High-Andean fruits are considered important for their domestic consumption and exportation potential. Among them, purple passion fruit (*Passiflora edulis* Sims) is largely accepted in European markets. However, its short shelf life, worsened with the limited knowledge of the species lead to rapid fruit deterioration. An important contribution to the development of this crop is fruit growth mathematical modeling, which allows estimating harvest related issues, in order to define applicable agronomic management protocols. Periodic destructive sampling was employed to investigate fruits of known age corresponding to ten purple passion fruit materials from the Colombian departments of Antioquia, Putumayo and Nariño. The fruits were analyzed for dry weight, polar and equatorial diameters, thermal time (TT) and relative growth rate (RGR). In order to assess fruit growth, some nonlinear models were fitted using time after flowering (DAF) to predict dry weight and polar and equatorial diameters. For each response, the best fitting model was chosen according to homogeneous distribution of residuals, higher coefficient of determination for prediction ($R^2_{\text{prediction}}$), and smaller Mean Square Error and PRESS values. RGR was used to identify and describe fruit growth stages, while the TT was employed as a complementary measure to compare fruit ripening stages. The studied parameters were satisfactorily explained by Weber’s Monomolecular model. Based on the models adjusted for fruit growth, it can be concluded that harvest must be carried out between days 85 - 90 after full bloom.

Key words: Growth dynamics, fruit development, tropical fruits, Passifloraceae.
ajustados, se puede inferir que la cosecha debe realizarse entre los 85 y 90 días siguientes a la plena floración.

Palabras clave: Dinámica del crecimiento, desarrollo del fruto, frutas tropicales, pasifloras.

INTRODUCTION

Usually marketed fresh, high-Andean fruits are highly demanded by consumers. Their short shelf life determines rapid deterioration of physiological functions, which affects fruit quality and makes it necessary to conduct characterization studies on the physical, physiological and biochemical processes that accompany the ripening process (Andrade-Cuvi et al. 2013; Ramirez et al. 2013; Torres et al. 2013). A wide range of fruit species with potential to be developed as commercial crops has been recognized in the Colombian Andes (Schotsmans & Fischer, 2011; Lagos-Santander et al. 2013; Llanos et al. 2013; Abreu et al. 2014). Among them, purple passion fruit (Passiflora edulis Sims) exists, most of which production is currently exported, amounting 3,319 t in 2012, traded for an FOB value of U.S. $ 15,766.034, mostly to European markets (CCB, 2014).

Following Aristizábal (2003), studies about fruit growth (mainly dealing with irreversible size and dry weight increase) and development (gradual change in size, structure and function) are important to assess optimum ripening stage (Cañizares et al. 2003; Tapia et al. 1998), determine growth behavior through time, estimate fruit size (Avanza et al. 2008) and weight (Coome, 1976) at harvest, propose agricultural management strategies (Rojas et al. 2008; Casieria & Cardozo, 2009), establish phenological stages, and analyze fruit formation and structural development (Mazorra et al. 2006).

A mathematical model allows synthesizing and increasing knowledge about a given system (López et al. 2005), evaluating potential management strategies and estimating potential yield, costs and benefits obtained with the use of specific practices such as fertilization, irrigation, or even commercial transactions (Cañizares et al. 2003; Tapia et al. 1993). Among the non-linear models used to characterize growth and/or development as functions of time, the logistic, monomolecular, exponential (Aristizábal, 2003; Rojas et al. 2008) and Michaelis-Menten (Rojas et al. 2008) models hold an outstanding place.

Characterized by its sigmoid shape, the logistic model results from the combination of the exponential and monomolecular models, separated by an inflection point. The exponential model describes steady growth progress (decline) (Rojas et al. 2008) as the result of previously accumulated (lost) weight; thus explaining why small seeds produce smaller seedlings than those produced by medium or large seeds (Aristizábal, 2003).

The monomolecular model shows how a plant’s dry weight change rate is determined by future growth, thus estimating growth rates steady decline as the fruit reaches full size (Aristizábal, 2003). It has been used to estimate the growth of different plant and pathogen structures, as is the case of sweet orange (Citrus sinensis var. Valencia Late) fruit growth, modeled by Avanza et al. (2008). These authors resorted to diameter as a function of days after full flowering, as represented by the equation Diameter (mm) =G \left[1−\beta e^{\left(\text{YDDP}F\right)}\right].

