer functions (25) are expanded as in (27). Therefore, the poles of the compensated transfer functions correspond to the open loop poles of the dc/dc converter and filter, which are always stable [5], and the compensated system will be stable regardless the converter topology. Such a condition permits to adopt the proposed technique to any PV system based on a dc/dc converter.

$$G_{PVd}(s) = P_{PVd}(s)/Q_{PVd}(s), \quad G_{PVb}(s) = P_{PVb}(s)/Q_{PVb}(s), \quad G_{nf}(s) = P_{nf}(s)/Q_{nf}(s) \quad (26)$$

$$\begin{aligned} T_{PVd}(s) &= P_{PVd}(s)/Q_{PVd}(s), \\ T_{PVb}(s) &= \frac{P_{PVb}(s) \cdot Q_{PVd}(s) \cdot Q_{nf}(s) + P_{PVd}(s) \cdot P_{nf}(s) \cdot Q_{PVb}(s) \cdot K_{sa}}{Q_{PVb}(s) \cdot Q_{PVd}(s) \cdot Q_{nf}(s)} \end{aligned} \quad (27)$$

To illustrate the system stability, a second order filter is adopted (28), where B represents the -3 dB bandwidth of the band-pass filter and  $\omega_0$  the center frequency in rad/s.

$$G_{nf}(s) = \frac{k_f \cdot B \cdot s}{s^2 + B \cdot s + \omega_0^2} \quad (28)$$

The poles of  $G_{nf}(s)$ ,  $T_{PVb}(s)$  and  $T_{PVd}(s)$  for the Boost, Buck and Buck-Boost converters are

given in (29) and (30), where it is confirmed that both  $T_{PVb}(s)$  and  $T_{PVd}(s)$  are always stable since the real parts of  $s_{nf}$ ,  $s_{PVd}$  and  $s_{PVb}$  are negative for

$$s_{nf} = \left( -B \pm \sqrt{B^2 - 4 \cdot \omega_0^2} \right) / 2 \quad (29)$$

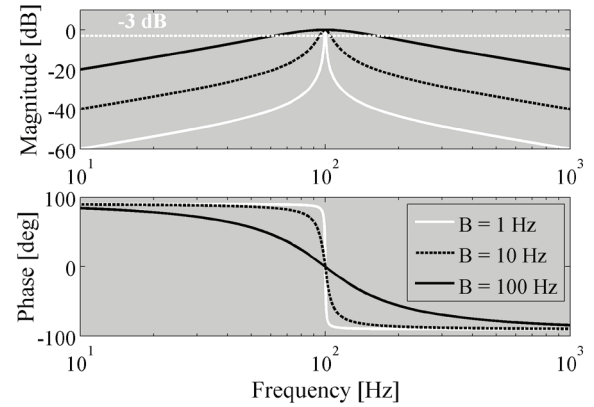
$$s_{PVd} = s_{PVb} = \begin{cases} \frac{-L \pm \sqrt{L^2 - 4 \cdot L \cdot C_i \cdot R_{PV}^2}}{2 \cdot L \cdot C_i \cdot R_{PV}}, & \text{for Boost} \\ \frac{-L \cdot V_{PV0} \pm \sqrt{L^2 \cdot V_{PV0}^2 - 4 \cdot L \cdot C_i \cdot R_{PV}^2 \cdot V_0^2}}{2 \cdot L \cdot C_i \cdot R_{PV} \cdot V_{PV0}}, & \text{for Buck} \\ \frac{-L \cdot (V_{PV0} + V_0) \pm \sqrt{L^2 \cdot (V_{PV0} + V_0)^2 - 4 \cdot L \cdot C_i \cdot R_{PV}^2 \cdot V_0^2}}{2 \cdot L \cdot C_i \cdot R_{PV} \cdot (V_{PV0} + V_0)}, & \text{for Buck - Boost} \end{cases} \quad (30)$$