Rojas et al. (2008) estimated fresh weight of Manzano hot pepper (Capsicum pubescens) through the function \( Y = a(1-e^b) \), by measuring non-destructive parameters such as water volume displaced by the fruit in a graduated cylinder. Costa et al. (2002) have observed that Mitscherlich’s monomolecular model can be applied to the simulation of disease progress, prevention and resulting damage and losses. In this case, disease progress rate is proportional to initial inoculum amount and progress rate, both assumed to be constant. The equation that describes the model is \( \frac{dx}{dt} = rM \left(1-x\right) \), \( rM \) being the specific rate for this model (\( rM = \text{initial inoculum} \times \text{rate} \)), and \( (1-x) \) representing the healthy tissue. Michaelis-Menten’s model is recommended to describe plant growth in response to limiting factor increases (Mancera et al. 2003).

Replacing the Gaussian function coefficients with mathematical functions that include the effect of population density, Villegas et al. (2004) obtained kinetic models that simulate total biomass growth in tomato (Solanum lycopersicum) cv. Gabriela, under greenhouse conditions and defined agronomic management. Tapia et al. (1993) adjusted equations proposed by Bailey & Clutter (1974) to explain the development of equatorial diameter and age in olives (Olea europaea). In the same vein, Cañizares et al. (2003) described the growth of the fruit of guava (Psidium guajava) with a double sigmoid curve. In turn, Casieria & Cardozo (2009) adjusted cubic models to fruits of tomato cv. Quindio, grown in open field conditions. Finally, Rojas et al. (2008) recommend the monomolecular model to estimate fruit dry weight increase in Manzano hot pepper by means of a single non-destructive parameter: water volume displaced by the fruit in a graduated cylinder.

Shiomi et al. (1996) and Carvajal et al. (2012) observed a rapid length and diameter increase in fruits of purple passion fruit around the 20th day after flowering (DAF), and considered it as a species-specific pattern. Fruit weight in this crop was observed to increase until 20 DAF (Shiomi et al. 1996), whereas Carvajal et al. (2012) found this rise to continue until 42 DAF, followed by a more gradual progress towards the ripening period. Shiomi et al. (1996) also reported a second weight rise, probably due to juice accumulation. While some fruits such as peach (Prunus persica) (Salisbury & Ross,
1994) exhibit double sigmoid growth, others have simple sigmoid growth, as is the case of passion fruit (*Passiflora edulis*) (Lederman & Gazit, 1993), champa (*Campomanesia lineatifolia*) (Álvarez et al. 2009) and star fruit (*Averrhoa carambola*) (González et al. 2001). Thus, based on non-linear models, the objective of this study was to model purple passion fruit growth to serve as a reference in planning of cultural practices associated with the harvest.

**MATERIALS AND METHODS**

The evaluated crop was grown in the municipality of Rionegro, rural settlement of Llanogrande, department of Antioquia, at La Selva Research Center of Corporación Colombiana de Investigación Agropecuaria – Corpoica (6°7’ 49.9” N, 75°24.9’ W; 2,090 m.a.s.l.). Climatic parameter yearly average scores were: temperature, 17°C; precipitation, 1,917 mm; relative humidity (RH), 78%; sunshine, 1,726 hours year⁻¹; evapotranspiration, 1,202 mm. The climate corresponds to a Lower Montane Rain Forest. The trial was conducted in an experimental area where 10 purple passion fruit accessions were randomly planted. The materials are part of the Colombian Gene Bank (administered by Corpoica), which after Amplified Length Polymorphism (AFLP) and Simple Sequence Repeat (SSR) molecular analysis, was reported to have low genetic variability (Ortiz et al. 2012). Fruit tracking was done by labeling flowers with and without herkogamy at their homogamous phase, making use of colored threads (Ángel et al. 2011). Fruit age was measured in days after flowering (DAF), corresponding the day of flower labeling to day zero (0 DAF).

Destructive samplings were carried out every seven days for a period of 16 weeks, starting on 7 DAF, and finishing on 112 DAF. Each sampling consisted in ten randomly chosen fruits. The samples were transported in expanded polystyrene boxes containing dry ice to keep an internal temperature of 4°C. Fruit parameters determination was carried out at the post-harvest laboratory of Corpoica, under average temperature and relative humidity (RH) conditions of 20°C and 70%, respectively.

The following variables were recorded:

**Dry weight (DW).** Expressed in grams. This parameter was obtained after oven dry fruits at 70°C. until they reached constant weight.

**Polar (PD) and equatorial (ED) diameters.** These parameters were measured in centimeters on each fruit, with a digital L&W Tools™ caliper. Polar diameter was taken from the peduncle insertion scar to the opposite extreme of the fruit. Equatorial diameter was taken along the widest belt of the fruit.

**Thermal Time (TT).** This concept is based on the notion that in order to shift from one growing stage to another, plants need to accumulate minimum amounts of temperature. In consonance with Fischer et al. (2009), the base temperature (*Tb*) has been fixed at 10°C. Conceptually, base temperature is the temperature at which development stops through cold. In the current study, TT (expressed as Growing Degree Days - GDDs) was calculated according to the simple triangle methodology proposed by the University of California (2013).

**Relative Growth Rate (RGR).** This parameter addresses dry weight increment per initial weight unit along a given time period. It was deduced through the following equation:

\[
RGR = \frac{\ln(W_2) - \ln(W_1)}{t_2 - t_1}
\]

*Ln = Natural logarithm; Wᵰ = Initial weight; W₂ = Final weight; tᵰ = Starting time; t₂ = Final time*

Fruit growth analysis was preceded by the evaluation of the non-linear models reported by Kiviste et al. (2002). Each model was adjusted for dry weight, polar diameter and equatorial diameter, always using DAF as the predictive variable. For each response variable, we chose the best fitting model, *i.e.*, the one offering the most homogeneous residual distribution, the highest predicted coefficient of determination (*R²* prediction), and the lowest values of the PRESS statistic and Mean Square Error. RGR was used to limit and describe the different fruit growth stages, whereas TT was employed as a complementary measure to compare fruit ripening stages.

**RESULTS AND DISCUSSION**

**Dry weight.** Purple passion fruit increased during all the growing stage. Growth is mainly due to cell division until it reaches an ED of 4.72cm and a PD of 5.46 cm. From then on, size increment is the result of cell elongation taking place mainly at the mesocarp (González et al. 2001).

Three growing periods were identified: an initial stage went until 14 DAF, with a RGR of 0.319 g day⁻¹; the second stage took up to 28 DAF, with a RGR of 0.065 g day⁻¹; and the final stage took up to 112 DAF, RGR being 0.0255 g day⁻¹ (Figure 1). This indicates that growth takes place mainly during the first month. RGR approached zero at about 91 DAF. Hence, under the conditions of the current study, fruit harvest can be carried out at 85 – 90 DAF, when accumulated TT was 589.73 and 635.23 GDDs.

In studying purple passion fruits, Shiomi et al. (1996) observed a rapid fresh weight increase that lasted until 20 DAF and went on at a slow pace until ripening. Flórez et al. (2012)...
report an 85 – 90 DAF period before reaching physiological maturity, corroborated through seed characteristics, which, in contrast to previous stages, corresponded to a hard, black seed coat. That work also reports inter-cellular space enlargement inside the fruit during the first 20 to 35 DAF. Carvajal et al. (2012) observed physiological maturity at around 80 DAF, whereas Pinzón et al. (2007) recommend stage three of the fruit color scale they developed as the optimum harvest moment, but they do not mention any approximate fruit age.

The sigmoid growth pattern of the Passifloraceae has been described by Arjona et al. (1991), Lederman & Gazit (1993), Pocasangre et al. (1995), Gómez et al. (1999), Villanueva et al. (1999) and García (2008). In accordance with the results of the current study, Shiomi et al. (1996) found the same tendency in purple passion fruit. Dry weight evolution was adjusted to a simple sigmoid Weber monomolecular model with a $R^2_{\text{prediction}}$ value of 0.92 (Table 1; Figure 2).