### Band-pass filter design

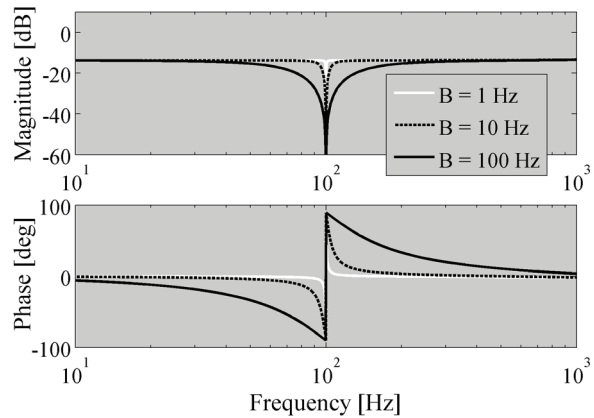
The center frequency  $\omega_0$  of the band-pass filter must be set at the double of the grid frequency, 100 Hz in Europe and 120 Hz in America. The bandwidth  $B$  must be set in agreement with the grid frequency oscillations, but in general a larger  $B$  provides a better mitigation of  $\Delta V_b$  oscillations since more frequencies are filtered. The effect of  $B$  on both the band-pass filter and the compensated system frequency responses is illustrated in figure 9, it considering a Boost converter and the following parameters:  $V_{PV0} = 28.7$  V,  $V_0 = 140$  V,  $I_{PV}$  at  $V_{PV0} = 3.7$  A,  $I_{SC} = 5$  A,  $C_i = 22$   $\mu$ F,  $L = 47$   $\mu$ H,  $\omega_0 = 2 \times n(\pi) \times 100$  rad/s,  $k_i = 1$ , and a  $F_{sw} = 50$  kHz switching frequency.

Figure 9 shows that for any value of  $B$ , the compensated PV system accurately rejects the frequency component selected by  $\omega_0$ , but a larger  $B$  provides robustness against grid frequency variation. Moreover, equation (27) and figure 9 also show that additional band-pass filters can be introduced to reject multiple components, i.e. grid noise injected by electromechanical machines.

positive values of  $B$ ,  $L$ ,  $C_i$ ,  $V_{PV0}$ ,  $V_0$ , and  $R_{PV}$ .  $R_{PV}$  is always positive because  $I_{PV} > 0$  (3). Therefore, the compensated system is always stable.



(a) Band-pass filter

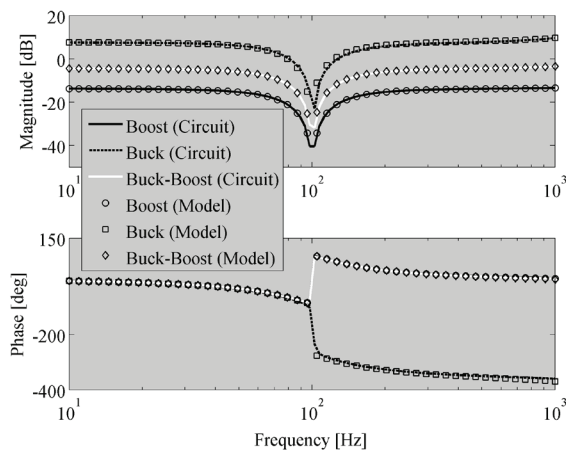


(b) Compensated PV system

**Figure 9** Effect of the Band-pass filter bandwidth



Finally, figure 10 presents the frequency responses of the compensated PV systems based on Boost, Buck, and Buck-Boost converters. Such diagrams were obtained by simulating the non-linear circuits and compensators in the power electronics simulator PSIM, and by means of the small-signal models calculated in (27). It is noted the accurate representation of the non-linear circuits provided by the models, which confirms the validity of the previous analyses.



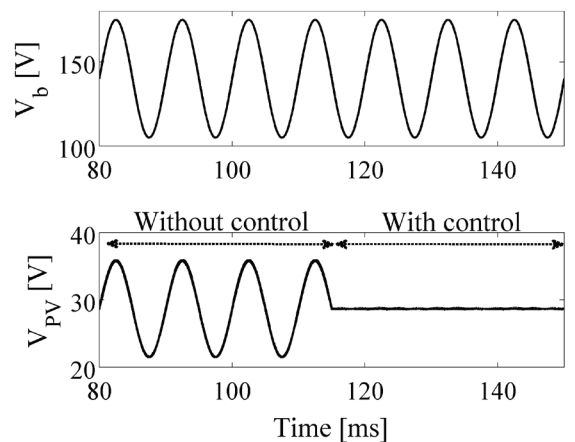
**Figure 10** PV systems frequency responses: circuit and model comparison

### Simulation results

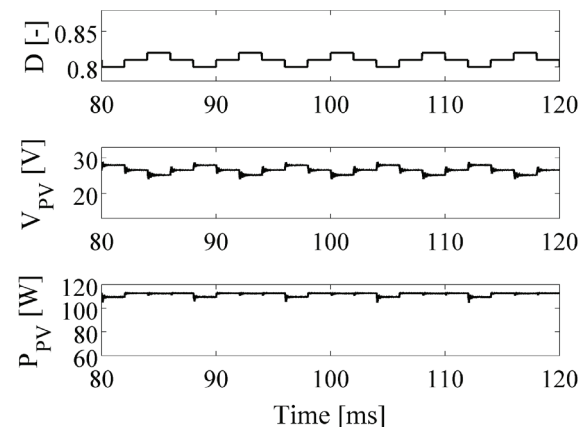
The effectiveness of the compensation technique was tested using the parameters previously defined for the Boost case with  $B = 2 \times \pi \times 100$  rad/s,  $V_0 = 12$  V for the Buck case and  $V_0 = 48$  V for the Buck-Boost case. Such conditions guarantee the consistency of the simulation results. Moreover, a 100 Hz oscillation on the DC-link voltage, with a peak-to-peak amplitude of 50 % of the DC voltage, was considered to test the compensation systems.

Figure 11(a) shows the simulation of the Boost-based PV system where, as predicted in figure 10, the 100 Hz  $\Delta V_b$  perturbation is successfully mitigated. The figure also permits to contrast the system behavior with and without compensation. Figure 11(b) confirms that the compensated system of figure 7 is able to operate with a traditional

MPPT controller in the same way as in classical mode (a), rejecting the effect of oscillations at the DC-link. In such a simulation the same MPPT controller used in figure 2 was considered, obtaining the same power but in presence of a 50 %  $\Delta V_b$  perturbation. Such a condition makes possible to adopt non-electrolytic capacitors.



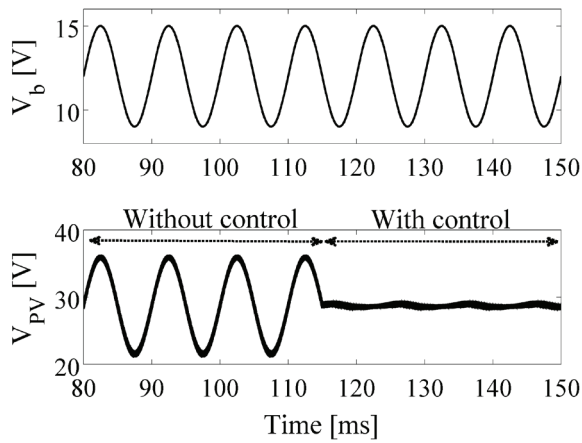
(a) Mitigation of the  $V_b$  perturbation



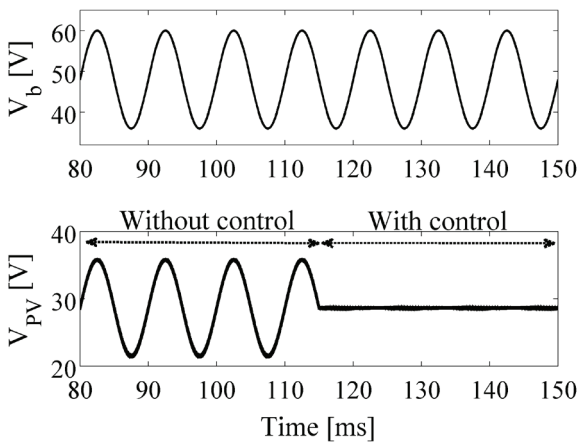
(b) MPPT operation

**Figure 11** Boost based PV system control

Similarly, figure 12 shows the simulation of the PV systems based on Buck and Buck-Boost converters. As predicted in figure 10, the 100 Hz  $\Delta V_b$  perturbation is successfully mitigated in both cases by means of the calculated  $\Delta D$  compensators. It is noted a higher ripple in the Buck case since the same capacitor was used for all the converters to provide a fair comparison.