Table 1. Estimators of Weber’s monomolecular model parameters $Y = a(1-e^{b+c})$ and goodness of fit statistics employed for purple passion fruit (*Passiflora edulis* Sims) growth analysis.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Model parameters</th>
<th>$\sum_i \left( \frac{r_i}{1-h_i} \right)^2$</th>
<th>Mean Square Error</th>
<th>$R^2_{\text{prediction}}$</th>
</tr>
</thead>
</table>
| Dry weight        | $a=18.3726$  
|                   | $b=0.0526$    
|                   | $c=0.0104$    | 165.438                  | 1.05337              | 0.92459                |
| Equatorial diameter | $a=5.3015$  
|                   | $b=0.2726$    
|                   | $c=0.0954$    | 12.8769                  | 0.28008              | 0.91515                |
| Polar diameter    | $a=5.7760$  
|                   | $b=0.8810$    
|                   | $c=0.1926$    | 13.8462                  | 0.29319              | 0.90046                |

Figure 1. Relative growth rate in purple passion fruits (*Passiflora edulis* Sims).
Other authors have described this same parameter through different models. Almanza et al. (2009) adjusted a logistic model to grape (*Vitis vinifera*) growth; González et al. (2001) adapted a polynomial model in star fruit; Casierra & Cardozo (2009) fitted a cubic model in tomato cv. Quindío; Hernández & Martínez (1994) developed a quadratic model for tree tomato; and Rodríguez et al. (2006) generated a cubic model for pineapple guava (*Acca sellowiana*). All these models exhibited large $R^2$ values, thus showing their remarkable predictive capacity.

**Polar diameter.** This parameter was fitted by a simple sigmoid Weber monomolecular model with a $R^2$ prediction value of 0.90 (Table 1; Figure 3). Swift growth lasted until 21 DAF, when it tended to stabilize, as also observed by Shiomi et al. (1996), Carvajal et al. (2012) and Flórez et al. (2012) in the same fruit; in passion fruit by Arjona et al. (1991), Lederman and Gazit (1993), Tapia et al. (1998) and Gómez et al. (1999); and in sweet grenadilla (*Passiflora ligularis* by García (2008). Around this time, the fruit reaches definite size, followed by cell differentiation and fruit filling, as reported by Salisbury & Ross (1994) in describing the timing of this process. The values obtained for this parameter in the current study are within the range described by Orjuela et al. (2011) (Table 2). As it is observable in this fruit’s characteristic shape, simple polar diameter was found to be larger than equatorial diameter, in agreement with reports by Gómez et al. (1999) in purple passion fruit and by García (2008) in sweet grenadilla.

**Equatorial diameter.** This parameter showed sigmoid behavior, in agreement with previous observations by Shiomi et al. (1996) in purple passion fruit, by Arjona et al. (1991) in mayop (*P. incarnate*) and purple passion fruit, and by Villanueva et al. (1999) and Gómez et al. (1999) in yellow passion fruit. In the mentioned species, the exponential phase occurs between seven and 15 days after anthesis, depending on the environment where the fruits have grown. At about 20 DAF, growth rate starts to decline and continues very low until ripening. After modeling equatorial diameter with Weber’s monomolecular model, García (2008) found a similar behavior in sweet grenadilla, which showed a $R^2$ value of 0.91 (Table 1; Figure 4), thus exhibiting a sigmoid growth pattern similar to that of the polar diameter and to scores reported by Orjuela et al. (2011).

In this regard, Carvajal et al. (2012) observed that purple passion fruit diameter and length underwent a rapid growth stage until the fifth week of age and then stabilized until the tenth week; which is not entirely consistent with the findings of this study. Likewise, Pincón et al. (2007) found that this plant produces fruits with respective polar and equatorial diameters of 50 and 56 mm, which decline along the ripening
Figure 3. Purple passion fruit (*Passiflora edulis* Sims) polar diameter behavior according to age. The solid line represents the function estimated by Weber’s monomolecular model. Discontinuous lines correspond to 95% confidence limits for the expected values. Circles indicate observed data.