(a) Buck based system



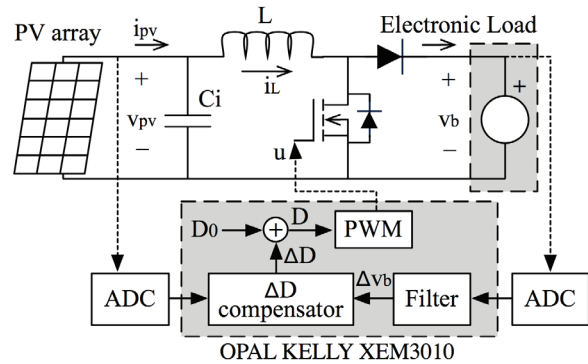
(b) Buck-Boost based system

**Figure 12** Control of Buck and Buck-Boost based PV systems: mitigation of the  $V_b$  perturbation

### Experimental results

The behavior predicted by the analytical and simulation results was experimentally verified. The correctness of the approach was illustrated by means of a *proof of concept* PV system based on a Boost converter, which requires a low-side circuitry for driving the active devices, simplifying the practical implementation in comparison to the Buck and Buck-Boost cases. The applicability of the proposed duty cycle compensations to the Buck and Buck-Boost cases has been demonstrated by means of the simulation results. Figure 13(a) shows the block diagram of the experimental system using

a Kyocera KC120 PV panel and an electronic load that imposes a 50 %  $\Delta V_b$  perturbation at 100 Hz. The duty cycle compensation is calculated in a Xilinx Spartan3 XC3S1500 FPGA mounted in an Opal Kelly XEM 3010 board [8], and the PV and  $V_b$  voltages are acquired by means of an Analog to Digital Converter (ADC). In addition, the band-pass filter, the PWM, and the steady state duty cycle  $D_0$  are programmed inside the FPGA. Finally, the laboratory setup is presented in figure 13(b).



(a) Block diagram

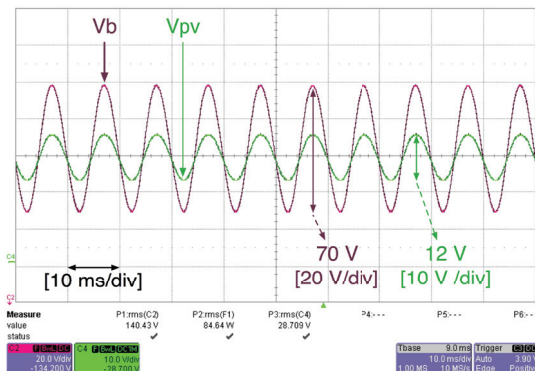


(b) Laboratory setup

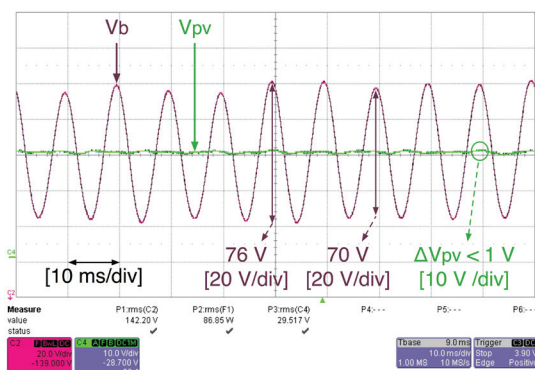
**Figure 13** Experimental system

Figure 14(a) shows the PV system operation without the duty cycle compensation exhibiting the propagation of the 100 Hz oscillations from the DC-link to the PV panel terminals. Instead, figure 14(b) shows the PV system operation using the duty cycle compensation, where the  $V_b$

perturbations were attenuated to less than 1 V, which is acceptable since the DC-link oscillations exhibit additional low frequency components generated by the electronic load current absorption.



(a) Without duty cycle compensation



(b) With duty cycle compensation

Figure 14 Experimental results

## Conclusions

A duty cycle compensation technique to mitigate the effect of DC-link voltage oscillations on PV systems has been presented. Explicit design equations have been provided for systems based on Boost, Buck and Buck-Boost dc/dc converters operating in CCM. Such equations do not depend on the systems parameters, therefore they are applicable to any system exhibiting the same circuitry. If discontinuous conduction mode [5] is required, different equations must be derived. Small-signal models of the PV systems have been calculated, demonstrating the stability of the compensated systems. In addition, the compensators have been validated by means of

simulation results, and satisfactory experimental results have confirmed the correctness of the technique. Finally, the duty cycle compensation can be improved by considering parasitic elements, additional dc/dc converter topologies, and the operation in discontinuous conduction mode.

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