Table 2. Mean ± standard deviation of purple passion fruit (*Passiflora edulis* Sims) physical parameters as observed through time.

<table>
<thead>
<tr>
<th>Fruit age (DAF*)</th>
<th>Equatorial diameter (cm)</th>
<th>Polar diameter (cm)</th>
<th>Dry weight (g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>1.65 ± 0.13</td>
<td>2.15 ± 0.17</td>
<td>0.21 ± 0.04</td>
</tr>
<tr>
<td>14</td>
<td>3.85 ± 0.21</td>
<td>4.91 ± 0.20</td>
<td>1.92 ± 0.23</td>
</tr>
<tr>
<td>21</td>
<td>4.72 ± 0.22</td>
<td>5.46 ± 0.22</td>
<td>3.03 ± 0.33</td>
</tr>
<tr>
<td>28</td>
<td>4.82 ± 0.17</td>
<td>5.43 ± 0.26</td>
<td>3.66 ± 0.71</td>
</tr>
<tr>
<td>35</td>
<td>5.21 ± 0.17</td>
<td>5.97 ± 0.17</td>
<td>6.33 ± 2.61</td>
</tr>
<tr>
<td>42</td>
<td>5.25 ± 0.30</td>
<td>6.05 ± 0.31</td>
<td>5.91 ± 0.76</td>
</tr>
<tr>
<td>49</td>
<td>5.40 ± 0.19</td>
<td>6.14 ± 0.20</td>
<td>6.40 ± 1.76</td>
</tr>
<tr>
<td>56</td>
<td>5.34 ± 0.14</td>
<td>5.66 ± 0.28</td>
<td>7.66 ± 0.86</td>
</tr>
<tr>
<td>63</td>
<td>5.42 ± 0.17</td>
<td>5.58 ± 0.15</td>
<td>7.89 ± 0.89</td>
</tr>
<tr>
<td>70</td>
<td>5.19 ± 0.15</td>
<td>5.79 ± 0.13</td>
<td>9.49 ± 0.91</td>
</tr>
<tr>
<td>77</td>
<td>5.08 ± 0.21</td>
<td>5.94 ± 0.34</td>
<td>9.66 ± 0.97</td>
</tr>
<tr>
<td>84</td>
<td>4.96 ± 0.25</td>
<td>5.36 ± 0.28</td>
<td>9.88 ± 1.13</td>
</tr>
<tr>
<td>91</td>
<td>5.44 ± 0.14</td>
<td>5.89 ± 0.15</td>
<td>11.78 ± 1.32</td>
</tr>
<tr>
<td>98</td>
<td>5.37 ± 0.26</td>
<td>5.72 ± 0.14</td>
<td>10.57 ± 1.95</td>
</tr>
<tr>
<td>105</td>
<td>5.33 ± 0.15</td>
<td>5.76 ± 0.30</td>
<td>12.20 ± 1.07</td>
</tr>
<tr>
<td>112</td>
<td>5.32 ± 0.20</td>
<td>5.72 ± 0.15</td>
<td>12.03 ± 0.74</td>
</tr>
</tbody>
</table>

*Days after flowering*
Franco, G.; Cartagena, J.R.; Correa, G.: Gulupa fruit growth

To summarize: the description of the fruit growth is a useful element for the future construction of a model, that achieves simulate the potential production of purple passion fruit crop. Analysis of purple passion fruit growth and development serves as a guide for scheduling crop management practices such as pruning, fertilization and irrigation, in order to optimize the source/sink relations. Nonetheless, as the plant is constantly bearing fruit at different developmental stages, the average demand is relatively constant, which is why agricultural tasks should be based on the predominant fruit developmental stage. Based on the model adjusted to fruit growth, it is possible to foresee that harvest can be scheduled on days 85 – 90 after an abundant flowering, since the equatorial and polar diameters and dry weight tended to stabilize. The values estimated by the model explain each of the variables determined in relation to field observations, therefore, properly interpret the physiological processes taking place in the fruit in each of their ages.

Conflicts of interest: The manuscript was prepared and reviewed with the participation of all the authors, who declare that no conflict of interest that threatens the validity of the results presented.

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